

The approved original version of this thesis is available at the main library of the Vienna University of Technology.

http://www.ub.tuwien.ac.at/en



FAKULTÄT FÜR !NFORMATIK Faculty of Informatics

Complementary Methods for the Enrichment of Linked Data

DISSERTATION

submitted in partial fulfillment of the requirements for the degree of

Doktor der Technischen Wissenschaften

by

Dipl.-Ing. Stefan Bischof Registration Number 0327033

to the Faculty of Informatics at the TU Wien

Advisor: Univ.-Prof. Dr. Axel Polleres

The dissertation has been reviewed by:

Prof. Dr. Oscar Corcho

Dr. Claudia d'Amato

Vienna, 12th October, 2017

Stefan Bischof

© Stefan Bischof 2017

The research presented herein was partially funded by the Vienna Science and Technology Fund (wwTF) under grant number ICT12-015.

To my wife Herlinde and our son Moritz

Declaration

I declare that this thesis has been composed by me and is based on my own work, unless stated otherwise. No other person's work has been used without due acknowledgement in this thesis. All references and verbatim extracts have been quoted and all sources of information, including graphs and datasets, have been specifically acknowledged.

Vienna, 12 October 2017

Stefan Bischof

Zusammenfassung

Offen verfügbare Daten, die basierend auf Semantic Web Standards und Linked Data Prizipien in einem einheitlichen Format am Web veröffentlicht werden, stellen eine hochwertige Quelle zur Datenanalyse dar. Obwohl die Integration von Daten der Hauptanwendungsfall von Semantic Web Technologien ist, ist eine solche Intgration in der Praxis nicht trivial, da trotz einheitlicher Syntax aber wegen unvollständiger Daten eine semantische Heterogenität überwiegt. Als praktischen Anwendungsfall vergleichen wir in dieser Dissertation statistische Städtedaten, die bereits öffentlich im Word Wide Web in (semi-) strukturierter Form als Linked Data zur Verfügung stehen. Dazu evaluieren wir verschiedene Datenquellen und integrieren passende Datensätze durch den Einsatz von Semantic Web Technologien. Zuerst befassen wir uns in dieser Arbeit speziell mit der Herausforderung vollständige und vergleichbare Daten aus offenen RDF Datenbanken zu extrahieren, besonders im Hinblick auf OWL Entailment Regimes. Wir kommen zu dem Schluss, dass OWL Inferenz alleine keine ausreichende Lösung für unvollständige Daten und Heterogenitätsprobleme ist. Als Ansatz um diese Probleme insbesondere für numerische Daten zu lösen, entwickeln wir Methoden um fehlende Daten abzuschätzen, basierend auf bekannten statistischen Methoden sowie auf der deklarativen Repräsentation von numerischen Beziehungen in Form von algebraischen Gleichungen. Schlussendlich diskutieren wir Kombinationen dieser Methoden und entwickeln einen kombinierten Ansatz zur Verknüpfung regelbasierter und statisischer Methoden zur Anreicherung von Linked Data.

Abstract

Data published in accordance with Semantic Web standards and Linked Data principles constitutes a prime source of openly available data ready for analysis in a unified format. Even though the main use case of Semantic Web technologies is data integration, in practice getting comparable data is not trivial, that is heterogeneity problems and challenges arising through incomplete data prevail despite syntactic homogeneity. The use case we focus on in this thesis revolves around comparing statistical data about cities found on the Web in (semi-) structured form integrated as Linked Data. Firstly, we evaluate different data sources and eventually integrate suitable datasets using Semantic Web technologies and RDF. Hereby, the work specifically addresses the challenges of getting complete data from SPARQL endpoints, for instance with respect to OWL entailment regimes. However, we come to the conclusion that OWL inference alone is insufficient for resolving incompleteness and heterogeneity problems, especially for numerical data. To this end, we develop methods to infer missing numerical data exploiting statistical methods and equational knowledge. Lastly, we discuss combinations of these methods, i.e. we develop a combined approach for integrating rule-based and statistical methods for Linked data enrichment.

Acknowledgements

I would like to thank *everyone* who helped me, in one way or another, during my study and the writing of this thesis. First of all, I want to thank my co-authors Axel Polleres, Andreas Harth, Benedikt Kämpgen, Markus Krötzsch, Sebastian Rudolph and Patrik Schneider for their cooperation and many insightful discussions. I am grateful to my examiners Oscar Corcho and Claudia d'Amato for their feedback on an earlier version of this thesis. Many thanks to Kenneth Kirrane for proof-reading the whole thesis, Josiane Xavier Parreira for feedback and Sabrina Kirrane for encouragement in the last weeks. Moreover, I want to thank my boss at Siemens, Herwig Schreiner, for giving me the freedom to pursuit this thesis. Thanks to my family and friends for understanding and encouraging me. Above all, I am most indebted to my supervisor Axel Polleres, for his guidance and advice as well as (sometines intense) discussions on numerous technical details. Finally, and in particular, thanks to my wife Herlinde for *everything*.

Contents

Part I FOUNDATION - 1

- 1 INTRODUCTION -3
- 1.1 Challenges and Research Questions 4
- 1.2 Contributions and Structure 7
- 2 PRELIMINARIES 11
- 2.1 Resource Description Framework 11
- 2.2 SPARQL 13
- 2.3 Semantic Web Reasoning 17
- 2.4 Statistical Linked Data and Provenance 22

Part II THEORY - 27

- 3 SCHEMA-AGNOSTIC QUERY REWRITING -29
- 3.1 Introduction 29
- 3.2 OWL QL: RDF Syntax and Rule-Based Semantics 31
- 3.3 OWL QL Reasoning with SPARQL Path Expressions 34
- 3.4 OWL QL Query Rewriting with SPARQL 1.1 43
- 3.5 Optimisation and Implementation Remarks 45
- 3.6 Evaluation 55
- 4 RDF ATTRIBUTE EQUATIONS -65
- 4.1 Introduction 65
- 4.2 Extending Description Logics by Equations 67
- 4.3 SPARQL over RDF Attribute Equations 70
- 4.4 Implementation Approaches 75
- 4.5 A Practical Use Case and Experiments 76
- 4.6 Related Work 78

Part III APPLICATION - 81

- 5 OPEN CITY DATA PIPELINE -83
- 5.1 Introduction 83
- 5.2 Overview and System Architecture 86
- 5.3 Unified View over Statistical Linked Data 91
- 6 QB EQUATIONS -95
- 6.1 Introduction 95
- 6.2 QB Equations RDF Syntax 96
- 6.3 Rule-Based Semantics for QB Equations 99
- 6.4 Implementation of QB Equations in the OCDP 108
- 6.5 Related Work 109
- 7 EQUATIONS AND STATISTICAL METHODS COMBINED -113
- 7.1 Introduction 113
- 7.2 Imputation: Predicting Missing Values 114
- 7.3 Evaluation 121
- 7.4 Related Work 125

Part IV CONCLUSION - 133

- 8 SUMMARY AND DISCUSSION -135
- 8.1 Summary 135
- 8.2 Critical Assessment of Research Questions 137
- 8.3 Future Work 139

Part V APPENDICES - 147

- A RDF PREFIXES 149
- B data conversion, linking and integration -151
- B.1 Statistical Linked Data Wrappers 151
- B.2 Linking and Mapping Data 152
- B.3 Data Crawling and Integration 154
- C Complete example of QB equation steps -157

BIBLIOGRAPHY - 161

PART I

FOUNDATION

Introduction

1

The futurist Naisbitt wrote in 1982, "we are drowning in information, but we are starved for knowledge" [Naisbitt 1982]. With the advent of the World Wide Web (www) [Berners-Lee 1989], the amount of information in the form of hypertext documents is even more vast and is continuously increasing.

To gain knowledge from an ocean of data we can perform *data analysis*. Regardless of the concrete process a data analyst or data scientist follows—for example Han [2012], Pyle [1999] and Schutt and O'Neil [2013]—one of the first necessary and most time intensive tasks of data analysis is *data preparation*, which includes *data cleaning* and *data integration*. Experts agree that around 60% of the time in data analysis is spent on data preparation alone [Cabena et al. 1998; CloudFlower 2016; Pyle 1999]. Therefore efficient data preparation approaches are crucial.

Search engines were built to automatically structure and find knowledge in this information ocean. But the search engines could not *understand* the contents of the documents they were linking to. This *web of documents* was then augmented and extended with the *web of data*; a process ignited by the seminal idea of the Semantic Web [Berners-Lee, J. Hendler and Lassila 2001]. The Semantic Web aims to provide a framework of languages and methods to build "a new form of Web content that is *meaningful* (emphasis added) to computers" [Berners-Lee, J. Hendler and Lassila 2001] and thus eventually allowing machines to automatically produce and ingest information [Heath and Bizer 2011; Berners-Lee 2006; Bernstein, J. Hendler and N. Noy 2016]. Nevertheless, the web of data only contributes to the explosion of the amount of information and does not save us from drowning.

Semantic Web technologies aim to provide means to perform data integration and preparation more efficiently and—eventually—in an automated fashion [Janowicz et al. 2015]. In practice, however, even getting comparable data is not trivial; that is different kinds of heterogeneity problems and challenges arise [Bernstein, J. Hendler and N. Noy 2016]. Converting data to Semantic Web data formats alone does therefore not resolve heterogeneity, and actual *meaningful* interlinking can only be partially automated and still involves manual intervention. Even though data published following Semantic Web principles constitutes a prime source of openly available data in a unified format, this data still needs preprocessing before being ready for data analysis. In this work we focus on automatic taxonomic and numerical reasoning to get more complete query answers necessary for data analysis.

THE ORIGINAL MOTIVATION of this thesis is the collection, integration and analysis of openly available statistical data of cities worldwide, from a practical use case within Siemens, with the goal to score and compare cities based on this data. City data is an interesting domain because of the societal and economical implications of more and more people living and working in cities: since 2014 more than 50% of the population lives in cities-this ratio is still increasing [United Nations 2015b]. The United Nations (UN) defined in their 2030 Agenda for Sustainable Development [United Nations 2015a] one goal specific to cities "Sustainable Development Goal 11: Make cities and human settlements inclusive, safe, resilient and sustainable". When evaluating progress on this goal the UN also uses statistical city data. Different organisations also acknowledge the importance of cities and city data by publishing analyses of cities such as the Mercer's Quality of Living Ranking [Mercer 2017], the Economist Intelligence Unit's Global Liveability Ranking[The Economist Intelligence Unit 2017] or the Siemens Green City Index [The Economist Intelligence Unit 2012]. These reports are used by city administration for decision support or for example for companies to aid in computing premium allowances for expatriate employees.

However, these existing reports have several disadvantages: (i) the underlying data is often already outdated when the analysis is published, (ii) the underlying data is not publicly available, making an evaluation of validity or reliability of the results hardly possible; additionally the computation of the resulting scores and rankings is often not documented well enough to reproduce the results (iii) the underlying data and the resulting scores and rankings are often not reusable, either because of technical or legal reasons.

OUR HYPOTHESIS in this thesis is that in fact a lot of the underlying data used to generate these reports is already available in one or the other form publicly as *open data* and that—by exploiting Semantic Web technologies—we can collect and integrate this data to eventually enable the up-to-date generation of such reports in an automated fashion while retaining data lineage.

1.1 Challenges and Research Questions

Data integration is an important part of data preparation and it is the main use case for Semantic Web technologies. While integration is not always simple to achieve, Semantic Web technologies provide different tools to address it. Apart from data integration other steps of data preparation, e.g. data cleaning, data reduction, data transformation [Han 2012], are hard to achieve with existing Semantic Web technologies alone. In particular the manipulation of numbers can be cumbersome and is thus often left to dedicated data analysis tool which are not integrated into Linked Data based workflows. Therefore information about the data origin and processing is lost in the process. Reasoning about and processing of taxonomic knowledge is well addressed within Semantic Web research, reasoning about and processing numerical data is—with few exceptions—still a widely neglected area.

When building a Semantic Web analysis platform several problems arise, which cannot be solved efficiently by engineering but pose interesting research problems. In this work we are concerned with three of such challenges.

Reasoning Capabilities of SPARQL Endpoints Unknown

Linked Data and other RDF data is often accessible via open SPARQL endpoints where data is modelled after OWL ontologies. However, these endpoints often do not or only partially support ontological reasoning (for example on certain fragments of OWL such as RDFS only) or it is unclear whether or to which extent reasoning already was applied to the data. Thus, we need means to assess if reasoning is performed. If not, we still want to be able to do reasoning with the tools SPARQL provides.

In the case of OWL QL ontologies which we are considering in this thesis, a user can still get complete query answers by using *ontology mediated query answering* (OMQA) techniques [Bienvenu and Ortiz 2015]. In OMQA the query is first rewritten into a new query, by taking the ontology into account. For our main use case however, OMQA has two disadvantages: (i) RDF triple stores do not distinguish between terminological and assertional knowledge like Description Logic and OMQA, thus the ontology must be extracted beforehand for the rewriting step (ii) the rewritten query is exponentially large in the size of the input query in the worst case [Calvanese, De Giacomo et al. 2007].

Research question 1. Can we produce and effectively use rewritings of SPARQL queries which are independent of the ontology and avoid the exponential blowup of standard query rewriting techniques?

We aim to push the boundaries of enabling OWL QL on off-the-shelf SPARQL endpoints by query rewriting and without knowing the ontology upfront.

Equational Background Knowledge Unusable for Reasoning

Even if ontological reasoning is complete, certain "ontological" background knowledge, such as equations on numeric values, are out of scope of ontological reasoners.

Data analysts working with statistical data (or other numeric data in general) are interested in computing indicators to represent some characteristic. For example the *number of unemployed persons* is an important indicator when evaluating the economic situation of a region. But only when normalising this indicator to the population number (usually including only persons of employable age) of the region and thus computing the *unemployment rate* regions then become comparable.

These computations are usually defined as functions or equations. *Equations* describe relations between numerical attributes. While OWL provides terminological reasoning services, knowledge about attributes (concrete values like numbers or strings) is only weakly supported. Equations are not expressible by OWL 2 alone. Extending OWL to express equations and a corresponding semantics for computation would give us the means to compute new values like the GDP per capita or check numerical attributes for consistency.

Research question 2. Can we express and effectively use equational knowledge about numerical values of instances along with RDFS and OWL to derive new values?

By using equational knowledge we can transparently compute new numerical values for missing value prediction, for computing derived indicators or simply for converting values between units.

Ontological Reasoning Insufficient for Predicting Missing Values

Real-world datasets are often missing a part of the data which would be needed for data analysis, e.g. to be able to compute indicators and scores for all desired cities. Ontological reasoning alone is insufficient to impute missing values for analysis because it lacks significant reasoning capabilities for numeric values. Automatic computation of new values based on equational knowledge alone will often still not give enough data to conduct an analysis. Standard statistical missing data methods are also challenged by the high rate of missing values in such datasets. A combination of equationally derived values and statistical methods could improve the overall missing value estimation quality.

Research question 3. Can we combine statistical inference with OWL and equational knowledge to improve missing value imputation?

With this combined workflow we expect higher quality missing value predictions as well as a higher number of missing value predictions. Ideally we could combine all three methods, namely statistical missing-value imputation, equational knowledge and ontological reasoning. As we discuss in Chapter 8, an effective approach to this ideal combination is non-trivial to find.

OVERALL WE ARE interested to find out to what extent we can use standard off-the-shelf tools such as SPARQL engines to answer the research questions.

1.2 Contributions and Structure

We now introduce four contributions of this thesis to address the three research questions.

1.2.1 Contribution to research question 1

Schema-agnostic rewriting We introduce schema-agnostic query rewriting in SPARQL 1.1 as a way to transparently, i.e. independently of the ontology, rewrite a SPARQL query into a new SPARQL query. The rewriting exploits SPARQL 1.1 property path expressions to navigate the ontology at runtime and thus turns an off-the-shelf SPARQL 1.1 engine into an OWL QL reasoner.

We introduced schema-agnostic query rewriting in SPARQL 1.1 at the International Semantic Web Conference 2014 [Bischof, Krötzsch et al. 2014a], and also published a paper at the Description Logic Workshop 2015 [Bischof, Krötzsch et al. 2015]. A journal submission containing an extensive evaluation of schema-agnostic querying is currently in preparation [Bischof, Krötzsch et al. 2017]. Schema-agnostic rewriting is presented in Chapter 3.

1.2.2 Contributions to research question 2

In general RDF allows two ways to model numerical data: (i) as a numeric literal (attribute) in a binary relation in RDF—the equivalent in OWL being *DataProperty* (ii) as part of an n-ary (or reified) statement, as for example modelled by the measure dimension in the Data Cube vocabulary [Cyganiak, Reynolds and Tennison 2014]. The following two contributions describe expressing and reasoning with equational knowledge for these two cases.

RDF Attribute Equations We define an extension of the Description Logic equivalent to RDFs to express relations between numerical attributes (equations) for RDF attributes. We give an algorithm for SPARQL query rewriting to transparently compute new values for backward chaining reasoning.

We presented RDF attribute equations at the Extended Semantic Web Conference 2013 [Bischof and Polleres 2013]. These results are presented in Chapter 4.

QB Equations We introduce QB equations, an approach to compute new numerical (statistical) data by exploiting equational knowledge for multidimensional databases. QB equations use the Data Cube vocabulary and provide detailed provenance information on how values are computed and can propagate error estimates of input values. Error estimates quantify how much reported indicator values potentially deviate from the real value. Such error estimates can stem from observed values or from statistical missing value

imputation algorithms. We give an RDF syntax and semantics and present experimental results of a prototype implementation.

1 http://citydata.wu.ac.at/ocdp

A journal submission containing the QB equations as well as an improved version of the Open City Data Pipeline¹ is accepted for publication in the Special Issue on *Semantic Statistics* of the Journal of Web Semantics [Bischof, Harth et al. 2017]. QB equations are described in Chapter 6.

1.2.3 Contribution to research question 3

Combined missing value prediction We introduce a process to fill in missing values which usually occur in Linked Data, especially when integrating data in one domain from different sources. The described process combines statistical missing value imputation applied on data given in the Data Cube vocabulary with QB equations.

We introduced the Open City Data Pipeline and specifically the first part of the combined missing value prediction—two machine learning methods for missing value prediction—at the Know@LOD workshop [Bischof, Martin et al. 2015b] co-located with ESWC 2015. We presented an extension of the above paper on the Open City Data Pipeline at the International Semantic Web Conference 2015 [Bischof, Martin et al. 2015a], where we additionally evaluated the cross-dataset-predictions and automatic learning of indicator mappings between datasets. A journal submission containing the QB equations as well as an improved version of the Open City Data Pipeline is accepted for publication in the Special Issue on *Semantic Statistics* of the Journal of Web Semantics [Bischof, Harth et al. 2017] and served as a basis for Chapter 7.

APART FROM the research questions, our use case motivates the four previous technical contributions with a concrete application scenario. The Open City Data Pipeline is a platform to collect, integrate, enrich and republish Linked Data about cities based on off-the-shelf Semantic Web technologies.²

2 http://citydata.wu.ac.at/ocdp/

1.2.4 Outline

The current Part I *Foundations* contains this introduction chapter as well as the *Preliminaries*.

Chapter 2 explains shared definitions used in the following chapters. This mainly includes Semantic Web foundations, including description logics and Semantic Web technologies.

Part II *Theory* contains the two theoretical foundational building blocks necessary later, addressing research questions 1 and 2.

Chapter 3 introduces schema-agnostic rewriting. We give formal definitions and an extensive evaluation.

Chapter 4 introduces RDF attribute equations. We extend a common description logic to support reasoning with equational knowledge and give an experimental evaluation.

Part III *Application* describes our main use case and its implementation in the Open City Data Pipeline. Furthermore this part describes two research contributions addressing research questions 2 and 3.

- *Chapter 5* describes our main use case in more detail. The chapter explains the architecture of the Open City Data Pipeline and how the data needed for the following chapter is modelled.
- *Chapter 6* describes QB equations, which express equational knowledge for the Data Cube vocabulary. We introduce an RDF syntax, a semantics based on the evaluation of SPARQL queries until a fixpoint is reached.
- *Chapter 7* we present a combined workflow integrating statistical machine learning methods with reasoning based on equational knowledge. In a practical evaluation we show how the combined method can help in building a system to process data for analysis and further publication in the domain of city data.
- In Part IV Conclusion we summarise and conclude this work.
- *Chapter 8* summarises this work and evaluate the presented contributions with respect to the research questions. We finish with a list of open questions interesting for future work.

In Part V *Appendices* we give technical details of RDF serialization, specific parts of the Open City Data Pipeline implementation as well as a complete example of the QB equation implementation.

Preliminaries

This chapter provides the preliminaries needed for the following chapters. In particular this chapter includes an introduction to basic Semantic Web technology specifications such as w₃c standards as well as their formal underpinnings. We keep this chapter to the necessary minimum and refer the interested reader to more extensive resources at the end of each section.

Section 2.1 introduces the underlying Semantic Web data model RDF and Section 2.2 describes the corresponding query language SPARQL. OWL 2, a knowledge representation language along with reasoning formalisms applicable to OWL are described in Section 2.3. Section 2.4 describes relevant Linked Data Vocabularies.

2.1 Resource Description Framework

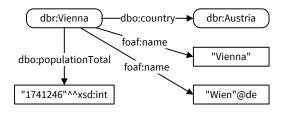
The Resource Description Framework (RDF) specifies the foundational data model of Semantic Web Technologies. RDF is primarily the definition of a graph-based data model, to describe any kind of things (called *resources*). In RDF we distinguish three types of such resources: IRIS, blank nodes and literals. *Internationalized Resource Identifiers* (IRI) are used to *name* resources. A resource could be any physical thing such as a rock or a person, or a immaterial thing such as a city or the *concept* of a smart city itself. If, for some reason, it is unnecessary to give a resource an explicit name, a *blank node* can be used; formally a blank node can be seen as an anonymous existential variable. Lastly, a *literal* is a data value which can be of one of several types: a simple string, e.g. "Vienna", a string with a language tag, e.g. "Wien"@de, where de represents the German language or literals with a datatype, e.g. "1741246"^^xsd:int, where xsd:int represents integer numbers [Klyne, Carroll and McBride 2014].

The basic building block of the RDF data model is an RDF triple (or simply *triple*) consisting of a *subject*, *predicate* and *object*, where subject and object are often depicted as nodes and the predicate as the label of the directed link connecting the subject to the object. Each of the three can be an IRI. Subject and object can also be a blank node, i.e. an unlabelled entity. The object can also consist of a literal, i.e. an atomic value in a simple datatype such as string or integer.

Definition 2.1 (RDF term, RDF triple, RDF graph). Let I be the set of all IRIS, L be the set of all literals and B the set of all blank nodes where all these three sets are pairwise disjoint. The set L is comprised of all literals with language tags, literals with datatype IRIS and plain literals, i.e., literals with no language tag or datatype IRI. Then the set of *RDF terms* T is the union of these sets $I \cup L \cup B$. An *RDF triple* is a triple (s, p, o) $\in (I \cup B) \times I \times T$ where s is the *subject*, p the *predicate* and o the *object*. A set of RDF triples is an *RDF graph*.

The RDF specificatication originally specified only the RDF/XML syntax—an XML based syntax for the RDF data model [Gandon and Schreiber 2014]. In this work we will use the more compact and human-friendly Turtle syntax instead to denote RDF triples and RDF graphs [Beckett et al. 2014]. Turtle provides two syntaxes for an IRI, either as IRI enclosed in a pair of angle brackets http://dbpedia.org/resource/Vienna or as CURIE [Birbeck and Mc-Carron 2010], a syntax for expressing compact IRIS.¹ With a prefix declaration such as @prefix dbr: http://dbpedia.org/resource/ we can express the same IRI as before as dbr:Vienna. Blank nodes can be expressed either as CURIE with the underscore '_' as prefix or as a pair of square brackets. Literals are either given as plain literals, as literals with language tag or as literals with datatype annotation. RDF triples are then written by simply joining subject, predicate and object with white space and terminated by a dot. To reduce redundancy a semicolon can be used to implicitly repeat the subject and a comma to implicitly both subject and predicate.

Example 2.1. Rounded rectangles depict nodes—more specifically CURIES in the following example—and rectangles literals. The following figure shows an RDF graph with a subject node dbr:Vienna, which is connected to the object node dbr:Austria via the predicate dbo:country. The other three triples show three different forms of literals as objects. While "Vienna" is a plain literal, "Wien"@de is a literal with a language tag for German and "1741246"^^xsd:int is a typed literal, an integer number in this case. We use IRIS and triples from the DBPEDIA RDF graph [Bizer et al. 2009]², which includes foaf:name from the friend of a friend ontology (FOAF).³



This graph can then be represented in Turtle RDF syntax as follows:

@prefix dbr: <http://dbpedia.org/resource/>
@prefix dbo: <http://dbpedia.org/ontology/>
@prefix foaf: <http://xmlns.com/foaf/0.1/>
dbr:Vienna a dbo:City .

1 Apart from this initial description we will usually also use the term *IRI* instead of CURIE.

2 http://dbpedia.org/

3 http://xmlns.com/foaf/0.1/

dbr:Vienna dbo:country dbr: Austria . dbr:Vienna foaf : name "Vienna" . dbr:Vienna foaf : name "Wien"@de . dbr:Vienna dbo:populationTotal "1741246"^^xsd: integer .

Using semicolons and commas we can write the same RDF graph more compactly as follows:

```
@prefix dbr: <http://dbpedia.org/resource/>
@prefix dbo: <http://dbpedia.org/ontology/>
@prefix foaf: <http://xmlns.com/foaf/0.1/>
dbr:Vienna a dbo:City ;
dbo:country dbr:Austria ;
foaf:name "Vienna", "Wien"@de;
dbo:populationTotal "1741246"^^xsd:integer .
```

 \diamond

For a more compact representation we will use the prefix declarations from Appendix A instead of listing them in every example.

Summary The RDF as a data model can represent arbitrary resources which are named using IRIS, relations between resources also named using IRIS plus concrete atomic attribute values wich are represented by possibly typed literals. As syntax we use CURIES and Turtle. The texbook by Hitzler, Krötzsch and Rudolph [2009] contains a complete introduction to RDF.

2.2 SPARQL

Just as for relational data, we need tools to access and process data given in RDF. Analogous to sQL for relational data, the query language for RDF is SPARQL [Harris and Seaborne 2013].

2.2.1 SPARQL Syntax

The SPARQL language builds upon basic graph patterns (BGP) as the foundational patterns which map variables to RDF resources, as well as more complex graph patterns built on top of BGPs.

A triple pattern is a simple extension of the RDF triple by allowing a variable in each position and a path expression as predicate.

Definition 2.2 (triple pattern, BGP). Let V be the set of variables, disjoint from T. Then a *triple pattern* is a triple $(I \cup B \cup V) \times (I \cup V) \times (T \cup V)$. A *basic graph pattern* (BGP) is a set of triple patterns.

Path expressions work like regular expressions over edges in RDF graphs and can be used in a SPARQL BGP on predicate position to form path patterns.

Definition 2.3 (path expression, path pattern). The set of *path expressions* E is defined inductively as follows: (i) Every IRI is a path expression (ii) For e

and *f* being property expressions, the following expressions are property expressions as well: (*`e*) for inverse, $(e \mid f)$ for sequence, $(e \mid f)$ for alternative and (e^*) for Kleene star. As usual, parentheses can be omitted if there is no danger of confusion. A *path pattern* is a triple $(\mathbf{T} \cup \mathbf{V}) \times \mathbf{E} \times (\mathbf{V} \cup \mathbf{V})$.

Additionally to triple patterns we also allow path patterns in BGPs.

More complex graph patterns allow value creation, filtering, conjunction, disjunction and optional matching.

Definition 2.4 (graph pattern). The set of *graph patterns* is defined inductively as follows:

- а вср is a graph pattern
- if e is a SPARQL expression, p is a graph pattern and ?v is a variable not occurring in p, then BIND(e AS ?v) is a graph pattern
- if e is a SPARQL expression and p is a graph pattern, then {p} FILTER(e) is a graph pattern
- if p and q are graph patterns, then $\{p\}$ UNION $\{q\}$, $\{p\}$ OPTIONAL $\{q\}$ and $\{p\}$. $\{q\}$ are graph patterns

SPARQL expressions can be used for filtering but also for value creation.

Definition 2.5 (SPARQL expression). *SPARQL expressions* are defined induct-ively:

- a variable is a SPARQL expression
- an RDF term is a SPARQL expression
- if *p* is a graph pattern, then EXISTS{*p*} is a SPARQL expression
- if e_1, \ldots, e_n are SPARQL expressions and f is one of the SPARQL functions⁴ CONCAT, REPLACE, IRI, ABS, NOW, NOT or IF, then $f(e_1, \ldots, e_n)$ is a SPARQL expression
- if e_1 and e_2 are SPARQL expressions, then $e_1 = e_2$, $e_1 < e_2$, $e_1 <= e_2$, $e_1 != e_2$, $e_1 > e_2$ and $e_1 >= e_2$ as well as e_1 && e_2 and $e_1 \parallel e_2$ are SPARQL expressions

SPARQL allows three result forms for querying RDF or one form for updating RDF graphs.⁵

Definition 2.6 (SPARQL query, result form). A *SPARQL query* consists of a triple (R, P, G) where *P* is a graph pattern, *G* is an RDF graph and *R* is a *result form* defined as one of four cases as follows:

- SELECT $v_1 \dots v_n$ is a result form for the variables v_1, \dots, v_n
- CONSTRUCT $\{T\}$ is a result form
- ASK is a result form
- INSERT $\{T\}$ is a result form

where *T* is a set of triple patterns called *graph template*.

A template, as needed for CONSTRUCT and INSERT consists of a set of triple

4 see Harris and Seaborne [2013] for a complete list of spargL functions, we restrict ourselves here to the ones used in the course of this thesis

5 the other result forms are not relevant for this thesis [Harris and Seaborne 2013] patterns.

SPARQL defines a *dataset* which consists of one so called *default graph* and a set of named graphs, where a *named graph* is a pair (i, G) where $i \in I$ and G is an RDF graph. Since this practical feature is not necessary in this thesis, we operate on a single graph G instead.

Example 2.2. The following query is a SELECT query containing one path pattern

```
SELECT ?thing ?name
WHERE { ?thing dbo:country?/foaf:name ?name }
```

The next example is a CONSTRUCT query and contains two triple patterns in a BGP, a BIND pattern for value creation and a triple pattern in the CONSTRUCT template:

```
CONSTRUCT { ?thing dbo:populationDensity ?populationDensity }
WHERE { ?thing dbo:populationTotal ?population ;
dbo:areaTotal ?area .
BIND(?population/?area AS ?populationDensity) }
```

 \diamond

2.2.2 SPARQL Semantics

We define the semantics of SPARQL queries extending J. Pérez, Arenas and Gutierrez [2009] with operators needed in the course of this work. Th necessary extensions include the following SPARQL 1.1 features: path expressions, value assignment, more SPARQL expressions as well as update queries. We thus define a set semantics in contrast of the bag semantics of the SPARQL specification. First we define the semantics of path expressions.

Definition 2.7. We define the *evaluation* of path expressions with respect to an RDF graph *G* as a binary relation over $\mathbf{I} \cup \mathbf{B}$ in an inductive way: for $p \in \mathbf{I}$, $\llbracket p \rrbracket_G = \{(u_1, u_2) \mid u_1 \ p \ u_2 \in G\}$, inverse $\llbracket^{\hat{p}} \rrbracket_G = \{(u_2, u_1) \mid (u_1, u_2) \in \llbracket p \rrbracket_G\}$, sequence $\llbracket p \ q \rrbracket_G = \{(u_1, u_3) \mid (u_1, u_2) \in \llbracket p \rrbracket_G, (u_2, u_3) \in \llbracket q \rrbracket_G\}$, alternative $\llbracket p \ q \rrbracket_G = \llbracket p \rrbracket_G \cup \llbracket q \rrbracket_G$, Kleene star $\llbracket p^* \rrbracket_G = \bigcup_{n \ge 0} \llbracket p^n \rrbracket_G$ where $\llbracket p^0 \rrbracket_G = \{(u, u) \mid u \in \mathbf{I} \cup \mathbf{B}$ occurs in *G*} and $\llbracket p^{n+1} \rrbracket_G = \llbracket p^n \rrbracket_G \circ \llbracket p \rrbracket_G$.

Next we define the semantics of triple patterns and BGPs. Blank nodes in BGPs work like scoped variables and are instantiated via a mapping σ . The mapping μ then is a partial mapping from variables to RDF terms.

Definition 2.8. The *evaluation* $[\![b]\!]_G$ of a basic graph pattern *b* with respect to an RDF graph *G* is the set of all partial mappings μ from variables in *b* to IRIS, blank nodes or literals of *G*, such that there exists some mapping σ from all blank nodes in *b* to terms of *G* for which $\mu(\sigma(b)) \in G$. Two mappings μ_1 and μ_2 are *compatible* if for all ? $v \in \text{dom}(\mu_1) \cap \text{dom}(\mu_2)$ the mappings are the same μ_1 (?v) = μ_2 (?v). The domain dom(μ) of a mapping μ is the set of variables where μ is defined. We can now define the evaluation of the other graph patterns over a graph.

Definition 2.9. The *evaluation* $[\![p]\!]_G$ of a graph pattern p over an RDF graph G is defined recursively as follows:

- $[[p_1 . p_2]]_G = \{ \mu_1 \cup \mu_2 \mid \mu_1 \in [[p_1]]_G, \mu_2 \in [[p_2]]_G \text{ and } \mu_1, \mu_2 \text{ are compatible} \}$
- $[[p_1 \text{ UNION } p_2]]_G = \{ \mu \mid \mu \in [[p_1]]_G \text{ or } \mu \in [[p_2]]_G \}$
- $[[p_1 \text{ OPTIONAL } p_2]]_G = [[p_1 \cdot p_2]]_G \cup \{ \mu \in [[p_1]]_G \text{ for all } \mu' \in [[p_2]]_G, \mu, \mu' \text{ are not compatible } \}$
- $\llbracket p \text{ FILTER } e \rrbracket_G = \{ \mu \mid \mu \in \llbracket p \rrbracket_G \text{ and } \llbracket \mu(e) \rrbracket_G = true \}$
- $\llbracket p \operatorname{BIND}(e \operatorname{AS} ?v) \rrbracket_G = \{ \mu_1 \cup \mu_2 \mid \mu_1 \in \llbracket p \rrbracket_G, \mu_2 = \{ ?v \mapsto \llbracket \mu_1(e) \rrbracket_G \} \}$

We say a graph pattern gp has a *match* into a graph G if $[gp]_G \neq \emptyset$.

We slightly abuse the notation by extending the mapping μ to all SPARQL expressions, so the mapping $\mu(e)$ maps a SPARQL expression e to a SPARQL expression e' where all variables are replaced according to μ .⁶

Definition 2.10. The *evaluation* $[\![e]\!]_G$ of a SPARQL expression *e* over an RDF graph *G* is defined recursively as follows:

- for an RDF term $t \in \mathbf{T}$, $[t]_G = t$
- for a graph pattern p, $[[EXISTS{p}]]_G = true$ if $[[p]]_G \neq \emptyset$ and *false* otherwise
- $[[CONCAT(e_1, ..., e_n)]]_G$ returns the concatenation of $[[e_1]]_G, ..., [[e_n]]_G$ to one string
- [REPLACE(s, p, r)]_G returns the string [[s]_G where the string [[r]]_G replaces matches of the regular pattern p in s
- $[\operatorname{IRI}(e)]_G$ converts the string $[e]_G$ into an IRI
- $[ABS(e)]_G$ returns the absolute value of a number $[e]_G$
- $[NOW()]_G$ returns the current date and time
- $[[NOT(e)]]_G$ returns *true* if $[[e]]_G = false$ and *false* otherwise
- $\llbracket \mathsf{IF}(c, i, e) \rrbracket_G$ returns $\llbracket i \rrbracket_G$ if $\llbracket c \rrbracket_G = true$ and $\llbracket e \rrbracket_G$ otherwise
- for the comparison operators ∘ ∈ {=, <, <=, >, >=, !=}, the evaluation [[e₁ ∘ e₂]]_G returns the boolean value of the corresponding comparisons for numbers [[e₁]]_G and [[e₂]]_G
- $\llbracket e_1 \&\& e_2 \rrbracket_G$ returns *true* if $\llbracket e_1 \rrbracket_G = true$ and $\llbracket e_2 \rrbracket_G = true$ and *false* otherwise
- $\llbracket e_1 \parallel e_2 \rrbracket_G$ returns *true* if $\llbracket e_1 \rrbracket_G = true$ or $\llbracket e_2 \rrbracket_G = true$ and *false* otherwise

Whenever the type of one of the subexpressions does not match the expected type in the definition, the result is undefined.

Finally we define the answers of a complete SPARQL query.

Definition 2.11. The set of *answers* of a SELECT query (SELECT $?v_1 \dots ?v_n, P, G$) is the set obtained by restricting every partial function $\mu \in \llbracket P \rrbracket_G$ to the variables $?v_1, \dots ?v_n$.

The set of *answers* of a CONSTRUCT query (CONSTRUCT T, P, G) returns the RDF graph obtained by applying each mapping μ in the evaluation $[\![P]\!]_G$

6 Similarly to J. Pérez, Arenas and Gutierrez [2009] we use a two-valued logic here for SPARQL expressions. However the semantics would be easily generalisable to add the third value *error* to the official three-valued logic, see Polleres and Wallner [2013]. to each triple in the template *T*. For each blank node in *T* a fresh blank node is created for each mapping $\mu \in [\![P]\!]_G$.

The *answer* of an ASK query (ASK, P, G) returns *true* if $\llbracket P \rrbracket_G \neq \emptyset$ and *false* otherwise.

The INSERT query (INSERT T, P, G) replaces the RDF graph G with a new RDF graph G' which is the union of G and the RDF graph obtained by applying each mapping μ in the evaluation $\llbracket P \rrbracket_G$ to each triple in the template T. As for the CONSTRUCT query, for each blank node in T a fresh blank node is created for each mapping $\mu \in \llbracket P \rrbracket_G$.

Example 2.3. The first query of Example 2.2 returns the set of mappings (often visualised as a table) with ?thing being mapped to an IRI or blank node representing a city, and ?name being mapped to the name of the city or the country the city belongs to. For the example graph from Example 2.1 we will get the following two results:

?thing	?name
dbr:Vienna	"Vienna"
dbr:Vienna	"Wien"@de

If the country dbr:Austria had a triple with the predicate foaf:name as well, we would get an additional result.

For the second query of Example 2.2 and the RDF graph from Example 2.1 plus the triple dbr:Vienna dbo:areaTotal 414650000.0"^^xsd:double, we would get the following RDF graph as a result, giving us the population density of Vienna per m²: dbr:Vienna dbo:populationDensity 0.004199. \diamond

Summary SPARQL 1.1 is an expressive query language to process RDF data. The textbook by DuCharme [2013] gives a good introduction to SPARQL 1.1. While Hitzler, Krötzsch and Rudolph [2009] cover only the older SPARQL specification [Prud'hommeaux and Seaborne 2008]. Kaminski, Kostylev and Grau [2017] give a formal analysis of new SPARQL 1.1 features, in particular assignment, subqueries and aggregation.

2.3 Semantic Web Reasoning

To increase the expressiveness of RDF the w₃c also published the RDF Schema (RDFS) [Brickley and Guha 2014] and the Web Ontology Language (OWL) specifications [OWL Working Group 2009]. In this thesis we refer only to the most recent versions of these specifications, namely, RDFS 1.1 and OWL 2.

RDF allows resources to be assigned to classes by using rdf:type as predicate in triples where the instance is at the subject position and the class is at the object position. RDFs extends RDF by essentially four constructs, which are rdfs:subClassOf, rdfs:subPropertyOf, rdfs:domain and rdfs:range (cf. Gutierrez, 18

Hurtado and Mendelzon [2004]). Where rdfs:subClassOf and rdfs:subProperty-Of allow to create hierarchies of classes and properties, respectively, where the subclass (subproperty) is the subject and the superclass (superproperty) is the object. The properties rdfs:domain and rdfs:range relate a property p, in the subject position of the axiom triple, to a class in the object position of the axiom triple. Given a triple x p y, rdfs:domain specifies the class for x and rdfs:range specifies the class for y.

OWL is a language to represent ontologies, which in turn are descriptions about things (called *resources*), groups of resources and their relations [Hitzler, Krötzsch et al. 2009]. The semantics of OWL can either be given by the RDF semantics or by a mapping to description logic. The definition we choose is the latter one, called the *direct semantics*. The family of OWL specifications defines three different fragments of the OWL language called *OWL profiles* [Motik, Cuenca Grau et al. 2009] which allow tractable reasoning for different reasoning tasks. In this thesis we restrict ourselves to the so-called *OWL QL profile* and its corresponding description logic DL-Lite, which are tailored to allow tractable query answering.

This section first introduce *description logics*, which is the foundational logic for the RDFS and OWL semantics definition. Afterwards we introduce the different RDFS and OWL constructs with their corresponding RDF syntax and then define the semantics of RDFS and OWL by translation to a suitable description logic. Eventually we introduce *ontological query answering* as the idea of answering queries in the presence of ontologies.

2.3.1 Description Logics and OWL

Description Logic (DL) (cf. Baader, Calvanese et al. [2007]) is a logic-based knowledge representation formalism. Besides the Semantic Web, DLs are used in several areas, for example for conceptual modelling (e.g. Calvanese, Lenzerini and Nardi [1998]), information integration (e.g. N. F. Noy [2004]) or ontological query answering (see below).⁷

As explained above we will only use one specific description logic in this thesis: DL-Lite, originally denoted as DL-Lite_{\mathcal{R}} by [Calvanese, De Giacomo et al. 2007]. We will now formally define DL-Lite and extend the notions of *class* and *property* informally introduced by RDFs above.

Definition 2.12. Let A be an atomic class name and P be an atomic property name. B is a basic class and Q is a basic property. C is a complex class expression and R is a complex property expression. Then classes and properties are defined as follows:

$B \coloneqq A \mid \exists Q$	$Q \coloneqq P \mid P^-$
$C := B \mid \neg B$	$R \coloneqq Q \mid \neg Q$

Definition 2.13. A DL-Lite knowledge base (KB) $\mathcal{K} = (\mathcal{T}, \mathcal{A})$ consists of a TBox \mathcal{T} and an ABox \mathcal{A} . The TBox is a set of class inclusion axioms $B \sqsubseteq C$

7 See Baader, Calvanese et al.[2007] and Baader, Horrocks et al.[2017] for more examples.

OWL RDF syntax	DL syntax
 owl:Thing	Т
owl:Nothing	\perp
owl:someValuesFrom owl:Thing; owl:onProperty P	$\exists P$
owl:someValuesFrom C ; owl:onProperty Q	$\exists Q.C$
B rdfs:subClassOf C	$B_1 \sqsubseteq C_2$
B_1 owl:equivalentClass B_2	$B_1 \equiv B_2$
B_1 owl:disjointWith B_2	$B_1 \sqsubseteq \neg B_2$
P_1 owl:inverseOf P_2	$P_1 \equiv P_2^-$
Q rdfs:subPropertyOf R	$Q \sqsubseteq R$
Q_1 owl:equivalentProperty Q_2	$Q_1 \equiv Q_2$
P rdfs:domain A	$\exists P \sqsubseteq A$
P rdfs:range A	$\exists P^- \sqsubseteq A$
P_1 owl:propertyDisjointWith P_2	$P_1 \sqsubseteq \neg P_2$
Q_1 owl:complementOf Q_2	$Q_1 \equiv \neg Q_2$
x rdf:type A	A(x)
x R y	R(x, y)
x owl:differentFrom y	$x \neq y$

Table 2.1: Corresponding expressions of OWL and DL syntax

and property inclusion axioms $Q \sqsubseteq R$. The ABox is a set of class membership axioms A(a) and property membership axioms P(a, b).

Definition 2.14. An *interpretation* $I = (\Delta^{I}, \cdot^{I})$ consists of a non-empty set Δ^{I} called the *object domain* and an *interpretation function* \cdot^{I} which is defined as follows:

$A^I \subseteq \Delta^I$	Class assertion
$P^I \subseteq \Delta^I \times \Delta^I$	Property assertion
$(\exists Q)^I = \left\{ x \mid \exists y.(x,y) \in R^I \right\}$	Existential restriction
$(P^{-})^{\mathcal{I}} = \left\{ (x, y) \mid (y, x) \in \mathbb{R}^{\mathcal{I}} \right\}$	Inverse
$(\neg B)^I = \Delta^I \setminus B^I$	Class negation
$(\neg Q)^I = \Delta^I \times \Delta^I \setminus Q^I$	Property negation

An interpretation I satisfies an axiom α , denoted $I \models \alpha$, in the following cases:

$$I \models C \sqsubseteq A \text{ if } C^{I} \subseteq A^{I}$$
$$I \models P_{1} \sqsubseteq P_{2} \text{ if } P_{1}^{I} \subseteq P_{2}^{I}$$
$$I \models C(a) \text{ if } a^{I} \in C^{I}$$
$$I \models P(a, b) \text{ if } (a^{I}, b^{I}) \in P^{I}$$

Finally, an interpretation I is called a *model* of a KB $\mathcal{K} = (\mathcal{T}, \mathcal{A})$, written $I \models \mathcal{K}$, if I satisfies all axioms in \mathcal{T} and \mathcal{A} .

Table 2.1 shows the conversion from OWL to the DL syntax where the equivalence axiom $X \equiv Y$ is used as a short hand for the two corresponding inclusion axioms $X \sqsubseteq Y$ and $Y \sqsubseteq X$. The mapping is based on the OWL to

RDF mapping [Patel-Schneider and Motik 2009]. Additionally the OWL RDF syntax provides the following shorter notations to express sets of (more than two) pairwise disjoint classes B_1, \ldots, B_n , properties P_1, \ldots, P_n and instances l_1, \ldots, l_n :

x rdf:type owl:AllDisjointClasses; owl:members (B₁,..., B_n) x rdf:type owl:AllDisjointProperties; owl:members (P₁,..., P_n) x rdf:type owl:AllDifferent; owl:members (I₁,..., I_n)

Qualified existential restriction $B' \sqsubseteq \exists R.B$ is only used as syntactic sugar since it can also be written with a fresh property name R_B according to our defined DL as follows:

$$B' \sqsubseteq \exists R_B, \exists R_B^- \sqsubseteq B, R_B \sqsubseteq R$$

In the literature class disjointness is sometimes alternatively written as $B \sqcap B' \sqsubseteq \bot$; the same applies to property disjointness.

2.3.2 Ontological Query Answering

After introducing Description Logics and their usage in Semantic Web standards, we now turn towards query answering. The topic of answering queries in the presence of ontologies has received substantial attention from the knowledge representation community, notably Calvanese, De Giacomo et al. [2007], Poggi et al. [2008] and Artale et al. [2009] and to some extent from the database community, e.g. Calì, Gottlob and Lukasiewicz [2012]. As Onto*logical Query Answering* we understand the idea of getting not only explicitly stored data (so called extensional data) from a database, but also data which can be indirectly entailed from the combination of extensional data with an ontology (so called intensional data). In the literature the terms Ontology-Mediated Query Answering (OMQA) and Ontology-Based Data Access (OBDA) refer to the same idea. Originally OBDA also included a step mapping the resulting query to relational database queries. In this thesis we follow recent developments and use the terms OBDA, OMQA and ontological query answering interchangeably. Specifically we follow DL-Lite, the most popular approach of OBDA, which is based on the intuitive idea of rewriting a query into a new query which contains all the necessary functionality to give complete results with respect to the ontology TBox when evaluated on the ABox. We refer again to Calvanese, De Giacomo et al. [2007] who introduced not only different variants of DL-Lite, but also an algorithm for ontological query answering which we present in this section and adapt later in Chapter 4. We now formally define conjunctive queries.

Definition 2.15 (conjunctive query, union of conjunctive queries). A *conjunctive query* (CQ) is an expression of the form

$$q(\vec{x}) \leftarrow \exists \vec{y}.\phi(\vec{x},\vec{y})$$

```
Algorithm 2.1: PerfectRef(q, \mathcal{T})
Input: Conjunctive query q, TBox \mathcal{T}
Output: Union of conjunctive queries P
P \coloneqq \{q\}
repeat
     P' := P
     for each q \in P' do
          foreach q in q do
                                                                                  // expansion
               for
each inclusion axiom I in \mathcal T do
                    if I is applicable to q then
                         P \coloneqq P \cup \{q[g/\operatorname{gr}(g,I)]\}
          for
each g_1, g_2 in q do
                                                                                  // reduction
               if g_1 and g_2 unify then
                    P := P \cup \{\tau(\operatorname{reduce}(q, q_1, q_2))\}
until P' = P
return P
```

where \vec{x} is a sequence of variables called *distinguished variables*, \vec{y} is a sequence of variables called *non-distinguished variables*, and ϕ is a conjunction of **class** and **property atoms** of the forms C(x) and P(x, y) respectively where x, y are constant symbols from I or variables (distinguished or non-distinguished). A set of queries with the same head $q(\vec{x})$ is a *union of conjunctive queries* (UCQ).

We now define answers of conjunctive queries when evaluated over DL-Lite knowledge bases.

Definition 2.16 (answer of a CQ over a KB). For a conjunctive query q and a KB \mathcal{K} the *answer to* q *over* \mathcal{K} is the set ans (q, \mathcal{K}) , consisting of tuples \vec{a} of constants from $I_{\mathcal{K}}$ such that $\vec{a}^{\mathcal{M}} \in q^{\mathcal{M}}$ for every model \mathcal{M} of the KB \mathcal{K} .

Since we are rewriting SPARQL queries to SPARQL queries and are not concerned with providing access to non-RDF databases we use OMQA instead of the more specific *ontology based data access* (OBDA).

The OWL QL profile allows conjunctive query answering in LOGSPACE data complexity [Motik, Cuenca Grau et al. 2009].

The function PerfectRef defined in Algorithm 2.1 (as defined by Calvanese, De Giacomo et al. [2007]) rewrites a CQ q to a UCQ P considering the inclusion axioms of the TBox \mathcal{T} . For a CQ q and two atoms a and b, the expression q[a/b] denotes the conjunctive query resulting from replacing a by b in the CQ q and the function reduce(q, a, b) returns the conjunctive query resulting from applying the most general unifier between a and b to q. For an atom g and an inclusion axiom I, the function gr(g, I), as defined in Algorithm 2.2, The function $\tau(q)$ replaces each unbound variable occurring in the CQ q by "_". Since we will not depend on the reduction step later in this thesis, we will not go into more detail and refer to Calvanese, De Giacomo et al. [2007] for formal definitions concerning reduction and unification in particular.

Algorithm 2.2: gr(g, I)

if g = A(x) then if $I = A_1 \sqsubseteq A$ then return $A_1(x)$ else if $I = \exists P \sqsubseteq A$ then return $P(x, _)$ else if $I = \exists P^- \sqsubseteq A$ then return $P(_, x)$ else if $g = P(x, _)$ then if $I = A \sqsubseteq \exists P$ then return A(x)else if $I = \exists P_1 \sqsubseteq \exists P$ then return $P_1(x, _)$ else if $I = \exists P_1^- \sqsubseteq \exists P$ then return $P_1(_, x)$ else if $g = P(_, x)$ then if $I = A \sqsubseteq \exists P^-$ then return A(x)else if $I = \exists P_1^- \sqsubseteq \exists P^-$ then return $P_1(x, _)$ else if $I = \exists P_1^- \sqsubseteq \exists P^-$ then return $P_1(x, _)$ else if g = P(x, y) then if $I = P_1 \sqsubseteq P$ or $I = P_1^- \sqsubseteq P^-$ then return $P_1(x, y)$ else if $I = P_1 \sqsubseteq P$ or $I = P_1^- \sqsubseteq P$ then return $P_1(x, y)$

Summary The standard Description Logic textbook Baader, Calvanese et al. [2007] and the more recently published Baader, Horrocks et al. [2017] give an extensive definition and explanation of Description Logics in general. Krötz-sch [2012] gives an introduction and discussion of the OWL profiles. Bienvenu and Ortiz [2015] explain OMQA and Calvanese, De Giacomo et al. [2009] and Kontchakov, Rodriguez-Muro and Zakharyaschev [2013] describe OBDA.

2.4 Statistical Linked Data and Provenance

The idea of Linked Data (LD) (or the web of data) aims to enable easier publication of RDF data on the web by relying on the Hypertext Transfer Protocol (HTTP) and thus exploiting the existing infrastructure of the www to publish and access data. To this end Berners-Lee introduced the following so called *Linked Data principles* [Berners-Lee 2006]:

- 1. Use URI s as names for things
- 2. Use HTTP URIS so that people can look up those names.
- 3. When someone looks up a URI, provide useful information, using the standards (e.g. RDF, SPARQL)
- 4. Include links to other URI s, so that they can discover more things

Following the w₃c specifications and the definitions above we use the term *resource* instead of *thing*. Furthermore, the *Universal Resource Identifiers* (URI) used in the Linked Data principles where subsumed by IRIs in the later versions of the Semantic Web standards: RDF 1.1 [Klyne, Carroll and McBride 2014], RDFS 1.1 [Brickley and Guha 2014], OWL 2 [OWL Working Group 2009] and SPARQL 1.1 [Harris and Seaborne 2013].

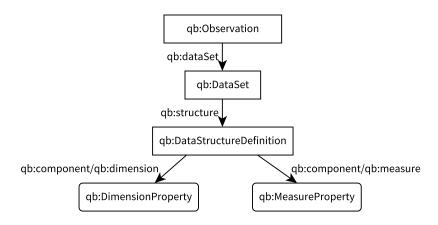


Figure 2.1: Illustration of most important classes of the RDF Data Cube Vocabulary with properties (or property chains) between instances of classes; adapted from "Outline of the vocabulary" in the QB specification.

The amount of data published following the Linked Data principles is continuously growing [Abele et al. 2017; Ermilov et al. 2016]. Linked Data sources use lightweight ontologies called *vocabularies* to structure their data. Repositories such as *Linked Open Vocabularies* document a wide range of vocabularies [Vandenbussche et al. 2017]. Most of the top used ontology constructs are covered by OWL QL [Glimm, Adian Hogan et al. 2012]. In this work we reuse two existing vocabularies: the RDF Data Cube Vocabulary for modelling multidimensional numerical data and the PROV vocabulary for modelling provenance information.

2.4.1 RDF Data Cube Vocabulary

The RDF Data Cube Vocabulary (QB) [Cyganiak, Reynolds and Tennison 2014] is a widely-used vocabulary to describe numeric data using a multidimensional data model [Gray et al. 1997]. QB, as a W3C recommendation has established itself as the standard for aggregating and (re-)publishing statistical observations on the web, with off-the-shelf tools to process and visualise QB data. Figure 2.1 provides an overview of QB with the most important classes and properties.

QB allows to describe datasets/cubes (instances of qb:DataSet) with observations (instances of qb:Observation). We use the terms (statistical) dataset, QB dataset and cube synonymously. Every dataset has a certain structure (instance of qb:DataStructureDefinition (DSD) that—using a chain of properties qb:component before qb:measure or qb:dimension—defines measures (instances of qb:MeasureProperty) and dimensions (qb:DimensionProperty). Attributes (qb:AttributeProperty) allow to add information to observations to qualify and interpret the observed values. A qb:DataSet provides all necessary information about a cube. The qb:DataSet IRI gives the name of the relation in the tabular representation defined by the cube. The qb:DataStructureDefinition—the metadata of the cube/dataset—defines the independent and dependent attributes of the relation as well as their possible attribute values. The qb:Observation instances describe the entities in the relation.

In the following, we illustrate how the metadata of a population dataset can be modelled using QB.

```
eurostat:id/urb_cpop1#ds a qb:DataSet;
rdfs:label "Population on 1 January by age groups and sex-cities and greater cities ";
qb:structure </dsd/urb_cpop1#dsd>.
eurostat:dsd/urb_cpop1#dsd a qb:DataStructureDefinition;
qb:component[qb:dimension dcterms:date];
qb:component[qb:dimension estatwrap:cities ];
```

qb:component[qb:dimension estatwrap:indic_ur];

qb:component [qb:measure sdmx-measure:obsValue] .

In the example, a data structure definition (DSD) defines the independent, categorical properties of the dataset, so-called *dimensions*: date, city and indicator. Also, the DSD defines one dependent numeric property, so-called *measure*. The data structure definition could also include all valid dimension values, such as all city IRIS for the dimension estatwrap:cities.

Now, we give an example of how one data point can be modelled using QB:

```
_:obs1 a qb:Observation ;
qb:dataSet eurostat:id/urb_cpop1#ds;
estatwrap: cities eurostat – cities :Vienna ;
estatwrap:indic_ur eurostat – indic_ur:Population ;
dcterms:date "2013" ;
sdmx-measure:obsValue "1741246".
```

The example describes an observation of 1741246 inhabitants of Vienna in 2013 in the population dataset of Eurostat. The observation is modelled with a blank node.

The QB specification defines the notion of *well-formed cubes* [Cyganiak, Reynolds and Tennison 2014] based on constraints that need to hold on a dataset. When generating and publishing QB datasets, we ensure that these constraints are fulfilled. For instance, when we later generate new observations via predictions and computations we also generate new datasets containing these values.

2.4.2 Provenance Annotations

To make observations more traceable and allow to judge the trustworthiness of data, we go beyond the lightweight approach of using Dublin Core properties such as dc:publisher to refer from a dataset to its publisher. We use the PROV ontology [Lebo, McGuinness and Sahoo 2013] to add provenance annotations, such as the agents and activities that were involved in generating observations from other observations (e.g., predicting, inferencing); Figure 2.2 gives a highlevel overview of the three main concepts. On a high level

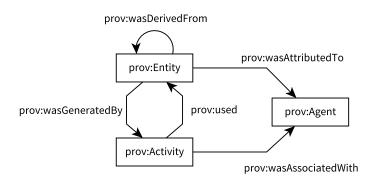


Figure 2.2: Overview of the PROV ontology

PROV distinguishes between entities, agents, and activities. A prov:Entity can be all kinds of things, digital or not, which are created or modified. *Activities* are the processes which create or modify entities. An prov:Agent is something or someone who is responsible for an activity (and indirectly also for an entity). A prov:Activity is something that happens and, in our case, generates new observations from other observations. PROV also defines *plans* which can be understood as any kind of predefined workflow which a prov:Activity might follow to create or modify an entity. Additionally PROV also allows to tag certain activities with *time*, for example a timestamp when an entity was created. The following RDF fragment shows a PROV example of two observations, where a QB observation ex:obs123 was derived from another observation ex:obs789 via an activity ex:activity456 on the 15th of January 2017 at 12:37. This derivation was executed according to the rule ex:rule937 with an agent ex:fred being responsible.

```
ex:obs123 prov:generatedAtTime "2017-01-15T12:37:00";
prov:wasDerivedFrom ex:obs789;
prov:wasGeneratedBy ex:activity456 .
ex: activity456 prov: qualifiedAssociation [
prov:wasAssociatedWith ex:fred ];
prov:hadPlan ex:rule937 .
```

Summary Wood et al. [2013] and Heath and Bizer [2011] both introduce Linked Data. Moreau and Groth [2013] describe provenance with the PROV ontology while the best resource for the RDF Data Cube Vocabulary is still the official specification [Cyganiak, Reynolds and Tennison 2014].

PART II

THEORY

3

Schema-Agnostic Query Rewriting

As a first contribution, we describe our idea of exploiting SPARQL 1.1 for query rewriting to implement OWL QL reasoning in a single query. Parts of this chapter have been published as Bischof, Krötzsch et al. [2014a] and Bischof, Krötzsch et al. [2014b].

Section 3.1 gives an introduction to schema-agnostic query rewriting and compares it to ontology-based rewriting techniques. Section 3.2 introduces OWL QL and relate its semantics to a *chase* procedure. Section 3.3 develops queries for implementing basic OWL QL reasoning in SPARQL 1.1. Section 3.4 extends these queries into a schema-agnostic query rewriting procedure for conjunctive queries. Section 3.5 defines three approaches to optimize query evaluation of schema-agnostic query rewriting. Section 3.6 evaluates schema-agnostic rewriting with a prototype implementation. The prototype is compared with ontology-based rewriting techniques and the different optimization approaches are evaluated as well.

3.1 Introduction

SPARQL 1.1 [Harris and Seaborne 2013], the revision of the original W3C SPAR-QL standard [Prud'hommeaux and Seaborne 2008], introduces significant extensions to the capabilities of the RDF query language [Harris and Seaborne 2013]. Even at the very core of the query language, we can find many notable new features, including *property paths*, *value creation* (BIND), negation and extended filtering capabilities. In addition, the SPARQL 1.1 entailment regimes specification defines query answering over OWL ontologies, taking full advantage of ontological information in the data [Glimm and Ogbuji 2013].

Query answering in the presence of ontologies is also known as *ontology-based data access* (OBDA) or *ontology-mediated query answering* (OMQA)¹ and has long been an important topic in applied and foundational research. Even before SPARQL provided support for this feature, several projects used ontologies to integrate disparate data sources, or to provide views over legacy databases, e.g. [Calvanese, De Giacomo et al. 2007; Pérez-Urbina, Motik and Horrocks 2010; Rodriguez-Muro, Kontchakov and Zakharyaschev 2013; Di Pinto et al. 2013; Kontchakov, Rodriguez-Muro and Zakharyaschev 2013]. The w3C OWL 2 Web Ontology Language includes the OWL QL language profile,

1 we will use OBDA and OMQA synonymously in this thesis

which was specifically designed for this application [Motik, Cuenca Grau et al. 2009]. With the arrival of SPARQL 1.1, every aspect of OBDA is thus supported by tailor-made w₃c technologies.

In practice, however, SPARQL and OWL QL are rarely integrated. Most of the works on OBDA address the problem of answering *conjunctive queries* (CQs), which correspond to SELECT-PROJECT-JOIN queries in SQL, and (to some degree) to BGPS in SPARQL. The most common approach for OBDA is *query rewriting*, where a given CQ is rewritten into a (set of) CQs that fully incorporate the schema information of the ontology. The answers to the rewritten queries are guaranteed to agree with the answers of the original queries, considering the ontology. This approach separates the ontology (used for query rewriting) from the rest of the data (used for query answering), and typically the latter is stored in a relational database. Consequently, the rewritten queries are often transformed into SQL for query answering. SPARQL and RDF do not necessarily play a role in this.

In this chapter, we take a fresh look at the problem of OBDA query rewriting with SPARQL 1.1 as our target query language. The additional expressive power of SPARQL 1.1 allows us to introduce a new paradigm of *schemaagnostic query rewriting*, where the ontological schema is not needed for rewriting queries. Rather, the ontology is stored *together with the data* in a single RDF database. This is how many ontologies are managed today, and it corresponds to the W3C view on OWL and RDF, which does not distinguish schema and data components. The fact, that today's OBDA approaches separate both parts testifies to their focus on relational databases. Our work widens the scope of OWL QL to RDF-based applications, which have hitherto focused on OWL RL as their ontology language of choice.

Another practical advantage of schema-agnostic query rewriting is that it supports frequent updates of both data and schema. The rewriting system does not need any information on the content of the database, while the SPAR-QL processor that executes the query does not need any support for OwL. This is particularly interesting if a database can only be accessed through a restricted SPARQL query interface that does not support reasoning. For example, we have used our approach to check the consistency of DBPEDIA under OWL semantics, using only the public Live DBPEDIA SPARQL endpoint² (it is inconsistent: particularly every library is inferred to belong to the mutually disjoint classes "Place" and "Agent").

Worst-case reasoning complexity remains the same in all cases, yet our approach is much more practical in the case of standard reasoning and BGP rewriting. For general CQs, the rewritten queries are usually too complex for today's RDF databases to handle. Nevertheless, we think that our "SPARQL 1.1 implementation" of OWL QL query answering is a valuable contribution, since it reduces the problem of supporting OWL QL in an RDF database to the task of optimizing a single (type of) query. Since OWL QL subsumes RDFS, one can also apply our insights to implement query answering under RDFS ontologies,

2 http://live.dbpedia.org/sparql

which again leads to much simpler queries.

3.2 OWL QL: RDF Syntax and Rule-Based Semantics

OWL QL is one of the OWL 2 profiles, which restricts the OWL DL ontology language to ensure that reasoning is tractable [Motik, Cuenca Grau et al. 2009]. To ensure compatibility with SPARQL, we work only with the RDF representation of OWL QL here [Patel-Schneider and Motik 2009]. Like OWL DL, OWL QL requires "standard use" of RDFs and OWL vocabulary, i.e., special vocabulary that is used to encode ontology axioms in RDF is strictly distinct from the ontology's vocabulary, and can only occur in specific triple patterns [de Bruijn and Heymans 2007; Muñoz, J. Pérez and Gutiérrez 2007]. Only a few special IRIS, such as owl:Thing, can also be used like ontology vocabulary in axioms.

In the RDF serialisation of OWL, classes, properties and individuals are represented by RDF elements, where complex class expressions and complex property expressions are represented by blank nodes. Whether an expression is represented by an IRI or a blank node does not have an impact on ontological entailment, so we ignore this distinction. OWL DL allows us to use a single IRI to represent an individual, a class and a property in the same ontology; owing to the restrictions of standard use, it is always clear which meaning applies in a particular case.³ Hence we will also work with one single set of IRIS.

Next, we define the constrains that an RDF graph has to satisfy to represent an OWL QL ontology. We transfer the syntactical constraints of DL-Lite in Section 2.3.1 to the RDF representation of OWL QL. To this end, consider a fixed RDF graph *G*. A *property expression in G* is an IRI or a blank node *x* that occurs in a pattern {*x* owl:inverseOf *P*} with $P \in I$. We use **PRP** for the set of all property elements in a given RDF graph. OWL QL further distinguishes two types of class expressions with different syntactic constraints. The set **SBC** of *subclasses in G* consists of all IRIs and all blank nodes *x* that occur in a pattern {*x* owl:onProperty *P*; owl:someValuesFrom owl:Thing}, where $P \in$ **PRP**. The set **SPC** of *superclasses in G* is defined recursively as follows. An element *x* is in **SPC** if it is in $I \cup B$, and *G* contains one of the following patterns:

- {x owl:onProperty **PRP**; owl:someValuesFrom y} where $y \in$ **SPC**;
- {x owl:intersectionOf (y_1, \ldots, y_n)} where $y_1, \ldots, y_n \in SPC$;
- {x owl:complementOf y} where $y \in$ SBC.

G is an *OWL QL ontology* if it uses (only) the following triple "patterns" (unrelated to SPARQL triple patterns) to encode *axioms*:

- {I PRP I}
- I rdf:type SPC
- {SBC rdfs:subClassOf SPC}

3 The owL specification uses the term *punning* for this feature [Hitzler, Krötzsch et al. 2009].

- {SBC owl:equivalentClass SBC}
- \$ {SBC owl:disjointWith SBC}
- {PRP rdfs:range SPC}
- {PRP rdfs:domain SPC}
- {PRP rdfs:subPropertyOf PRP}
- {PRP owl:equivalentProperty PRP}
- {PRP owl:inverseOf PRP}
- {PRP owl:propertyDisjointWith PRP}
- I {I owl:differentFrom I}
- \$ {B rdf:type owl:AllDisjointClasses; owl:members (SBC, ..., SBC)}
- B rdf:type owl:AllDisjointProperties; owl:members (PRP, ..., PRP)
- {B rdf:type owl:AllDifferent; owl:members (I, ..., I)}

G is an OWL QL ontology if every triple in *G* is part of a unique axiom, a unique complex class or property definition used in such axioms. For simplicity, we ignore triples used in annotations or ontology headers. Moreover, we do not consider the following OWL QL property characteristics: symmetry, asymmetry and global reflexivity. Asymmetry and reflexivity are not a problem, but their explicit treatment would inflate our presentation considerably. Symmetry, in contrast, cannot be supported with SPARQL 1.1, as we have shown in Bischof, Krötzsch et al. [2014a]. This is not a major limitation of our approach, since symmetry can be expressed using inverses. This shows that rewritability of an ontology language does not depend on ontological expressiveness alone.

The semantics of OWL QL is inherited from OWL DL. However, since the OWL QL profile does not support any form of disjunctive information, one can also describe the semantics by defining a *universal model*, i.e., a structure that realizes all entailments of an ontology, but no additional entailments. Such a "least model" exactly captures the semantics of an ontology.

To define a universal model for OWL QL, we define a set of RDF-based inference rules, similar to the rules given for OWL RL in the standard [Motik, Cuenca Grau et al. 2009]. In contrast to OWL RL, however, the application of rules can introduce new elements to an RDF graph, and the universal model that is obtained in the limit is not finite in general. Indeed, our goal is not to give a practical reasoning algorithm, but to define the semantics of OWL QL in a way that is useful for analysing the correctness of the rewriting algorithms we introduce.

The main rules for reasoning in OWL QL are defined in Table 3.1. A rule is *applicable* if the premise on the left matches the current RDF graph and the conclusion on the right does not match the current graph; in this case, the conclusion is added to the graph. In the case of rule (3.2), this requires us to create a fresh blank node. In all other cases, we only add new triples composed of existing elements. Rules like (3.3) are actually schemas for an infinite number of rules for lists of any length *n* and any index $i \in \{1, ..., n\}$. Rules Table 3.1: RDF inference rules for OWL QL

\rightarrow [] rdf:type owl:Thing	(3.1)
?X rdf:type [owl:onProperty ?P;	
owl:someValuesFrom $?C] \rightarrow ?X ?P [rdf:type ?C]$	(3.2)
?X rdf:type [owl:intersectionOf	
$(C_1, \ldots, C_i, \ldots, C_n) \rightarrow X \text{ rdf:type } C_i$	(3.3)
?X rdf:type ?C . ?C rdfs:subClassOf ?D \rightarrow ?X rdf:type ?D	(3.4)
?X rdf:type ?C . ?C owl:equivalentClass ?D \rightarrow ?X rdf:type ?D	(3.5)
?X rdf:type ?C . ?D owl:equivalentClass ?C \rightarrow ?X rdf:type ?D	(3.6)
?X ?P ?Y . ?C owl:onProperty ?P;	
owl:someValuesFrom owl:Thing \rightarrow ?X rdf:type ?C	(3.7)
?X ?P ?Y . ?P rdfs:domain ?C \rightarrow ?X rdf:type ?C	(3.8)
?X ?P ?Y . ?P rdfs:range ?C \rightarrow ?Y rdf:type ?C	(3.9)
?X ?P ?Y . ?P owl:inverseOf ?Q \rightarrow ?Y ?Q ?X	(3.10)
?X ?P ?Y . ?Q owl:inverseOf ?P \rightarrow ?Y ?Q ?X	(3.11)
?X ?P ?Y . ?P rdfs:subPropertyOf ?Q \rightarrow ?X ?Q ?Y	(3.12)
?X ?P ?Y . ?P owl:equivalentProperty ?Q \rightarrow ?X ?Q ?Y	(3.13)
?X ?P ?Y . ?Q owl:equivalentProperty ?P \rightarrow ?X ?Q ?Y	(3.14)
INDIVIDUAL(?X) \rightarrow ?X rdf:type owl:Thing	(3.15)
?X rdf:type owl:Thing . ?Y rdf:type owl:Thing \rightarrow ?X owl:topObjectProperty ?Y	(3.16)

(3.15)-(3.16) cover owl:Thing and owl:topObjectProperty, which lead to conclusions that are true for "all" individuals. To ensure standard use, we cannot simply assert *x* rdf:type owl:Thing for *every* IRI *x*, and we restrict instead to IRIS that are used as individuals in the ontology.

We define INDIVIDUAL(x) to be the following SPARQL pattern:

{x rdf:type owl:NamedIndividual} UNION {x rdf:type ?C . ?C rdf:type owl:Class} UNION {x ?P ?Y . ?P rdf:type owl:ObjectProperty} UNION {?Y ?P x . ?P rdf:type owl:ObjectProperty}

Note that this also covers any newly introduced individuals.

Definition 3.1. The *chase* G' of an OWL QL ontology G is a possibly infinite RDF graph obtained from G by application of the rules of Table 3.1, where every rule that is applicable has eventually been applied.

Finally, some features of OWL QL can only make the ontology inconsistent, but not introduce any other kinds of positive entailments, according to the patterns shown in Table 3.2. If any of these match, the ontology is inconsistent, every OWL axiom is a logical consequence, and there is no universal model.

The following corollary follows directly from Definition 3.1 and entailment for the two cases of a consistent and of an inconsistent ontology. Table 3.2: RDF inference patterns for inconsistency in OWL QL

?X owl:bottomObjectProperty ?Y	(3.17)
?X rdf:type owl:Nothing	(3.18)
?X rdf:type ?C . ?X rdf:type [owl:complementOf ?C]	(3.19)
?X rdf:type ?C . ?X rdf:type ?D . ?C owl:disjointWith ?D	(3.20)
?X rdf:type ?C _i . ?X rdf:type ?C _j .	
_:b rdf:type owl:AllDisjointClasses; owl:members $(?C_1, \ldots, ?C_i, \ldots, ?C_j, \ldots, ?C_n)$	(3.21)
?X ?P ?Y . ?X ?Q ?Y . ?P owl:propertyDisjointWith ?Q	(3.22)
?X ?P _i ?Y . ?X ?P _j ?Y:b rdf:type owl:AllDisjointProperties;	
owl:members (?P1,, ?P _i ,, ?P _j ,, ?P _n)	(3.23)
?X owl:differentFrom ?X	(3.24)
_:b rdf:type owl:AllDifferent; owl:members $(?I_1, \ldots, ?X, \ldots, ?X, \ldots, ?I_n)$	(3.25)

Corollary 3.1. Consider an OWL QL ontology G with chase G' and a basic graph pattern P. A variable mapping μ is a solution for P over G under the OWL DL entailment regime iff either (1) μ is a solution for P over G' under simple entailment, or (2) one of the patterns of Table 3.2 matches G'.

3.3 OWL QL Reasoning with SPARQL Path Expressions

Next, we define SPARQL 1.1 queries to solve standard reasoning tasks of the OWL QL profile. We start with simple cases, and then consider increasingly complex reasoning problems.

We first focus on the property hierarchy. An axiom of the form p rdfs:sub-PropertyOf q is entailed by an ontology G if, for newly introduced individuals a and b, $G \cup \{a \ p \ b\}$ entails $\{a \ q \ b\}$. By Corollary 3.1, the rules of Section 3.2 represent all possibilities for deriving this information. In this particular case, we can see that only rules (3.10)-(3.14) in Table 3.1 can derive a triple of the form $a \ q \ b$, where q is a regular property. The case q = owl:topObjectPropertyis easy to handle, since p rdfs:subPropertyOf owl:topObjectProperty is always true (which is also shown by rules (3.15) and (3.16)). In addition, it might be that $G \cup \{a \ p \ b\}$ is inconsistent, implied by rules of Table 3.2; we will ignore this case for now, since it requires more powerful reasoning, and come back to it later in this section.

Definition 3.2. We introduce sPO, invOf and eqP as abbreviations for rdfs:sub-PropertyOf, owl:inverseOf and owl:equivalentProperty, respectively, and define the following composite property path expressions

> SpoEqp := (spo | eqP | ^eqP) Inv := (invOf | ^invOf) subPropertyOf := (SpoEqp | (Inv / SpoEqp* / Inv))* subInvPropertyOf := SpoEqp* / Inv / subPropertyOf

Moreover, for an arbitrary term x, let UNIVPROPERTY[x] be the following pattern: {owl:topObjectProperty (SPOEQP | INV)* x}.

The pattern SUBPROPERTYOF does not check for property subsumption that is caused by the inconsistency rules in Table 3.2, but it can be used to check for subsumptions related to owl:topObjectProperty. This relies on the following correctness property of the pattern UNIVPROPERTY[*p*]. We provide a particularly detailed proof here, since many of our later correctness properties will rely on similar arguments.

Lemma 3.1. Consider a consistent OWL QL ontology G with property $p \in PRP$. Then G entails owl:topObjectProperty rdfs:subPropertyOf p if and only if the pattern UNIVPROPERTY[p] matches G.

Proof. For the "if" direction, we assume that the pattern UNIVPROPERTY[p] matches G. We need to show that G entails owl:topObjectProperty rdfs:sub-PropertyOf p. Using Corollary 3.1, this is equivalent to the claim: the triple _:a p _:b can be derived by applying the deduction rules of Table 3.1 to $G \cup \{ _:a \text{ owl:topObjectProperty }_:b \}$. In particular, we know that the latter is consistent, since otherwise G would clearly be inconsistent as well.

Thus assume a path $(\text{SPoEQP} | \text{INV})^n$ of length $n \ge 0$ from owl:topObject-Property to p. We show the claim by induction on n. For n = 0, p = owl:top-ObjectProperty and the claim is immediate. For n > 0, let p' be the element in the path that is reached after n - 1 steps in the path (and for which the claim was already shown by induction). We distinguish cases according to which of the optional properties q in the pattern connects p' to p:

- If q = rdfs:subPropertyOf, then we can apply rule (3.12) to derive _:a p _:b from _:a p' _:b. Since the latter can be derived from G ∪ {_:a owl:topObject-Property _:b} by the induction hypothesis, the claim follows.
- The cases q = owl:equivalentProperty and q = owl:equivalentProperty are similar using rules (3.13) and (3.14), respectively.
- If q = owl:inverseOf, we can use the same argument as before to obtain a derivation of _:a p _:b from G ∪ {_:b owl:topObjectProperty _:a}, using rule (3.10) in the last step. Note that we apply the induction hypothesis to an input with _:a and _:b swapped. To get the desired derivation, we note that _:b owl:topObjectProperty _:a can be derived from _:a owl:topObjectProperty _:b by applying rule (3.15) to _:a and _:b, followed by rule (3.16).
- The case q = fowl:inverseOf is again similar, using rule (3.11).

For the "only if" direction, assume that _:a p _:b can be derived from the ontology $G \cup \{ _:a \text{ owl:topObjectProperty } _:b \}$ by applying the deduction rules. This can only be accomplished by applying rules (3.12)–(3.16). Moreover, we can assume without loss of generality that (3.15) and (3.16) are only applied at the beginning of the derivation to obtain $\{ _:b \text{ owl:topObjectProperty } _:a \}$ from $\{ _:a \text{ owl:topObjectProperty } _:b \}$ (the latter being the only interesting

derivation that rule (3.16) could produce here). Thus, to simplify our claim, consider a derivation of _:a p _:b can be derived from the following:

```
G \cup \{ :a \text{ owl:topObjectProperty } :b, :b \text{ owl:topObjectProperty } :a \}
```

The proof is by induction on the length ℓ of this derivation We claim that there is a path of the form $(SPOEQP | INV)^n$ of length $n \ge 0$ from owl:topObjectProperty to p.

If $\ell = 0$, p = owl:topObjectProperty the claim is immediate (with n = 0). For $\ell > 0$, we distinguish cases according to the rule applied in the last step of the derivation:

- Rule (3.12), (3.13) or (3.14) applied to a previous consequence {_:a p' _:b}. Then *G* contains a triple p' q p for q = rdfs:subPropertyOf, q = owl:equivalent-Property, or <math>q = `owl:equivalentProperty, respectively. By the induction hypothesis, there is a path as in the claim from owl:topObjectProperty to p'. We can extend this path by p' q p.
- Rule (3.10) or (3.11) applied to a previous consequence {_:b p' _:a}. Then G contains a triple p' q p for q = owl:inverseOf or q = `owl:inverseOf, respectively. The induction hypothesis applies since we can always swap _:a and _:b in a derivation. Thus there is a path as in the claim from owl:topObject-Property to p'. We can extend this path by p' q p.
- Rules (3.15) cannot occur by our assumption on the derivation.

The following result shows the essential correctness property of SUBPROP-ERTYOF on consistent ontologies.

Proposition 3.1. Consider an OWL QL ontology G with properties $p, q \in PRP$ such that $G \cup \{ _:a p _:b \}$ is consistent. Then G entails p rdfs:subPropertyOf q iff the pattern $\{p \text{ subPropertyOf } q\}$ UNION UNIVPROPERTY[q] matches G.

Proof. For the "if" direction, we have to show that the above described calculus allows us to derive the triple _:a q _:b from $G \cup \{ _:a p _:b \}$ whenever the pattern $\{p \text{ subPropertyOf } q\}$ UNION UNIVPROPERTY[q] matches G. We consider both cases of the UNION expression.

First, let p SUBPROPERTYOF q be the matching pattern of the query, that is, we find some $n \in \mathbb{N}$ and a path from p to q matching the regular expression (SPOEQP | (INV / SPOEQP* / INV))ⁿ. We show the claim via an induction over n. For n = 0 we obtain p = q, therefore _:a q _:b holds by assumption.

For the induction step, assume the claim holds for *n* and consider a path matching the expression $(\text{SpoEqp} | (\text{Inv} / \text{SpoEqp}^* / \text{Inv}))^{n+1}$, which means that there is an individual *p*' such that there is a path matching $(\text{SpoEqp} | (\text{Inv} / \text{SpoEqp}^* / \text{Inv}))^n$ from *p* to *p*' and a path matching $(\text{SpoEqp} | (\text{Inv} / \text{SpoEqp}^* / \text{Inv}))^n$ from *p* to *p*' and a path matching $(\text{SpoEqp} | (\text{Inv} / \text{SpoEqp}^* / \text{Inv}))^n$ from *p* to *p*' and a path matching $(\text{SpoEqp} | (\text{Inv} / \text{SpoEqp}^* / \text{Inv}))$ from *p*' to *q*'. By induction hypothesis, there is a derivation for _:a *p*' _:b (†). Now we further analyse the path from *p*' to *q*':

■ If SPOEQP matches this path then, for each of the possible sub-cases of

SPOEQP (viz. rdfs:subPropertyOf, owl:equivalentProperty, or ^owl:equivalent-Property) we find an appropriate rule (namely rule (3.12), (3.13), or (3.14) of Table 3.1, respectively) to derive _:a q _:b from _:a p' _:b.

If the path from p' to q is matched by (INV / SPOEQP* / INV), there are individuals q' and q'', such that there are (i) an INV path from p' to q', (ii) a path from q' to q'' matching SPOEQP^k for some k ≥ 0, and (iii) an INV path from q'' to q.

From (†) and (i), we can obtain _:b q' _:a (‡) via rule 3.10 or 3.11. Given (‡) and (ii), we can perform another induction over k, recalling the above argument regarding SPOEQP, to arrive at _:b q'' _:a. Now, exploiting (iii) and rule 3.10 or 3.11 once more, we finally obtain _:a q' _:b as claimed.

For the second part of the UNION expression, we note that from _:a p _:b, we can infer _:a owl:topObjectProperty _:b by means of rule 3.15 and 3.16. Then, we can invoke Lemma 3.1 to arrive at _:a q _:b as claimed.

For the "only if" direction, assume *G* is such that _:a q _:b can be derived from $G \cup \{ :a \ p \ :b \}$ by applying the deduction rules. If _:a q _:b can be derived from $G \cup \{ :a \ owl: topObjectProperty \ :b \}$, then the claim follows from Lemma 3.1. For the remaining case, we can restrict to derivations of _:a q _:b using rules (3.10)–(3.14). Clearly, any such derivation is linear, with each rule applying to a triple in *G* and a triple of the form _:a q' _:b or _:b q' _:b. Let $p = q_0, \ldots, q_n = q$ be the sequence of properties used in the latter. Only rules (3.10) and (3.11) can swap the order of _:a and _:b, hence there must be an even number of applications of these rules in the derivation. It is easy to see that the expression subProperty of hatches exactly these sequences of properties $q_0 \ldots q_n$.

We will extend this to cover the inconsistent case in Theorem 3.1 below. First, however, we look at entailments of class subsumptions. In this case, the main rules are (3.2)-(3.9). However, several of these rules also depend on property triples derived by rules (3.10)-(3.14), and we apply our results on property subsumption to take this into account.

Definition 3.3. Let eqC and sCO abbreviate owl:equivalentClass and rdfs:sub-ClassOf, respectively. We define property path expressions

```
INTLISTMEMBER := (owl:intersectionOf / rdf:rest* / rdf:first)

SOMEPROP := (owl:onProperty / SUBPROPERTYOF/

(^owl:onProperty | rdfs:domain))

SOMEPROPINV := (owl:onProperty / SUBINVPROPERTYOF / rdfs:range)

SUBCLASSOF := (sCO | eqC | ^eqC | INTLISTMEMBER |

SOMEPROP | SOMEPROPINV)*
```

Moreover, we let UNIVCLASS[*x*] denote the following pattern:

 $\{$ owl:Thing subClassOf $x \}$ UNION

```
{owl:topObjectProperty ((SPOEQP | INV)* /
(^owl:onProperty | rdfs:domain | rdfs:range)/SUBCLASSOF) x}
```

We can use subCLASSOF to check if a superclass expression in *G* is subsumed by a subclass expression in *G*; in particular, this applies to class names. As before, we exclude the possibility that one of the classes is incoherent (i.e., entailed to be equivalent to owl:Nothing).

Proposition 3.2. Consider an OWL QL ontology G with classes $c \in SPC$ and $d \in SBC$ such that $G \cup \{_:a \text{ rdf:type } c\}$ is consistent. Then G entails c rdfs:subClassOf d iff the pattern {c suBCLASSOF d} UNION UNIVCLASS[d] matches G.

Proof. For the "if" direction, we have to show that the above described calculus allows to derive the triple _:a rdf:type d from $G \cup \{ _:a rdf:type c \}$ whenever the pattern $\{c \ subClassOF \ d\}$ UNION univClass[d] matches G. We consider both cases of the UNION expression.

First, let *c* SUBCLASSOF *d* be the matching pattern of the query, that is, we find some $n \in \mathbb{N}$ and a path from *c* to *d* matching the regular expression (sCO | eqC | ^eqC | INTLISTMEMBER | SOMEPROP | SOMEPROPINV)^{*n*}. We show the claim via an induction over *n*. For n = 0 we obtain a = b, therefore _:a rdf:type *d* holds by assumption. For the induction step, assume the claim holds for *n* and consider a path matching the expression (sCO | eqC | ^eqC | INTLISTMEMBER | SOMEPROP | SOMEPROPINV)^{*n*+1} which means that there is a class *c'* such that there is a path matching (sCO | eqC | ^eqC | INTLISTMEMBER | SOMEPROP | SOMEPROPINV)^{*n*} from *c* to *c'* and a path matching (sCO | eqC | ^eqC | INTLISTMEMBER | SOMEPROPINV)^{*n*} from *c'* to *d'*. By induction hypothesis, we can deduce that _:a rdf:type *c'* must hold (†). Now we further analyse the path from *c'* to *d'* by separately considering the 6 disjunctive options:

- c' sCO d': we can use the induction hypothesis and rule (3.4) to infer the triple _:a rdf:type d'.
- c' eqC d': we can use the induction hypothesis and rule (3.5) to infer the triple _:a rdf:type d'.
- c' ^eqC d': we can use the induction hypothesis and rule (3.6) to infer
 _:a rdf:type d'.
- *c'* INTLISTMEMBER *d'*: presuming *G* to be a well-formed OWL QL graph, the regular expression INTLISTMEMBER only matches inside a structure of the shape *x* owl:intersectionOf $(x_1, ..., x_n)$ and connects *x* with some x_i . Then by the induction hypothesis and rule (3.3) we can infer _:a rdf:type *d'*.
- c' SOMEPROP d': in this case there must exist p and q connected by a path matching SUBPROPERTYOF such that G also contains the triples c' owl:onProperty p and either d' owl:onPropertyp or prdfs:domain d'. Again assuming well-formedness of G we can apply rule (3.2) to infer _:a p _:b for some fresh blank node _:b. Consequently, due to Proposition 3.1, we can infer _:a q _:b. Finally applying either rule (3.7) or rule (3.8), we arrive at _:a rdf:type d'.
- c' SOMEPROPINV d': in this case there must exist p and q connected by a

 Table 3.3: Pattern EMPTYCLASS[x] for detecting empty classes.

```
x (sCO | eqC | ^eqC | INTLISTMEMBER | owl:someValuesFrom |
  (owl:onProperty / (INV | SPOEQP)* / (^owl:onProperty | rdfs:domain | rdfs:range)))*
    ?C.{
  {?C SUBCLASSOF owl:Nothing} UNION
  {?C SUBCLASSOF ?D1 . {{?C SUBCLASSOF ?D2} UNION UNIVCLASS[?D2]} . {
    {?D1 disjointClasses ?D2} UNION
    {?V rdf:type owl:AllDisjointClasses . TWOMEMBERS[?V, ?D1, ?D2]}
  }} UNION
  {?C (owl:onProperty / (INV | SPOEQP)^*) ?P . {
    {?P SUBPROPERTYOF owl:bottomObjectProperty} UNION
    {?P SUBPROPERTYOF ?Q1
      {{?P subPropertyOf ?Q2} UNION UNIVPROPERTY[?Q2]}. {
      {?Q1 (owl:PropertyDisjointWith | ^owl:PropertyDisjointWith) ?Q2} UNION
      {?V rdf:type owl:AllDisjointProperties . TWOMEMBERS[?V, ?Q1, ?Q2]}
    }}
  }
}}
```

path matching SUBINVPROPERTYOF such that *G* also contains the triples c' owl:onProperty*p* and *p*rdfs:range d'. We can apply rule (3.2) to infer _:a *p* _:b for some fresh blank node _:b. Consequently, exploiting the argument in the proof of Proposition 3.1, we can infer _:b *q* _:a. Finally applying rule (3.9), we arrive at _:a rdf:type d'.

The case for UNIVCLASS[d] being the matching pattern can be shown in a way analogous to the one above, additionally using Rule (3.15) and rule (3.16) for the base cases.

For the "only if" direction, we have to analyse all possible proofs. For this, it is helpful to distinguish two cases: one where a proof can be found that directly applies the rule (3.15) to all occurrences of proof-tree leafs carrying _:a rdf:type *d*. In such a case, a match to UNIVCLASS[*d*] can be constructed from the proof. In all other cases we can construct a match to {*c* subCLASSOF *d*} in way very analogous to the argument in Proposition 3.2.

Finally, we must identify classes that are incoherent, i.e., for which the triple *c* rdfs:subClassOf owl:Nothing is entailed. To do this, we need to consider the patterns of Table 3.2.

Definition 3.4. For arbitrary terms *x*, *y* and *z*, let TWOMEMBERS[*x*, *y*, *z*] be the pattern {*x*(owl:members/rdf:rest*)?W.?W rdf:first *y*.?W(rdf:rest+/rdf:first)*z*}, and let DISJOINTCLASSES be the property path expression (owl:disjointWith | $^{owl:complementOf}$ | $^{owl:complementOf}$). The query pat-

Table 3.4: Pattern EMPTYPROPERTY[x] for detecting empty properties.

```
x (INV | SpoEqp |
```

- (^owl:onProperty / (sCO | eqC | ^eqC | INTLISTMEMBER | owl:someValuesFrom)*/
 owl:onProperty))* ?P . {
- {?P SUBPROPERTYOF owl:bottomObjectProperty} UNION

{?P subPropertyOf ?Q1

{{?P subPropertyOf ?Q2} UNION UNIVProperty[?Q2]} {
 {?Q1 (owl:PropertyDisjointWith | ^owl:PropertyDisjointWith) ?Q2} UNION
 {?V rdf:type owl:AllDisjointProperties . TWOMEMBERS[?V, ?Q1, ?Q2]}

```
}} UNION
```

```
{?P ((^owl:onProperty | rdfs:domain | rdfs:range) / subClassOF) ?C . {
```

- {?C SUBCLASSOF owl:Nothing} UNION
- {?C subClassOf ?D1 {{?C subClassOf ?D2} UNION univClass[?D2]} {
 {?D1 disjointClasses ?D2} UNION
 - {?V rdf:type owl:AllDisjointClasses . TWOMEMBERS[?V, ?D1, ?D2]}

```
}
```

```
}}
```

```
}}
```

terns EMPTYCLASS[x] and EMPTYPROPERTY[x] are defined as in Table 3.3 and Table 3.4 respectively.

As their names suggest, the patterns of the previous definition allow us to detect classes and properties that must be empty in every model of the ontology. To prove this, we first make some simpler observations:

Lemma 3.2. The pattern TWOMEMBERS[x, y, z] matches an ontology G iff G contains an RDF list x with two distinct elements y and z.

Lemma 3.3. Consider a consistent OWL QL ontology G with class c. Then $G \cup \{ :: a rdf:type c \}$ is inconsistent iff the pattern EMPTYCLASS[c] matches G.

Proof. The general structure of the proof is as in Lemma 3.1, but with a lot more cases to consider. We sketch the arguments in order to avoid getting lost in details here.

First, we can show a property of the first two lines of the pattern in Table 3.3. Namely, the variable ?C in the pattern generally represents a class that must be non-empty whenever the class x (c in our claim) is non-empty. Formally: G has a match for the pattern

```
c (rdfs:subClassOf | owl:equivalentClass | ^owl:equivalentClass |
INTLISTMEMBER | owl:someValuesFrom |
(owl:onProperty / (INV | SPOEQP)*/
(^owl:onProperty | rdfs:domain | rdfs:range))* d
```

if and only if $G \cup \{d \text{ rdfs:subClassOf owl:Nothing}\}$ is consistent but the following is inconsistent: $G \cup \{_:a \text{ rdf:type } c, d \text{ rdfs:subClassOf owl:Nothing}\}$.

This is shown by easy inductions as in Lemma 3.1. Most importantly, we need to observe that non-emptiness of classes can directly follow from the rules (3.1)–(3.9) and (3.15). The cases of (3.1) and (3.15) are not of interest, since they infer non-emptiness of owl:Thing: d in our claim cannot be a superclass of owl:Thing as this would make $G \cup \{d \text{ rdfs:subClassOf owl:Nothing}\}$ inconsistent. Of the remaining rules, (3.2)–(3.6) are are covered by the options rdfs:subClassOf, owl:equivalentClass, `owl:equivalentClass, INTLISTMEMBER and owl:someValuesFrom in the pattern, respectively.

For the remaining cases, we need to take derivations of property assertion triples into account. The only relevant rule to derive such triples from premises of the form _:a rdf:type c' is (3.2). After this, further property triples are inferred as in Proposition 3.1 using rules (3.10)–(3.14), corresponding (as shown before) to the expression (INV | SPOEQP)*. Again, owl:topObjectProperty is not of interest here since we assume $G \cup \{d \text{ rdfs:subClassOf owl:Nothing}\}$ to be consistent. Finally, property assertion triples can be used to transfer new class assertion triples in rules (3.7)–(3.9), corresponding to the final options (^owl:onProperty | rdfs:domain | rdfs:range) in the pattern. This correspondence of rules and patterns can be exploited to obtain the desired result by two inductions, as before.

The remaining parts of the pattern in Table 3.3 lists relevant cases in which the non-emptiness of the class represented by ?C would lead to inconsistency. These cases correspond to the patterns in Table 3.2. The cases (3.18)–(3.21) are covered by the patterns in the third to seventh line of Table 3.2, where we use (reasoning similar to) Proposition 3.2 for the essential correctness of subpatterns UNIVCLASS[?D2] and SUBCLASSOF. Cases (3.17), (3.22) and (3.23) are covered by the remaining lines, where we use Lemma 3.1 and Proposition 3.1 for the essential correctness of subpatterns SUBPROPERTYOF and UNIVPROPERTY[?Q2]. Cases (3.24) and (3.25) can only be violated by *G* initially and thus do not require checking here.

Lemma 3.2 provides the essential correctness of the pattern TWOMEM-BERS[x, y, z] used in several places. For cases (3.17), (3.22) and (3.23), we need to consider property assertion triples that are derived from the non-emptiness of ?C; the pattern used to find a non-empty property ?P is the same pattern that already occurred on the second line, and the same reasoning applies.

Using the correspondences between inference rules and patterns, we can thus prove the overall claim. $\hfill \Box$

Lemma 3.4. Consider a consistent OWL QL ontology G with property p. Then $G \cup \{ _:a p _:b \}$ is inconsistent iff the pattern EMPTYPROPERTY[p] matches G.

Proof. The proof follows the same arguments as the proof of Lemma 3.3. Indeed, many of the subpatterns used are the same, with the main difference being that we now start the derivation from property assertion triples rather than from class assertion triples. $\hfill \Box$

We can now completely express OWL QL schema reasoning in SPARQL 1.1:

Theorem 3.1. An OWL QL ontology G is inconsistent iff it has a match for the pattern

{?X rdf:type ?C . EMPTYCLASS[?C]} UNION
{?X ?P ?Y . EMPTYPROPERTY[?P]} UNION
{?X owl:differentFrom ?X} UNION
{?V rdf:type owl:AllDifferent . TWOMEMBERS[?V, ?X, ?X]}. (3.26)

G entails *c* rdfs:subClassOf *d* for $c \in$ SPC and $d \in$ SBC iff *G* is either inconsistent or has a match for the pattern

{c SUBCLASSOF d} UNION UNIVCLASS[d] UNION EMPTYCLASS[c]. (3.27)

G entails x rdf:type c iff G is either inconsistent or has a match for the pattern

{{x (rdf:type / subClassOF) c} UNION
{x ?P ?Y . ?P (subPropertyOF / (^owl:onProperty | rdfs:domain)/
 subClassOF) c} UNION
{?Y ?P x . ?P (subPropertyOF / rdfs:range / subClassOF) c}
} UNION UNIVCLASS[c] (3.28)

G entails *p* rdfs:subPropertyOf *q* for $p, q \in \mathbf{PRP}$ iff *G* is either inconsistent or has a match for the pattern

{p subPropertyOf q} UNION univProperty[q] UNION emptyProperty[p]. (3.29)

G entails x p y iff G is either inconsistent or has a match for the pattern

{ $x \$?R $y \$.?R subPropertyOf p} UNION { $y \$?R $x \$.?R subInvPropertyOf p} UNION univProperty[p]. (3.30)

Proof. In each of the cases, we can show correctness using similar techniques as in the proof of Lemma 3.1 and the subsequent proofs shown in this section. We consider each case individually.

For (3.26), correctness is an easy consequence of Lemmata 3.3 and 3.4, together with the observation that the two last lines of (3.26) correspond to the cases (3.24) and (3.25) in Table 3.2. We need to use rules (3.1) (for the first time) and (3.16) to see that (3.26) also covers the cases where owl:Thing is a subclass of owl:Nothing, or where owl:topObjectProperty is a subproperty of owl:bottomObjectProperty.

For (3.27), correctness follows from Proposition 3.2 and Lemma 3.3.

For (3.28), we see from Proposition 3.2 why the first and last line are correct. However, Proposition 3.2 only covers derivations that start from a class assertion triple. When checking for the type of an individual in (3.28), the derivation might also start at property assertion triples given in the ontology.

Our arguments in the proof of Proposition 3.2 covered property assertion triples, but only as an intermediate stage of the derivation. It is not hard to see that the second and third line of (3.28) are similar to the respective expressions SOMEPROP and SOMEPROPINV in Definition 3.3, and correctness is shown using the same reasoning as in the proof of Proposition 3.2.

For (3.29), correctness follows from Proposition 3.1 and Lemma 3.4.

For (3.30), correctness is a consequence of the same reasoning as in the proof of Proposition 3.1, together with the observation that SUBINVPROPER-TYOF is similar to SUBPROPERTYOF but swaps the sides. Note that only the rules (3.10)-(3.14) are relevant for normal derivations (not involving owl:top-ObjectProperty, which is covered by Lemma 3.1).

3.4 OWL QL Query Rewriting with SPARQL 1.1

After handling the basic reasoning tasks, namely, consistency checking, subsumption checking and instance checking, we now turn towards *query answering* over OWL QL ontologies using SPARQL 1.1. Research in OWL QL query answering typically considers the problem of answering *conjunctive queries* (CQs), which are conjunctions of OWL property and class assertions that use variables only in the place of individuals, not in the place of properties or classes (e.g. Calvanese, De Giacomo et al. [2007] or Calì, Gottlob and Pieris [2012]. Conjunction can easily be represented by a BGP in SPARQL, yet CQs are not a subset of SPARQL, since they also support (existential quantification of) non-distinguished variables. Normal query variables are called *distinguished*, while existentially quantified variables are called *non-distinguished*. Distinguished variables can only bind to elements of the ontology, whereas for non-distinguished variables it suffices if the ontology implies that some binding must exist.

Example 3.1. Consider an OWL ontology with the assertion :peter rdf:type :Person and the following axiom:

:Person rdfs:subClassOf [owl:onProperty :father; owl:someValuesFrom :Person]

This implies that :peter has some :father but the ontology may not contain any element of which we know that it plays this role. In this case, the SPAR-QL pattern {?X :father ?Y}, equivalent to the conjunctive query $q(?X, ?Y) \leftarrow$:father(?X, ?Y), would not have a match with ?X = :peter under OWL DL entailment. In contrast, if the variable ?Y were non-distinguished, as in the conjunctive query $q(?X) \leftarrow \exists$?Y:father(?X, ?Y), the query would match with ?X = :peter (and ?Y would not receive any binding). \diamond

SPARQL can only express CQs where all variables are distinguished. To define this fragment of SPARQL, recall that the OWL DL entailment regime of SPAR-QL 1.1 requires every variable to be *declared* for a certain type (individual, object property, datatype property, or class) [Glimm and Ogbuji 2013]. This requirement is the analogue of "standard use" on the level of query patterns, and it allows us to focus on instance retrieval here. We thus call a Basic Graph Pattern *P* CQ*-pattern* if:

- 1. *P* does not contain any OWL, RDF, or RDFS IRIS other than rdf:type in property positions,
- 2. all variables in *P* are declared as required by the OWL DL entailment regime,
- 3. property variables occur only in predicate positions,
- 4. class variables occur only as objects of triples with predicate rdf:type.

Rewriting CQ-patterns is then a straightforward application of Theorem 3.1:

Definition 3.5. For a triple pattern *x* rdf:type *c*, the rewriting [x rdf:type c] is the graph pattern (3.28) as in Theorem 3.1; for a triple pattern *x p y* with $p \in \mathbf{PRP}$, the rewriting [x p y] is the graph pattern (3.30). The rewriting [P] of a CQ-pattern *P* is obtained by replacing every triple pattern *s p o* in *P* by $\{[s p o]]\}$.

The following theorem follows from Definition 3.5, Theorem 3.1 and the proof of Theorem 3.1.

Theorem 3.2. If G is the RDF graph of a consistent OWL QL ontology, then the matches of a CQ-pattern P on G under OWL DL entailment are exactly the matches of [P] on G under simple entailment.

As a side remark, for this thesis we are not interested in rewriting general conjunctive queries with non-distinguished variables. However, in Bischof, Krötzsch et al. [2014a] we show how to obtain also such a rewriting.

Limitations We have seen that schema-agnostic query rewriting works for (almost) all of OWL QL, so it is natural to ask how far this approach can be extended. We outline the intuition of the natural limitations of SPARQL 1.1 as a query rewriting language and point out extensions to overcome these limits.

In Section 3.2, we excluded owl:SymmetricProperty from our considerations, because SPARQL 1.1 lacks the necessary expressivity to handle the RDF encoding [Bischof, Krötzsch et al. 2014a]. However, one can write *p* rdf:type owl:SymmetricProperty as *p* rdfs:subPropertyOf [owl:inverseOf *p*] and thus indirectly allow symmetric properties. One possible approach to directly deal with owl:SymmetricProperty is nSPARQL, which has been proposed as an extension of SPARQL 1.0 with a form of path expression that can test for the presence of certain side branches in property paths [J. Pérez, Arenas and Gutierrez 2010]. Similar test expressions have been considered in OBDA recently [Bienvenu, Calvanese et al. 2014].

By complexity-theoretic arguments we can furthermore exclude most ex-

tensions of OWL QL as well as other OWL profiles [Bischof, Krötzsch et al. 2014a]. These complexity-theoretic limitations can only be overcome by using a more complex query language. Many query languages with P-complete data complexity can be found in the Datalog family of languages (see for example Abiteboul, Hull and Vianu [1994]), which are supported by RDF databases like OWLIM and Oracle 11g that include rule engines.

3.5 Optimisation and Implementation Remarks

Theorem 3.2 provides a procedure to rewrite CQ-patterns under OWL DL entailment to SPARQL 1.1 graph patterns under simple entailment. With this rewriting procedure, called *BGP Schema-Agnostic Rewriting* (SAR) we can rewrite SPARQL queries but we in real-world queries will need to consider several practical issues. In this section we discuss these issues and introduce three orthogonal optimisation approaches to improve query evaluation times.

3.5.1 Implementation Remarks

Blank nodes cannot be shared across BGPs in SPARQL [Harris and Seaborne 2013, §4.1.4]. However, since SAR replaces each triple pattern with a UNION pattern, this restriction would lead to invalid queries. For example, the blank node _:x in the BGP {_:x rdf:type b . _:x c d} would be split across several BGPs. The mapping σ from blank nodes to RDF terms (see Definition 2.8) is "lost" outside of the BGP. Therefore, blank node mappings for the same blank node _:x from different BGPs cannot be joined, which contradicts the intended semantics. Since SPARQL variables can substitute blank nodes (under simple entailment) [Gutierrez, Hurtado and Mendelzon 2004; de Bruijn, Franconi and Tessaris 2005], we can retain the semantics by replacing each blank node in a BGP with a unique fresh variable. We call these variables *blank node variables*.

Multiset semantics In the preceding sections we considered SPARQL 1.1 under set semantics for easier handling. Since the official SPARQL semantics [Harris and Seaborne 2013] uses multisets, an implementation of SAR has to cater for duplicate results.⁴ To ensure correct answer cardinalities we could embed each BGP in a SPARQL 1.1 SELECT DISTINCT sub-query which projects the temporary variables away, but keeps the blank node variables which should only be projected away in the end.

In practice, however, users rarely rely on such semantically exact behaviour, but will either use DISTINCT⁵ for the whole query or accept duplicate results. For the rest of this chapter we will accept duplicate results. We note that this might lead to incoherent results considering complex operators such as solution modifiers, grouping and aggregates. 4 This applies to other query rewriting techniques as well, if the target language, like for example sqL, has a multiset semantics.

⁵ which also comes at a certain computational cost

An IMPLEMENTATION has to consider two cases:

First, ccording to (3.28) a triple pattern x rdf:type c is rewritten as follows (expanding UNIVCLASS):

```
\{x (rdf:type / SUBCLASSOF) c\} UNION
```

{*x* ?P ?Y.

```
?P (subPropertyOF / (^owl:onProperty | rdfs:domain) / subClassOF) c} UNION
{?Y ?P x . ?P (subPropertyOF / rdfs:range / subClassOF) c} UNION
{owl:Thing subClassOF c} UNION
{owl:topObjectProperty ((SpoEqP | INV)*/
    (^owl:onProperty | rdfs:domain | rdfs:range)/subClassOF) c} (3.31)
```

Second, for an arbitrary predicate $p \in PRP$ the triple pattern x p y is rewritten according to (3.30) as follows (expanding SUBINVPROPERTYOF):

 $\{ \{x \ ?R \ y \ . \ ?R \ subPropertyOf \ p \} \ UNION \\ \{y \ ?R \ x \ . \ ?R \ SpoEqp^* \ / \ Inv \ / \ subPropertyOf \ p \} \\ \} \ UNION \ univProperty[p]$ (3.32)

The SAR rewriting replaces each triple pattern of a SPARQL query by one of these complex graph patterns. Although the queries grow only by a constant factor, the resulting queries make heavily use of complex path expressions. When expanding the macros in these graph patterns to their definitions–see Listing 3.1 for expanding the macros of (3.31) and Listing 3.2 for expanding the macros of (3.32), where the line numbers given in the margin of the Listing match the lines in the equations—the need for optimization becomes apparent. To address this need we introduce three optimization approaches:

- Algebraic Path Equivalences Without relaxing the main assumption of SAR (no knowledge of the RDF graph required for rewriting) we can implement query optimization heuristics using algebraic equivalences
- *Remove Irrelevant Properties from Paths* By using information about the OWL and RDFs properties used in the ontology we can simplify the path expressions and in some cases also remove BGPs
- *Path Materialization* By allowing updates to the TBox of the RDF graph we can materialise certain path expressions and thereby use a partial ontology saturation approach.

In the remainder of this section we describe these three approaches in detail.

3.5.2 Algebraic Path Equivalences

A SPARQL sequence path could be translated to a BGP [Harris and Seaborne 2013, §18.4]. The path expression x p/q y is thus translated to x p ?v . ?v q y (with ?v being a fresh variable). We can generalize this to extract a common path fragment p over a UNION with the same object y.

Listing 3.1: Resulting graph pattern when expanding all macros of (3.31)

- 1 {{ x rdf:type/((((rdfs:subClassOf|owl:equivalentClass)|^owl:equivalentClass)|((owl:intersectionOf/(rdf :rest)*)/rdf:first))|((owl:onProperty/((((rdfs:subPropertyOf|owl:equivalentProperty)|^owl: equivalentProperty)|(((owl:inverseOf|^owl:inverseOf)/(((rdfs:subPropertyOf|owl: equivalentProperty)|^owl:equivalentProperty))*)/(owl:inverseOf|^owl:inverseOf))))*)/(^owl: onProperty|rdfs:domain)))|((((owl:inverseOf|^owl:inverseOf)/(((rdfs:subPropertyOf|owl:equivalentProperty)|^ owl:equivalentProperty)|(((owl:inverseOf|^owl:inverseOf)/(((rdfs:subPropertyOf|owl:equivalentProperty)|^ owl:equivalentProperty)|(((owl:inverseOf|^owl:inverseOf)/(((rdfs:subPropertyOf|owl: equivalentProperty)|(((owl:inverseOf|^owl:inverseOf|^owl:inverseOf))))*)/(owl: inverseOf|^owl:inverseOf))/(((rdfs:subPropertyOf|owl:equivalentProperty))^owl: equivalentProperty))*)/rdfs:range))* c } UNION
- 2 { *x* ?P ?Y.
- 3 ?P ((((rdfs:subPropertyOf|owl:equivalentProperty)|^owl:equivalentProperty))(((owl:inverseOf|^owl: inverseOf)/(((rdfs:subPropertyOf|owl:equivalentProperty))^owl:equivalentProperty))*)/(owl: inverseOf|^owl:inverseOf))))*/(^owl:onProperty|rdfs:domain)/(((((rdfs:subClassOf|owl: equivalentClass)|^owl:equivalentClass)|((owl:intersectionOf/(rdf:rest)*)/rdf:first))|((owl: onProperty/((((rdfs:subPropertyOf|owl:equivalentProperty)|^owl:equivalentProperty))(((owl: inverseOf|^owl:inverseOf)/(((rdfs:subPropertyOf|owl:equivalentProperty)|^owl: equivalentProperty))*)/(owl:inverseOf|^owl:inverseOf))))*)/(^owl:onProperty|rdfs:domain))) |((((owl:onProperty))*)/(owl:inverseOf|^owl:equivalentProperty)|^owl: equivalentProperty))*)/(owl:inverseOf)/(((rdfs:subPropertyOf|owl:equivalentProperty)|^owl: equivalentProperty))*)/(owl:inverseOf]^owl:inverseOf))))))))/(owl:inverseOf|^owl: equivalentProperty))*)/(owl:inverseOf]^owl:equivalentProperty)|^owl: equivalentProperty))*)/(owl:inverseOf]^owl:inverseOf)))))))/(owl:inverseOf]^owl: equivalentProperty))*)/(owl:inverseOf]^owl:inverseOf]^owl:inverseOf]^owl: equivalentProperty))*)/(owl:inverseOf]^owl:inverseOf]^owl:inverseOf]^owl: equivalentProperty))*)/(owl:inverseOf]^owl:equivalentProperty)]*)/rdfs:range))* c } UNION
- 4 {?Y ?P x . ?P ((((rdfs:subPropertyOf|owl:equivalentProperty)|^owl:equivalentProperty)|(((owl: inverseOf|^owl:inverseOf)/(((rdfs:subPropertyOf|owl:equivalentProperty)|^owl: equivalentProperty))*)/(owl:inverseOf[^owl:inverseOf))))*/rdfs:range/(((((rdfs:subClassOf|owl: equivalentClass)|^owl:equivalentClass)|((owl:intersectionOf/(rdf:rest)*)/rdf:first))|((owl: onProperty/((((rdfs:subPropertyOf|owl:equivalentProperty)|^owl:equivalentProperty))(((owl: inverseOf|^owl:inverseOf)/(((rdfs:subPropertyOf|owl:equivalentProperty)|^owl: equivalentProperty))*)/(owl:inverseOf]^owl:inverseOf)))*)/(^owl:onProperty|rdfs:domain)))|((((owl:onProperty))*)/(owl:inverseOf]^owl:equivalentProperty)|^owl: equivalentProperty))*)/(owl:inverseOf]/owl:equivalentProperty)|^owl: equivalentProperty))*)/(owl:inverseOf]^owl:inverseOf])))*)/(owl:inverseOf[^owl:inverseOf]^owl:inver
- 5 { owl:Thing (((((rdfs:subClassOf|owl:equivalentClass)|^owl:equivalentClass)|((owl:intersectionOf/(rdf: rest)*)/rdf:first))|(((owl:onProperty/((((rdfs:subPropertyOf|owl:equivalentProperty)|^owl: equivalentProperty)|(((owl:inverseOf|^owl:inverseOf)/((((rdfs:subPropertyOf|owl: onProperty|rdfs:domain)))|((((owl:onProperty))*)/(owl:inverseOf|^owl:inverseOf))))*)/(^owl: owl:equivalentProperty)|(((owl:inverseOf[^owl:inverseOf]^owl:equivalentProperty)|^ owl:equivalentProperty)|(((owl:inverseOf]^owl:inverseOf)/(((rdfs:subPropertyOf|owl: equivalentProperty)|(((owl:inverseOf]^owl:inverseOf]^owl:inverseOf])))*)/(owl: inverseOf[^owl:inverseOf)))*)/(owl: inverseOf[^owl:inverseOf)))*)/(owl: equivalentProperty)]*)/rdfs:range))* c } UNION
- 6 { owl:topObjectProperty ((((rdfs:subPropertyOf|owl:equivalentProperty)|^owl:equivalentProperty)|(owl:inverseOf|^owl:inverseOf)))*/((^owl:onProperty|rdfs:domain)|rdfs:range) /((((rdfs: subClassOf|owl:equivalentClass)|^owl:equivalentClass)|((owl:intersectionOf/(rdf:rest)*)/rdf:first))|((owl:onProperty/((((rdfs:subPropertyOf|owl:equivalentProperty)|^owl:equivalentProperty) |(((owl:inverseOf|^owl:inverseOf)/(((rdfs:subPropertyOf|owl:equivalentProperty)|^owl: equivalentProperty))*)/(owl:inverseOf|^owl:inverseOf))))*)/(^owl:onProperty|rdfs:domain)))|((((owl:onProperty))*)/(owl:inverseOf|^owl:equivalentProperty)|^owl:equivalentProperty)|(((owl:inverseOf|^owl:equivalentProperty)|^owl:equivalentProperty)|^owl: equivalentProperty))*)/(owl:inverseOf|^owl:inverseOf))))*)/(owl:inverseOf|^owl:inverseOf)/(((rdfs:subPropertyOf|owl:equivalentProperty)|^owl: equivalentProperty))*)/(owl:inverseOf|^owl:inverseOf)))*)/(owl:inverseOf|^owl:inverseOf)))*/((wl:inverseOf|^owl:inverseOf)))*)/(owl:inverseOf)/(((rdfs:subPropertyOf|owl:equivalentProperty))^owl: equivalentProperty))*/(owl:inverseOf|^owl:inverseOf)))*)/(owl:inverseOf)))*/(((rdfs:subPropertyOf|owl:equivalentProperty))^owl: equivalentPropertyOf|owl:equivalentProperty))*)/rdfs:range))* c }

Listing 3.2: Resulting graph pattern when expanding all macros of (3.32)

- 1 {{ x ?R ?y . ?R (((rdfs:subPropertyOf|owl:equivalentProperty)|^owl:equivalentProperty)|(((owl: inverseOf|^owl:inverseOf)/(((rdfs:subPropertyOf|owl:equivalentProperty)|^owl: equivalentProperty))*)/(owl:inverseOf|^owl:inverseOf)))* p } UNION
- 2 { y ?R x . ?R (((rdfs:subPropertyOf|owl:equivalentProperty)|^owl:equivalentProperty))*/(owl: inverseOf|^owl:inverseOf)/(((rdfs:subPropertyOf|owl:equivalentProperty)|^owl: equivalentProperty)|(((owl:inverseOf|^owl:inverseOf)/(((rdfs:subPropertyOf|owl: equivalentProperty))*)/(owl:inverseOf|^owl:inverseOf))* p }
- 3 }UNION { owl:topObjectProperty (((rdfs:subPropertyOf|owl:equivalentProperty)|^owl: equivalentProperty)|(owl:inverseOf|^owl:inverseOf))* p }}

Lemma 3.5. For the IRIS p, p_1 , p_2 , and the RDF terms x_1 , x_2 , y:

 $\{x_1 p_1 / p y\}$ UNION $\{x_2 p_2 / p y\} \equiv \{? \lor p y\}$. $\{\{x_1 p_1 ? \lor\}$ UNION $\{x_2 p_2 ? \lor\}\}$

where ?V is a fresh variable. A similar equivalence holds for distributivity of a shared prefix path over UNION.

Proof. This follows from the definition of the sequence operator and the distributivity of the join (.) operator over UNION [J. Pérez, Arenas and Gutierrez 2009; Schmidt, Meier and Lausen 2010]. □

Definition 3.6. For (3.31) the *algebraic path equivalences optimisation* (OE) applies Lemma 3.5 from left to right to extract SUBCLASSOF. The triple pattern testing the class *c* being a superclass of owl:Thing is replaced by a BIND pattern. Applying OE to (3.31) thus results in the following graph pattern:

```
{{?V SUBCLASSOF c}.
{{x rdf:type ?V} UNION
{x ?P ?Y . ?P SUBPROPERTYOF / (^owl:onProperty | rdfs:domain) ?V} UNION
{?Y ?P x . ?P (SUBPROPERTYOF / rdfs:range) ?V} UNION
{BIND(owl:Thing AS ?V)} UNION
{owl:topObjectProperty (SPOEQP | INV)*/
    (^owl:onProperty | rdfs:domain | rdfs:range) ?V}} (3.33)
```

For (3.32) OE applies the equivalence (3.5) to reuse SUBPROPERTYOF in the arbitrary predicate rewriting (note that in the first BGP we could replace ?R by ?V):

{?V SUBPROPERTYOF
$$p$$
}.
{{ $x ?V y$ } UNION
{ $y ?R x . ?R SpoEqp^* / Inv ?V$ }
} UNION UNIVPROPERTY[p] (3.34)

Additionally, we will need the following equivalence later for the path materialization optimizations:

$$p^* \equiv (p^+)$$
? (3.35)

Listing 3.3: Resulting graph pattern when expanding all macros of (3.33)

1	{ {?V ((((rdfs:subClassOf owl:equivalentClass) ^owl:equivalentClass) ((owl:intersectionOf/(rdf:rest)*)/
	rdf:first)) ((owl:onProperty/((((rdfs:subPropertyOf owl:equivalentProperty) ^owl:
	equivalentProperty) (((owl:inverseOf ^owl:inverseOf)/(((rdfs:subPropertyOf owl:
	equivalentProperty) ^owl:equivalentProperty))*)/(owl:inverseOf ^owl:inverseOf))))*)/(^owl:
	onProperty rdfs:domain))) ((((owl:onProperty/((((rdfs:subPropertyOf owl:equivalentProperty) ^
	owl:equivalentProperty) (((owl:inverseOf ^owl:inverseOf)/(((rdfs:subPropertyOf owl:
	equivalentProperty) ^owl:equivalentProperty))*)/(owl:inverseOf ^owl:inverseOf))))*)/(owl:
	inverseOf[^owl:inverseOf])/(((rdfs:subPropertyOf[owl:equivalentProperty) ^owl:
	equivalentProperty))*)/rdfs:range))* c } .
2	{ { x rdf:type ?V} UNION
3	{ x ?P _:b0 .?P ((((rdfs:subPropertyOf owl:equivalentProperty) ^owl:equivalentProperty) (((owl: inverseOf ^owl:inverseOf)/(((rdfs:subPropertyOf owl:equivalentProperty) ^owl:
	equivalentProperty))*)/(owl:inverseOf ^owl:inverseOf))))*/(^owl:onProperty rdfs:domain) ? V } UNION
4	{_:b1 ?P x . ?P ((((rdfs:subPropertyOf owl:equivalentProperty) ^owl:equivalentProperty) (((owl:
	inverseOf ^owl:inverseOf)/(((rdfs:subPropertyOf owl:equivalentProperty) ^owl:
	equivalentProperty))*)/(owl:inverseOf ^owl:inverseOf))))*/rdfs:range ?V } UNION
5	{ BIND(owl:Thing AS ?V) } UNION
6	{ owl:topObjectProperty ((((rdfs:subPropertyOf owl:equivalentProperty) ^owl:
	equivalentProperty) (owl:inverseOf ^owl:inverseOf)))*/((^owl:onProperty rdfs:domain) rdfs :range) ?V } } }

Remove Irrelevant Properties from Paths (OI) 3.5.3

If a property *p* never occurs in a graph, then no triple pattern with predicate p will evaluate to a solution mapping. Similarly, when p is used in a path pattern, then this path step will never evaluate to a solution mapping. Thus we can safely remove p from the path pattern and reduce the length and, in some cases, an operator of the paths, while still evaluating to the same solution mappings.

In SAR we are interested in removing OWL/RDFS properties not occurring in the TBox, thus achieving a pay-as-you-go behaviour: ontologies using only few different RDFS and OWL properties lead to shorter rewritten queries.

Definition 3.7. Let ϵ be the *empty reflexive property* of an arbitrary RDF graph G: each IRI in G is connected to itself via ϵ , which is disjoint from any other property. We use \perp as an abbreviation for owl:bottomObjectProperty. For arbitrary path expressions p_1 , p_2 , p_3 we define the following OI rewriting rules on property expressions:

$\perp^* \rightarrow \epsilon$	(3.36)
$\epsilon^* ightarrow \epsilon$	(3.37)
$\perp \rightarrow \perp$	(3.38)
$\hat{\epsilon} \rightarrow \epsilon$	(3.39)
$p_1 \mid \bot \mid p_2 \rightarrow p_1 \mid p_2$	(3.40)
$p_1 \mid \epsilon \mid p_2 \mid \epsilon \mid p_3 \rightarrow p_1 \mid \epsilon \mid p_2 \mid p_3$	(3.41)
$p_1 \ / \ \perp \ / \ p_2 \ ightarrow \perp$	(3.42)
$p_1 \ / \ \epsilon \ / \ p_2 ightarrow p_1 \ / \ p_2$	(3.43)

An OI rule $p' \to p''$ is *applicable* on a path expression p if the path expression p' occurs in p; in this case p' is replaced by p''. The *exhaustive application* of the OI rewriting rules until no rule is applicable anymore, is denoted as $p' \to p''$.

Optional patterns absorb \perp in rule (3.40) while sequence patterns absorb ϵ in rule (3.43). A property removed from a sequence in rule (3.42) is an effective way to remove the whole sequence.

Example. Let *p* be the path expression $a \mid (b / c^*)$. Let us examine what happens when ignoring each of *a*, *b* and *c* in *p* separately:

- When ignoring *a* in *p*, we can apply (3.40) and get the path expression b / c^* .
- When ignoring b in p, we can apply (3.42) and get the path expression consisting only of a.
- When ignoring *c* in *p*, we can apply first (3.36) and get the path expression *p*' = *a* | (*b* / *ε*). Next we can apply (3.43) on *p*' and end up with the path expression *a* | *b*.

We define *I* as the set of all OWL QL properties and $I' \subseteq I$ as the set of all OWL QL properties to ignore. In our case *I'* is comprised of those OWL QL properties not occurring in *G* (we could also selectively ignore properties despite them occurring in the ontology). Then for each $p \in I'$ we replace p by \perp . The OI rewriting rules are applied until no rule is applicable any more. Since each rule shortens the path by removing either a path operator or an IRI, exhaustive rule application is guaranteed to terminate.

Example. When ignoring rdfs:range by replacing rdfs:range with \perp in the paths of (3.33) the one BGP containing rdfs:range will be removed completely by applying the rules (3.42), (3.48) and (3.49). Another interesting case occurs when ignoring owl:inverseOf, thus replacing owl:inverseOf with \perp : The pattern expression subCLASSOF is reduced from originally 36 properties (10 of which are owl:inverseOf) to 12 properties:

```
\begin{split} subCLASSOF &\rightarrow^{*} (sCO \mid eqC \mid ^eqC \mid \\ (owl:intersectionOf / rdf:rest^{*} / rdf:first) \mid \\ (owl:onProperty / (sPO \mid eqP \mid ^eqP)^{*}/(^owl:onProperty \mid rdfs:domain)))^{*} \end{split}
```

Further ignoring owl:onProperty would remove the third line (apart from the final ")*"), while removing any of owl:intersectionOf or rdf:first would remove the second line of the path expression above. Listing 3.4 shows the complete resulting pattern when ignoring owl:inverseOf in Listing 3.3. By ignoring only a single OWL QL property, owl:inverseOf, we could significantly shorten the path expressions.

AFTER EXHAUSTIVELY APPLYING the OI rewriting rules ϵ , which is not directly expressible in SPARQL, can still occur in either 1. in one or more optional

Listing 3.4: Resulting graph pattern when expanding all macros of (3.33) and ignoring owl:inverseOf with OI

	<pre>{ {?V ((((rdfs:subClassOf owl:equivalentClass) ^owl:equivalentClass) ((owl:intersectionOf/(rdf :rest)*)/rdf:first)) ((owl:onProperty/(((rdfs:subPropertyOf owl:equivalentProperty) ^owl :equivalentProperty))*)/(^owl:onProperty rdfs:domain)))* c }</pre>
	$\{x \text{ rdf:type ?V}\}$ UNION
	{ x ?P _:b0 . ?P (((rdfs:subPropertyOf owl:equivalentProperty) ^owl:equivalentProperty))*/(^ owl:onProperty rdfs:domain) ?V } UNION
:	{ _:b1 ?P x . ?P (((rdfs:subPropertyOf owl:equivalentProperty) ^owl:equivalentProperty))*/ rdfs:range ?V } UNION
	{ BIND(owl:Thing AS ?V)} UNION
	{ owl:topObjectProperty (((rdfs:subPropertyOf owl:equivalentProperty) ^owl: equivalentProperty))*/((^owl:onProperty rdfs:domain) rdfs:range) ?V } } }

patterns as a result of (3.41) or 2. as the only remaining property of the whole path expression, as a direct result of (3.36), (3.37) or (3.39). We now discuss these two cases.

1. This case is resolved by rewriting each such optional pattern to the SPAR-QL'?' optional operator:

$$p_1 \mid \epsilon \mid p_2 \to (p_1 \mid p_2)?$$

 Subject and object must represent or bind to the same RDF term, is resolved by the following rewriting rules, where *r* is an RDF term and the expression gp[x/x'] replaces each occurrence of an RDF term or variable *x* in the graph pattern gp by the RDF term or variable x'.

$$gp. \{? \lor \epsilon x\} \to gp[? \lor /r] \tag{3.44}$$

$$gp : \{x \in ?\mathsf{V}\} \to gp[?\mathsf{V}/r] \tag{3.45}$$

$$\{? \mathsf{V} \in x\} \to \{\mathsf{BIND}(x \mathsf{AS} ? \mathsf{V})\}$$
(3.46)

$$\{x \in ?\mathsf{V}\} \to \{\mathsf{BIND}(x \mathsf{AS} ?\mathsf{V})\}$$
(3.47)

It is sufficient to address the cases of either object or subject being a variable for the triple expressions in (3.33) and (3.34). The rules (3.44) and (3.45) are correct because in our rewritings ?V is always a temporary variable occurring only in *gp*.

Now we CAN GENERALISE the OI rewriting rules to special cases of triple patterns and a graph pattern gp, to further simplify graph patterns. Rules (3.48) and (3.49) propagate triple patterns with \perp as predicate.

$$gp : \{x \perp y\} \to \{s \perp o\} \tag{3.48}$$

$$gp \text{ UNION } \{x \perp y\} \to gp$$
 (3.49)

The OI optimization of a path expression p considering the RDF graph G, denoted OI (p, G) is then defined as the exhaustive application of the OI rules on p' where p' is the path expression obtained when replacing all OWL properties not occurring in G by \perp .

In the degenerated case of ignoring *all* OWL and RDFS properties, OI restores the original triple patterns, i.e., after applying OI to the result of SAR the patterns (3.31) and (3.32) collapse back to x rdf:type c and x p y respectively. The same happens when applying OI to OE because in these cases SUBCLASSOF $\rightarrow \epsilon$ and SUBPROPERTYOF $\rightarrow \epsilon$ the rules (3.44) and (3.45) are applied.

3.5.4 Path Materialization

Since SAR always produces the same path patterns regardless of the ontology, it makes sense to materialize these paths to RDF predicates and adapt the rewriter accordingly by replacing the path expression by the temporary predicate.

Definition 3.8. We define a *materialization rule* $c \coloneqq p$ for an IRI c and a path expression p. The path expression p is *materialized* to an RDF graph G according to the materialization rule $c \coloneqq p$ by adding a triple x c y to G whenever x p y matches G.

Materializing a Kleene star expression An issue arises if the outermost operator of a path pattern *p* is a Kleene star (or the optional '?').

Example 3.2. If the WHERE part of a cache insert query of some path *p* looks like ?s p^* ?p then the cache property would be inserted as an identity relation for every IRI in the graph. Not just "ontology nodes" would be affected by also "ABox nodes". Therefore, as the number of cache triples increases with the data, we have to recompute the materialization for *every* update, not only TBox updates.

Materializing Kleene star paths in this manner makes separating TBox and ABox useless. We apply equivalence (3.35) to replace the Kleene star by the one-or-more operator + in this case, and in the query rewriting the cache property is used in an optional pattern.

As an alternative to the optional operator, we could also create a UNION of a triple pattern and a pattern binding the original object term to the variable.

First we define two new classes c:UnivClass and c:UnivProp to mark universal classes and universal properties, respectively. For this we generalize the notion of *materialization rules* to allow an RDF triple on the left hand side and a macro with a variable on the right hand side. Membership of these two new classes is computed with the following macros:

c rdf:type c:UnivClass := UNIVCLASS[c]
p rdf:type c:UnivProp := UNIVPROPERTY[p]

To simplify the notation in the rest of this chapter we assume that in graph G for every universal class c (and property p), which must match UNI-

VCLASS[*c*] (and UNIVPROPERTY[*p*]), there exists a triple *c* rdf:type c:UnivClass (and *p* rdf:type c:UnivProp.

For the materialization optimization we define two different variants:

- *Materialize complete paths* By materializing complete path expressions into the RDF graph and reducing each path pattern in the query to one triple pattern.
- *Materialize Kleene star expression* By materializing the longest Kleene-star expression into the RDF graph and reducing this complex path expression with a single property.

The first variant shortens the path maximally, while the second variant materializes only the (presumably) most costly operator: the Kleene star. We expect better query evaluation times from the first variant, and more space efficient materialization, i.e. less materialized triples, from the second variant. We now explain both variants in detail.

Before we detail the two variants of the mterialization optimization, we define the needed materialization rules.

Definition 3.9. For the path expression p occurring in the patterns (3.28) and (3.30) we define the following materialization rules:

c:dom := subPropertyOF / (^owl:onProperty rdfs:domain)	(3.50)
c:rng := subPropertyOF / rdfs:range	(3.51)
$c:sc \coloneqq (sCO \mid eqC \mid `eqC \mid intListMember \mid someProp \mid somePropInv)^+$	(3.52)
$c:sp := (SpoEqp (Inv / SpoEqp^* / Inv))^+$	(3.53)
$c:spi \coloneqq SpoEqp^* / Inv$	(3.54)
c:spo := SpoEqp ⁺	(3.55)

Materialize complete paths By materializing the complete path expressions we reduce the path pattern maximally, to a single triple pattern. We expect better query evaluation times from this optimization variant than from the following one.

Definition 3.10. Let *G* be an RDF and *gp* either the graph pattern (3.28) or (3.30) Furthermore $c_i := p_i$ is one of the materialization rules (3.50), (3.51) or (3.54), and $d_i := q_i$ is one of the materialization rules (3.52) or (3.53). Then OMA(*gp*) denotes the graph pattern resulting from replacing p_i by *c* and from replacing q_i by d_i ?. Moreover OMA(*G*) denotes the RDF graph obtained by adding a triple *x* c_i *y* for each match of *x* p_i *y*, and adding *x* d_i *y* for each match of *x* q_i *y*.

We can materialize *complete paths* created during SAR rewriting and thus reduce the path patterns in the rewriting to triple patterns and to optional path patterns.

In the rewriting the materialization issue discussed above affects the c:sc and the c:sp properties. Accordingly, we apply equivalence (3.35) to the c:sc

and the c:sp properties. The pattern (3.33) is rewritten by OMA as follows:

{?V c:sc? c}. {{x rdf:type ?V} UNION {x ?P ?Y . ?P c:dom ?V} UNION {?Y ?P x . ?P c:rng ?V} } UNION {c rdf:type c:UnivClass}} (3.56)

The pattern (3.34) is rewritten by OMA as follows:

Materialize longest Kleene star expression A more economic approach, considering the number of materialized triples, is to materialize only the *outer-most Kleene star path fragments*, since these fragments are usually not covered by indexes in existing SPARQL engines and are therefore hard to evaluate.

Definition 3.11. Let *G* be an RDF and *gp* either the graph pattern (3.28) or (3.30) Furthermore $c_i := p_i$ is one of the materialization rules (3.52), (3.53) or (3.55). Then OMS(*gp*) denotes the graph pattern resulting from replacing p_i by c_i ?. Moreover OMS(*G*) denotes the RDF graph obtained by adding a triple $x c_i y$ for each match of $x p_i y$.

Since all the paths materialized in this case have the Kleene star as the outermost operator, all cache properties are affected by the materialization issue discussed above.

The cache properties cache:starSC and cache:subClassOf from OMA optimization are the same. The same applies to the properties cache:starSP and cache:subPropertyOf from OMA.

The optimizations O_I and O_{Mx} (meaning both OMA and OMS) are orthogonal and can be combined to O_{IMx} . The query rewriting for O_{IMx} is the same as for O_{Mx} while the property removal is applied to the materialization queries. The pattern (3.33) is rewritten by OMS as follows:

$\{?V c:sc? c\}.$	
$\{x \text{ rdf:type } ?V\} \text{ UNION}$	
{x ?P ?Y . ?P (c:sp? / (^owl:onProperty rdfs:domain)) ?V} UNION	
{?Y ?P x . ?P (c:sp? / rdfs:range) ?V}	
} UNION {c rdf:type c:UnivClass}}	(3.58)

The pattern (3.34) is rewritten by OMS as follows:

This the semantics but might be infeasible in practice, because the whole materialization, including all cache properties, has to be recomputed for every TBox update. Depending on the actual changes of the TBox, a more refined materialization implementation can deliver better performance. Examples for such improvements are: (i) re-materializing only paths affected by the TBox change (ii) re-materializing only paths for classes or properties affected by the TBox change. Such an algorithm is beyond the scope of this work.

3.5.5 Implementation

We implemented the SAR rewriter as well as the optimization variants introduced in this section. The system takes as an input SPARQL query and rewrites it to a new SPARQL 1.1 query considering the chosen optimization strategy. The resulting query can then be evaluated by the SPARQL 1.1 engine.

The novel main component of a SAR system is the SAR query rewriter. We implemented the SAR rewriting component as a Java library built upon Apache Jena [Apache Jena 2017(a)] for parsing and manipulating SPARQL queries. We provide a command line application and a web user interface.⁶ The implementation can be configured to produce a query rewriting for each of the optimizations described in this section.

Additionally, we implemented an ontology analyser which uses ASK queries to list which OWL/RDFS properties are not used by an ontology; this is needed for OI.

3.6 Evaluation

Comparing a SAR implementation to other systems is difficult because SAR makes different assumptions than other systems.

It is important to note that query rewriting for OWL QL usually depends not only on the query but also the ontology. The ontology is not needed during query evaluation but for query rewriting, whereas the SAR rewriting is independent of the ontology but needs the ontology during query evaluation. This means other OWL QL rewriters need to rewrite the query again when the ontology changes, whereas the resulting SAR queries remain unchanged (except for ontology dependent optimizations).

Additionally, other OWL QL rewriters handle and produce only conjunctive queries and not SPARQL queries. These queries are not necessarily meant to be evaluated on SPARQL engines, although that would be possible in principle. The SAR implementation, however, handles and produces specifically SPARQL queries exploiting specific features of SPARQL that are in fact not present in relational database management systems out-of-the-box.

As comparison system we selected the REQUIEM rewriter [Pérez-Urbina, Motik and Horrocks 2010]. REQUIEM produces a rather small set of union of 6 both are linked from http://stefanbischof.at/sar

Benchmark	TBox	OWL QL fragment	ABox
LUBM (n)	306	246	$n \times 10k$
иовм (<i>n</i>)	977	539	$n \times 25k$
eugen (<i>n,m</i>)	$313 + m \times 80$	$313 + m \times 80$	$n \times 10k$
IMDB-MO	10 523	9 802	44 930 765
FLY	115 136	75 452	32 336
DBPEDIA+	3 1 3 0	3007	29 730 164

 Table 3.5: Number of triples for the different benchmarks

conjunctive queries (for OWL QL ontologies). REQUIEM provides three modes of operation: N for naive, i.e. no optimizations, F for full, i.e. query subsumption and dependency graph pruning or G for greedy, i.e. full plus unfolding of non-recursive non-query clauses.⁷ We adapted the REQUIEM source code to be able to rewrite SPARQL queries and also produce SPARQL queries for the benchmark queries.

We evaluate performance of query rewriting, the path materialization and query evaluation, separately and in total.

Evaluation System We executed the query evaluation on a CentOS Linux server with a 2.4GHz CPU of 8 cores and 64 GB of main memory and Java 7.

3.6.1 Benchmarks

Table 3.5 shows an overview of the different benchmark suites used in this evaluation.

Although, older than a decade, LUBM [Guo, Z. Pan and Heflin 2005] is still the standard benchmark often used when benchmarking OWL reasoners. LUBM contains an ontology from the university domain, a data generator for creating scaled datasets and 14 queries. LUBM contains a data generator creating around 10k triples for each *university*.

UOBM [Ma et al. 2006] is based on LUBM and contains new ontologies and an improved data generator.

EUGEN [Lutz et al. 2013] is an extension of LUBM aimed at benchmarking OBDA systems. The benchmark contains ontologies with varying numbers of subclasses for the classes "Department", "Course", "Student" and "Professor". Furthermore, it contains 6 queries which are longer (in the number of triple patterns) and thus harder to evaluate than LUBM.

IMDB-MO [Rodriguez-Muro, Kontchakov and Zakharyaschev 2013] uses the Movie Ontology (www.movieontology.org) and (the RDF version of) the data from IMDb (www.imdb.com/interfaces).

FLY (http://www.virtualflybrain.org) is an ontology modelling the anatomy of the fly. The ABox is rather small, but the TBox is complex.

DBPEDIA+ [Zhou et al. 2015] is a benchmark with DBPEDIA entities that is combined with an ontology of the tourism domain. The queries are only

7 the *G* optimization targets ontologies beyond OWL QL and will therefore not influence the rewritings [Pérez-Urbina, Horrocks and Motik 2009] atomic queries, i.e. instance retrieval, one query for each class and one for each property of the ontology.

We first created an OWL QL version of each of the used ontologies. The OWL QL extractor removes each OWL QL violation that OWLAPI [Horridge and Bechhofer 2011] reports. This step is necessary because REQUIEM can also rewrite ontology constructs not allowed in OWL QL by using more complex query languages.

3.6.2 SPARQL 1.1 engine

For the evaluation, we use the Blazegraph 1.5.3 triple store.⁸ Blazegraph is a graph database implementing interfaces for both SPARQL 1.1 and property graphs. We use Blazegraph in triples mode, and thus disable features unnecessary for this evaluation such as named graphs, inferencing and full-text index. Blazegraph includes the optional *Runtime Query Optimizer*⁹ (RTO) which is based on ROX [Abdel Kader et al. 2009] to improve join order of high latency queries by sampling different join orderings.

Another popular RDF triple store, OpenLink Virtuoso, showed unexpected behaviour when evaluating our SPARQL queries. Virtuoso is a relational database system which also provides a SPARQL engine. RDF is mapped to relational tables and SPARQL queries are evaluated via SQL queries. Unfortunately, the implementation of path patterns, especially transitivity, in Virtuoso (version 07.20.3214) is not compliant to the SPARQL 1.1 specification:

- 1. Virtuoso cannot evaluate transitive path patterns with both subject and object being unbound variables (depending on the query plan) and reports only the following error: "transitive start not given".
- 2. Virtuoso will not evaluate long queries at all. For many queries generated by our SAR implementation Virtuoso reports the following error: "The SPARQL optimizer has failed to process the query with reasonable quality. The resulting SQL query is abnormally long. Please paraphrase the SPARQL query".

Furthermore, Virtuoso forbids blank nodes as subjects in transitive path patterns with the following message: "Subject of transitive triple pattern should be variable or QName, not literal or blank node". The same applies to blank nodes as objects of transitive path patterns. Since the queries resulting from the SAR rewriting do not contain blank nodes as subjects or objects of path patterns we are not affected by this last limitation.

Let us illustrate these limitations using rewritings for the LUBM queries. Limitation 1 makes evaluation of the SAR and OI rewritings for the LUBM queries 1, 3, 5, 10, 11 and 13 impossible to evaluate on Virtuoso. Limitation 2 makes evaluation of the SAR and OI rewritings for the LUBM queries 2, 4, 7, 8, 9 and 12 as well as the OMS rewritings for the LUBM queries 2 and 9 impossible to evaluate on Virtuoso. Since for each query only one error is reported, it is not 8 http://www.blazegraph.com/

9 https://wiki.blazegraph.com/wiki/ index.php/QueryOptimization# Runtime_Query_Optimizer automatically clear which queries would suffer from both limitations.

Thus of the SAR and OI rewritings, Virtuoso can only evaluate the LUBM queries 6 and 14 (which both consist only of a single type triple pattern). Therefore we assume that the rewriting of type triple patterns is not affected by limitation 1 but that Virtuoso cannot process the arbitrary predicate rewriting.

Next we evaluate SAR and the optimization variations, considering query rewriting, path materialization and query answering.

3.6.3 Rewriting

First we evaluate the query rewriting step. We create 5 variations of all input queries:¹⁰

SAR plain schema-agnostic rewritingR REQUIEM rewritingOI rewriting ignoring non-occurring axiomsOMS rewriting materializing all non-simple star path fragmentsOMA rewriting materializing the complete paths expressions

Rewriting times Since the SAR rewriting depends only on the query and not the ontology, the rewriting times are dominated by parsing before, and query serialization after rewriting. The internal rewriting step is, similar to the RE-QUIEM implementation, only measured by the Java API. The rewriting for each of the queries of LUBM, IMDB-MO and EUGEN took less than 10 ms. While rewriting for OMA and OMS is significantly faster than the rewriting for SAR and OI, all in all the rewriting times are negligible compared to SPARQL query parsing times.

Used RDFs/OWL properties In the benchmark ontologies we found one to four ontology axiom properties we could ignore for the OI optimization as shown in Table 3.6. When considering only the OWL QL fragment, we could often ignore more axiom triples. Table 3.6 shows the OWL properties ignored by the OI optimization for the different ontologies. When reduced to OWL QL, LUBM reduces to RDFs plus owl:inverseOf. DBPEDIA+ was the only benchmark which did not include any kind of property equality or hierarchy.

REQUIEM rewriting Table 3.7 shows the results of REQUIEM, when rewriting queries of the EUGEN benchmark. Independent of the optimization used (full, greedy or naive) the rewriting takes much longer, and, not surprisingly, produces a large number of clauses. For the case of 10 or more subclasses, the EUGEN benchmark is practically infeasible for REQUIEM because the resulting SPARQL queries are not parsable by Blazegraph or Virtuoso anymore due to the high number of BGPS.

10 original and rewritten queries are available at http://stefanbischof.at/sar

Table 3.6: Properties that are ignored by O_I : \circ : property not used in OWL QL fragment ontology, \bullet : property not even used in the original ontology; all ontologies contained rdfs:domain, rdfs:range, rdfs:subClassOf, owl:onProperty and owl:inverseOf properties. Properties marked with \checkmark : occur also in the OWL QL fragment of the ontology and can therefore not be ignored by OI. The lower section of the table lists properties not used in the query rewriting but would only be used for consistency checking.

owl ql property	DBPEDIA+	EUGEN	FLY	IMDB-MO	LUBM	UOBM
rdfs:domain	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark
rdfs:range	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark
rdfs:subPropertyOf	•	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark
rdfs:subClassOf	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark
owl:onProperty	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark
owl:inverseOf	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark
owl:equivalentClass	\checkmark	•	0	\checkmark	•	0
owl:equivalentProperty	•	•	٠	•	•	\checkmark
rdf:first	\checkmark	•	0	\checkmark	0	0
rdf:rest	\checkmark	•	0	\checkmark	0	0
owl:intersectionOf	0	•	0	•	0	0
owl:disjointWith	0	•	0	0	•	0
owl:complementOf	0	•	•	•	•	0
owl:members	•	•	٠	0	•	•
owl:someValuesFrom	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark
owl:propertyDisjointWith	•	•	•	\checkmark	•	•

Table 3.7: REQUIEM rewriting times for the three different optimization variants "Full", "Greedy" and "Naive" in milliseconds and number of conjunctive clauses in the resulting UCQ for the EUGEN ontology with 10 subclasses for the classes "Department", "Course", "Student" and "Professor". Timeouts (>100 seconds) are denoted as "–".

		# of clauses/вдря			Re	ewriting [m	ıs]
Query	# subclasses	Full	Greedy	Naive	Full	Greedy	Naive
1	0	123	123	150	76	64	50
	10	11 453	11 453	11 700	45 988	33 050	5 185
2	0	320	320	2 560	2 591	1 889	871
	10	-	-	45 760	-	-	75 178
3	0	1 760	1 760	3472	4719	3 533	1 191
	10	6 720	6 720	11712	55 480	42 554	5 3 1 7
4	0	480	480	480	295	267	122
	10	-	-	-	-	-	-
5	0	90	90	6 0 7 6	5 809	2 674	1 847
	10	-	-	-	-	-	-
6	0	102	102	792	272	108	101
	10	702	702	10 062	15 711	1 375	3 709

		OMA			OMA and OMS		
Benchmark	c:dom	c:rng	c:spi	c:sc	c:sp	c:spo	
DBPEDIA+	669	584	2	1 922	2	0	
EUGEN 1	69	24	34	453	35	6	
EUGEN 10	69	24	34	753	35	6	
EUGEN 100	69	24	34	3 4 5 3	35	6	
FLY	8 1 4 3	7	8	timeout	41	35	
IMDB-MO	1 290	965	32	1 797	32	5	
LUBM	28	18	6	60	10	6	
UOBM	36	24	17	151	24	16	

Table 3.8: Number of triples generated by the OMA and OMS materializations

Table 3.9: Materialization times of the OMA and OMS optimization in milliseconds

		OMA			OMA and OMS		
Benchmark	c:dom	c:rng	c:spi	C:SC	c:sp	c:spo	
DBPEDIA+	356	74	36	4714	62	23	
EUGEN 1	178	98	45	5810	181	47	
EUGEN 10	171	98	53	8 6 1 1	182	49	
EUGEN 100	165	75	48	14 724	189	54	
FLY	145	83	32	timeout	121	50	
IMDB-MO	302	177	34	31 904	183	33	
LUBM	60	60	44	388	88	43	
UOBM	104	99	50	468	130	45	

3.6.4 Materialization

We consider the materialization queries for OMA and OMS as given in Section 3.5. The materializations were computed by two SPARQL Update queries, one for the OMA case and one for OMS. See Table 3.8 for the number of triples generated by the materialization queries and Table 3.9 for the time in milliseconds needed to compute the materialization on Blazegraph (Blazegraph could compute most of the materializations compared to other engines).

The number of cache triples is similar to the number of ontology triples (compare Table 3.8 with Table 3.5). Although the number of cache triples is significant compared to the ontology, it is negligible compared to the size of the whole graph including the ABox.

A majority of the cache triples result from the subClassOF macro which is also the longest path and the path which takes the longest to compute.

OMA versus OMS The materialization for OMA produces on average approx. 50% more triples than the materialization of OMS. Thus our assumption of the OMS materialization producing a smaller number of triples than the OMA materialization was confirmed by the evaluated ontologies.

In the case of the FLY ontology, we could not materialize the SUBCLASSOF

macro because Blazegraph ran out of heap space even with 12 GB of memory.

3.6.5 Query Answering

Figure 3.1 shows how the answering performance of the different queries in LUBM change when we increase the size of the RDF graph. We evaluated all 14 LUBM queries on 10 different RDF graphs with sizes from 1 to 20 universities where the data of one university amounts to around 10k triples.

With the exception of query 1, OMA is never slower than OMS. For some queries, like query 8 OI was performing even better than OMS.

The rather linear behaviour of some of the optimization variants can be explained by some LUBM queries always delivering the same results (from University0) regardless of the number of universities in the current RDF graph. The data generator creates every university disconnected from all other universities. The query result numbers are not affected by the number of universities for these queries.

Figure 3.2 shows the complete median query evaluation times (query rewriting plus query evaluation on Blazegraph) for SAR, the optimisations OI, OMS and OMA as well as the three requiem variants RN, RG and RF for the REQUIEM variants "naive", "greedy" and "full", respectively, in the different columns. The rows represent the 6 different queries of the EUGEN benchmark. Each query was evaluated for o and 10 subclasses of the classes "Department", "Course", "Student" and "Professor" (see also Table 3.7 before). Furthermore each query was evaluated three times using the standard settings and three times using the runtime optimizer. Missing values for RN, RG and RF stem either from timeouts in the rewriting step (see Table 3.7) or from stack overflow exceptions during query evaluation.

We can see in Figure 3.2 that for most queries REQUIEM could deliver quick results for the case of 0 subclasses, but would run into problems in the case of 10 subclasses; only RG and RF of query 6 would give results in the latter case. This behaviour of returning errors in the case of 10 subclasses is plausible when considering Table 3.7: each of these queries contains thousands of clauses/BGPS.

With the Blazegraph runtime optimizer enabled, the different SAR variants could evaluate most queries within the time limit. In a few cases Blazegraph performed better using the standard settings. With few exceptions, the different SAR rewritings and optimisations could evaluate both cases: o subclasses and 10 subclasses. For 10 subclasses the SAR rewritings and optimisations could perform similarly (in query 6) or better (queries 1, 2, 3 and 5) than any REQUIEM rewriting. The performance increase of the different SAR optimisations,

Figure 3.2 shows clearly that an *schema-agnostic* rewriting using SPARQL property paths *can* perform bettern than an *ontology-dependent* rewriting. In particular this means, that for a wider or deeper class hierarchy, the path-

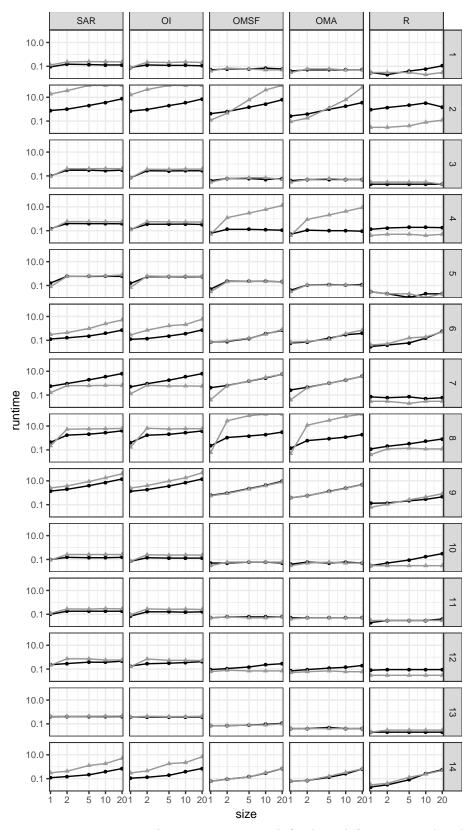


Figure 3.1: LUBM query evaluation times in seconds for the 14 different queries (rows) and optimization variants (columns) from 1 to 20 universities by Blazegraph; the black discs: standard settings; gray triangles: runtime optimizer enable.

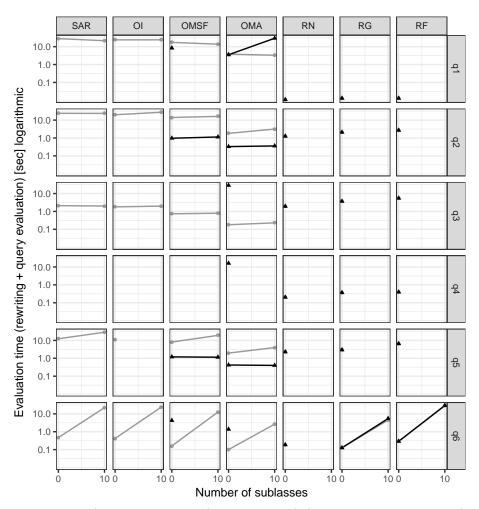


Figure 3.2: Median EUGEN query evaluation times including rewriting times in seconds for the 6 different queries (rows) and optimization variants/systems (columns) for 0 and 10 subclasses for Department, Course, Student and Professor by Blazegraph; the black discs: standard settings; gray triangles: runtime optimizer enabled.

based approach can deliver competitive performance.

3.6.6 Discussion

Query rewriting times are very fast due to the fact that the rewriting algorithm is rather simple and independent of the ontology.

With the exception of the FLY ontology the path materialization was always feasible. The number of materialized triples is shown to be comparable to the total number of ontology triples. OMS is shown to materialize significantly fewer triples than OMA.

Evaluating unoptimized schema-agnostic queries is always slower than evaluating the REQUIEM queries. In some cases a comparable performance with REQUIEM can be achieved with our optimized query rewritings. Generally SAR is better suited for simple queries than for more complex ones.

The different optimizations, especially materialization, showed much bet-

ter performance in many cases than the plain SAR rewriting. Ignoring unused ontology triples OI is usually better than unoptimized SAR. The materialization optimizations are usually better than OI. We have not seen any cases where the application of OI alone would improve query performance significantly. OMA, which needs more materialization triples, is usually better in terms of query evaluation performance than OMS which is more economical with respect to the number of materialised triples. The better query performance of OMA justifies the higher number of materialized triples.

Overall the evaluation showed that SAR rewritings can deliver competitive performance in case of a higher number of subclasses.

IN SUMMARY, schema-agnostic rewriting offers a novel reasoning technique for the OWL QL profile. The rewriting caters for the TBox and ABox being stored in a single RDF graph, and essentially implements an OWL QL reasoner in a SPARQL 1.1 query. The queries generated by the schema-agnostic rewriter are more general than OBDA queries in the sense that no new query rewriting is necessary when the ontology is changed. While the resulting queries are only larger by a constant factor—OBDA query rewritings suffer from an exponential blowup in the worst case—the queries are still large. The evaluation showed that unoptimized schema-agnostic rewriting has to pay a price for this property when comparing it to OBDA approaches which generate queries exactly tailored to the ontology. However, with appropriate optimizations, schema-agnostic rewriting could deliver query evaluation times comparable to OBDA implementations.

4

RDF Attribute Equations

After presenting our approach for schema-agnostic ontological reasoning by exploiting the SPARQL 1.1 feature "property paths", we present in this chapter our approach to reasoning with numerical values by exploiting a different SPARQL 1.1 feature for assigning computed numerical values to a variable. Parts of this chapter have been published as Bischof and Polleres [2013].

Section 4.1 gives a detailed motivation for this chapter. Section 4.2 defines our ontology language DL_{RDFS}^{E} , which extends the RDFS fragment of DL-Lite by simple equations. Section 4.3 defines SPARQL queries over DL_{RDFS}^{E} and presents our query rewriting algorithm, along with a discussion of considerations on soundness and completeness. Section 4.4 discusses alternative implementation approaches of DL_{RDFS}^{E} with DL reasoners and rules. Section 4.5 describes a use case experiment and compares our approach to rule implementations.

4.1 Introduction

A wide range of literature has discussed the completion of data represented in RDF with implicit information through ontologies, mainly through ontological or taxonomic reasoning for classes and properties using RDFS and OWL. However, a lot of implicit knowledge within real-world RDF data does not fall into this category: a large amount of emerging RDF data is composed of numerical attribute-value pairs assigned to resources. These attribute-value pairs, called *datatype properties* in OWL, can contain a lot of implicit information, such as functional dependencies between numerical attributes which are expressible in the form of simple mathematical equations. These dependencies include unit conversions (e.g. between degree Fahrenheit and degree Celsius) or functional dependencies, such as the population density that can be computed from the total population and the area of a populated spatial entity. Such numerical dependencies between datatype properties are not usable for computations in standard ontology languages such as RDFS or OWL. As we will see in Sections 4.4 and 4.5, rule-based approaches also fail to encode such dependencies in the general case.

Example 4.1. Sample RDF data about cities, integrated from sources such as

http://dbpedia.org/
 http://eurostat.linked-statistics.org/

66

DBPEDIA¹ or Eurostat,² may contain data of various levels of completeness and use numerical attributes based on different units like the following:

dbr:Jakarta dbo:tempHighC 33 . dbr:New_York dbo:population 8244910 . dbr:Vienna dbo:population 1714142 . dbr:New_York dbo:tempHighF 84 . dbr:New_York dbo:area_mile2 468.5 . dbr:Vienna dbo:populationDensity 4134 . dbr:Vienna dbo:area_km2 414.6 .

Users familiar with SPARQL might expect to be able to ask for the population density, or for places with temperatures over 90°F with SPARQL queries like the following:

```
SELECT ?C ?P WHERE { ?C dbo:populationDensity ?P } or
SELECT ?C WHERE { ?C dbo:tempHighF ?TempF FILTER(?TempF > 90) }
```

However, answers following implicitly from mathematical knowledge such as the following equations, would not be returned by those queries:

 $\label{eq:constraint} dbo:tempHighC = (dbo:tempHighF - 32) \cdot 5/9$ $\label{eq:constraint} dbo:populationDensity = dbo:population/dbo:area_km2 \qquad \diamondsuit$

One might ask why such equations cannot be directly added to the terminological knowledge modelled in ontologies? We aim to show that it actually can; further, we present an approach to extend the inference machinery for SPARQL query answering under ontologies to cater for such equations. Inspired by query rewriting algorithms for query answering over DL-Lite (see Section 2.3.1), we show how similar ideas can be deployed to extend a DL-Lite fragment covering the core of RDFs with so-called *equation axioms*.

We focus on query rewriting techniques rather than e.g. rule-based approaches such as swRL [Horrocks, Patel-Schneider et al. 2004], where the equations from Example 4.1 could be encoded as follows, given respective arithmetic built-in support in a swRL reasoner:

```
dbo:tempHighC(X, C) \Leftarrow dbo:tempHighF(X, F), C = (F - 32) \cdot 5/9 (4.1)
dbo:populationDensity(X, PD) \Leftarrow popoulation(X, P), area_km2(X, A), PD = P/A (4.2)
```

Where X, C, F, PD, P and A are variables. However, note that these rules are not sufficient to get the desired query results: (i) rule (4.1) is in the "wrong direction" to give results to the query in Example 4.1; that is, we would need different variants of the rule for converting from dbo:tempHighC to dbo:tempHighF and vice versa, and (ii) the above rules are not *DL-safe* [Motik, Ulrike Sattler and Studer 2005], i.e., it does not suffice to bind values only to explicitly named individuals, as we want to compute *new* values, which potentially leads to termination problems in rule-based approaches (as we demonstrate in Section 4.5). Our approach addresses both these points in that: (i) equations are added as first class citizens to the ontology language, where variants are considered directly, and (ii) the presented query rewriting algorithm always

terminates and returns finite answers; we will also discuss reasonable completeness criteria.

4.2 Extending Description Logics by Equations

We herein define a simple, restricted form of arithmetic equations and extend a lightweight fragment of DL-Lite by such equations.

Definition 4.1. Let $\{x_1, \ldots, x_n\}$ be a set of variables. A *simple equation* E is an algebraic equation of the form $x_1 = f(x_2, \ldots, x_n)$ such that $f(x_2, \ldots, x_n)$ is an arithmetic expression over numerical constants and variables x_2, \ldots, x_n , where f uses the elementary algebraic operators $+, -, \cdot, /$ and contains each x_i exactly once. Moreover, by vars(E) we denote the set of variables $\{x_1, \ldots, x_n\}$ appearing in a simple equation E.

That is, we allow non-polynomials for f—since divisions are permitted—but do not allow exponents (different from ±1) for any variable. Such equations can be solved symbolically for each x_i by only applying elementary transformations: i.e., for each x_i , where $2 \le i \le n$, an equivalent equation E' and function f' of the form $x_i = f'(x_1, \ldots, x_{i-1}, x_{i+1}, \ldots, x_n)$ are uniquely determined. Note that since each variable occurs only once, the standard procedure for solving single variable equations can be used. In analogy to the notation used by computer algebra systems (such as Mathematica or Maxima) we write solve($x_1 = f(x_2, \ldots, x_n), x_i$) to denote E' above.

4.2.1 The Description Logic $DL_{\text{RDFS}}^{\text{E}}$

When we talk about Description Logics in this chapter, we consider the RDFS fragment of DL-Lite which we extend by simple (attribute) equations. We call this fragment DL_{RDFS}^{E} , as it is just expressive enough to capture (the DL fragment of) the RDFS semantics [Hayes 2004] extended with equations. In contrast to DL-Lite_A introduced by Poggi et al. [2008], DL_{RDFS}^{E} leaves out property functionality, as well as class and property negation and we restrict ourselves to a single value domain for attributes, the set of rational numbers Q.3

Compared to DL-Lite introduced in Section 2.3 we distinguish properties between *object properties* P, with an IRI $i \in I$ as an RDF triple object, and *attributes* U with a number as the RDF triple object.

Definition 4.2. Let *A* be an atomic class name, *P* be an atomic property name, and *U* be an atomic attribute name. The sets of atomic class names, property names and attribute names are disjoint. Then a DL_{RDFS}^{E} class expression *C* is defined as $C := A \mid \exists P \mid \exists P^{-} \mid \exists U$.

Definition 4.3. A $DL_{\text{RDFS}}^{\text{E}}$ knowledge base (KB) $\mathcal{K} = (\mathcal{T}, \mathcal{A})$ consists of a finite

3 Note that since we only consider this single type of attribute, we also do not introduce value-domain expressions of Poggi et al. [2008]. set of terminological axioms \mathcal{T} (TBox) and assertions \mathcal{A} (ABox). For A, P_1 , P_2 , U_1 , U_2 and C denoting atomic classes, object properties, attributes and class expressions, respectively, \mathcal{T} can contain:

$C \sqsubseteq A$	(class inclusion axiom)
$P_1 \sqsubseteq P_2$	(property inclusion axiom)
$U_1 \sqsubseteq U_2$	(attribute inclusion axiom)
$U_0 = f(U_1,\ldots,U_n)$	(equation axiom)

For $a, b \in I$ and $q \in \mathbb{Q}$, an *ABox* is a set of *class assertions* A(a), *property assertions* P(a, b) and *attribute assertions* U(a, q). Finally, by $I_{\mathcal{K}}$ (and I_A, I_P, I_U , respectively), we denote the (finite) sets of constants from I appearing in \mathcal{K} (as classes, properties and attributes, respectively).

Table 2.1 show the correspondence between the DL syntax and the essential RDFs terminological vocabulary. For attributes, similar to object properties, we allow rdfs:subPropertyOf and ABox assertions. We use datatype literals of the type owl:rational from OWL 2 for rational numbers (which however subsumes datatypes such as xsd:integer and xsd:decimal more commonly used in real-world RDF data). We can encode equation axioms in RDF by means of a new property definedByEquation and write the respective arithmetic expressions $f(U_1, \ldots, U_n)$ as plain literals instead of breaking down the arithmetic expressions into RDF triples. While Sections 4.6 and 6.5 introduce related equation serialization alternatives, we follow the "RDFs scheme" of using a single triple for each axiom. This restriction allows simpler handling of the equations with a SPARQL-based implementation. An equation $U_0 = f(U_1, \ldots, U_n)$ is represented in RDF as U₀ definedByEquation "f(U₁,...,U_n)". In Chapter 6 we will use a specific *datatype* for such equation literals to explicitly type equations and distinguish them from other string literals.

As mentioned before in the context of Definition 4.1, we consider equations that result from just applying elementary algebraic transformations as equivalent. In order to define the semantics of equation axioms accordingly, we will make use of the following definition.

Definition 4.4. Let $E: U_0 = f(U_1, ..., U_n)$ be an equation axiom then, for any U_i with $0 \le i \le n$, we call the equation axiom resulting from solve(E, U_i) the U_i -variant of E.

Note that the DL defined herein encompasses the basic expressivity of RDFS (rdfs:subPropertyOf, rdfs:subClassOf, rdfs:domain and rdfs:range)⁴ and in fact, rather than talking about a restriction of DL-Lite_{\mathcal{R}}, we could also talk about an extension of DL-Lite_{RDFS} [Arenas et al. 2012].⁵

Extending the RDFs fragment of Definition 2.14 we now define the semantics of DL_{RDFS}^{E} .

Definition 4.5 (DL_{RDFS}^{E} model). An interpretation I satisfies an axiom of the form

4 leaving out subtleties such as e.g. those arising from non-standard use [de Bruijn and Heymans 2007] of the RDF vocabulary

5 DL-Lite_{RDFS} allows axioms of the form $P_1 \sqsubseteq P_2^-$, which we will not allow, since these in fact are beyond the basic expressivity of RDFS.

$$C \sqsubseteq A \text{ if } C^{I} \subseteq A^{I}$$

$$P_{1} \sqsubseteq P_{2} \text{ if } P_{1}^{I} \subseteq P_{2}^{I}$$

$$U_{1} \sqsubseteq U_{2} \text{ if } U_{1}^{I} \subseteq U_{2}^{I}$$

$$U_{0} = f(U_{1}, \dots, U_{n}) \text{ if}$$

$$\forall x, y_{1}, \dots, y_{n}(\bigwedge_{i=1}^{n}(x, y_{i}) \in U_{i}^{I}) \land \text{ defined}(f(U_{1}/y_{1}, \dots, U_{n}/y_{n}))$$

$$\Rightarrow (x, \text{ eval}(f(U_{1}/y_{1}, \dots, U_{n}/y_{n})) \in U_{0}^{I}$$

where, by $eval(f(U_1/y_1, \ldots, U_n/y_n))$ we denote the actual value in \mathbb{Q} from evaluating the arithmetic expression $f(U_1, \ldots, U_n)$ after substituting each U_i with y_i , and by defined($f(U_1/y_1, \ldots, U_n/y_n)$) we denote that this value is actually defined (i.e., does not contain a division by zero). Analogously, I satisfies an ABox assertion of the form

- C(a) if $a^{\mathcal{I}} \in C^{\mathcal{I}}$
- P(a, b) if $(a^{I}, b^{I}) \in P^{I}$
- U(a,q) if $(a^{\mathcal{I}},q) \in U^{\mathcal{I}}$

Finally, an interpretation I is called a *model* of a KB $\mathcal{K} = (\mathcal{T}, \mathcal{A})$, written $I \models \mathcal{K}$, if I satisfies all (property, attribute and class) inclusion axioms in \mathcal{T} , all *variants* of equation axioms in \mathcal{T} , and all assertions in \mathcal{A} .

Finally, we define conjunctive queries with assignments over DL_{RDFS}^{E} by extending Definition 2.15 with assignments.

Definition 4.6. A *conjunctive query with assignments* (CQA) is an expression of the form

$$q(\vec{x}) \leftarrow \exists \vec{y}. \phi(\vec{x}, \vec{y})$$

where \vec{x} is a sequence of variables called *distinguished variables*, \vec{y} is a sequence of variables called *non-distinguished variables*, and ϕ is a conjunction of **class**, **property** or **attribute atoms** of the forms C(x), P(x, y), and U(x, z), respectively, and **assignments** of the form $x_0 = f(x_1, \ldots, x_n)$ representing simple equations, where x, y are constant symbols from I or variables (distinguished or non-distinguished), z is either a value from \mathbb{Q} or a variable and the x_i are variables such that for all $i \ge 1$, x_i appears in an atom of the form $U(x, x_i)$ within ϕ . A set of queries with the same head $q(\vec{x})$ is a *union of conjunctive queries with assignments* (UCQA).

For an interpretation I, we denote by q^I the set of tuples \vec{a} of domain elements and elements of \mathbb{Q} which makes ϕ true,⁶ when \vec{a} is assigned to distinguished variables \vec{x} in q.

Definition 4.7. For a CQA q and a KB \mathcal{K} the *answer to* q *over* \mathcal{K} is the set $\operatorname{ans}(q, \mathcal{K})$ consisting of tuples \vec{a} of constants from $I_{\mathcal{K}} \cup \mathbb{Q}$ such that $\vec{a}^{\mathcal{M}} \in q^{\mathcal{M}}$ for every model \mathcal{M} of the KB \mathcal{K} .

Note that, as opposed to most DL-Lite variants (such as [Calvanese, De Giacomo et al. 2007]), $ans(q, \mathcal{K})$ in our setting is not necessarily finite, as shown by the following example. 6 We mean true in the sense of first-order logic, where we assume that the interpretation of arithmetic expressions is built-in with the usual semantics for arithmetic over the rational numbers \mathbb{Q} , and that equality "=" is false for expressions that yield division by zero on the right hand side.

Example 4.2. Let $\mathcal{K}_1 = (\mathcal{T}_1, \mathcal{A}_1)$ with $\mathcal{A}_1 = u_1(o_1, 1), u_2(o_1, 1), u_3(o_1, 1), \mathcal{T}_1 = \{e : u_1 = u_2 + u_3\}$ and $q(x) \leftarrow u_1(o_1, x)$ then $ans(q, \mathcal{K})$ contains each of the natural numbers ≥ 1 .

4.3 SPARQL over RDF Attribute Equations

In order to remain compatible with the notion of CQs in DL_{RDFS}^{E} , we only allow restricted BGPs in SPARQL queries.⁷ Similar to the CQ-patterns defined in Section 3.4, a BGP *p* must not contain any OWL, RDF or RDFS IRIS other than rdf:type in property position.

Following the correspondence of the DL_{RDFS}^E syntax, the RDF syntax and the restrictions we have imposed on BGPs, any BGP *P* can trivially be mapped to a (non-distinguished-variable-free) CQ of the form $q_P: q(vars(P)) \leftarrow \phi(P)$, where vars(*P*) is the set of variables occurring in *P*.

Example 4.3. Within the SPARQL query

SELECT ?X WHERE { { :01 : u1 ?X } FILTER (?X > 1) }

the BGP {:01:u1?X} corresponds to the CQ from Example 4.2.

 \diamond

FILTERs and other complex patterns are evaluated on top of BGP matching:

Definition 4.8 (Basic graph pattern matching for DL_{RDFS}^{E}). Let *G* be an RDF representation of a DL_{RDFS}^{E} KB \mathcal{K} . Then, the solutions of a BGP *P* for *G*, denoted as $[\![P]\!]_{G} = ans(q_{P}, \mathcal{K})$.

Note that here we slightly abused the notation using $ans(q_P, \mathcal{K})$ synonymous for what would be more precisely "the set of SPARQL variable mappings corresponding to $ans(q_P, \mathcal{K})$ ".

Adapting PerfectRef to DL_{RDES}^{E}

Next, we extend the PerfectRef algorithm, given in Algorithm 2.1, which reformulates a conjunctive query to directly encode needed TBox assertions in the query. The algorithm PerfectRefE in Algorithm 4.1 extends the original PerfectRef in Algorithm 2.1 by equation axioms and conjunctive queries containing assignments, as defined before, following the idea of query rewriting by "expanding" a conjunctive query Q to a union of conjunctive queries with assignments Q_0 that is translated to a regular SPARQL 1.1 query.

PerfectRefE first expands the atoms using inclusion axioms (lines 6–8) as in the original PerfectRef algorithm. Here, a DL_{RDFS}^{E} inclusion axiom *I* is *applicable* to a query atom *g* if the function grE (Algorithm 4.2) is defined.⁸ The only addition to Algorithm 4.2, when compared to Algorithm 2.2, is the "adornment" adn(g) of attribute atoms which we explain next, when turning to the expansion of equation axioms.

7 We note though, that soundness of our query rewriting approach would not be affected if we allowed arbitrary BGPs.

8 With DL^E_{RDFS} we cover only a weak DL, but we expect that our extension is applicable to more complex DLs such as the one mentioned by Calvanese, De Giacomo et al. [2007], which we leave for future work.

```
Algorithm 4.1: PerfectRefE(q, T)
```

```
Input: Conjunctive query q, TBox \mathcal{T}
Output: Union of conjunctive queries with assignments
P \coloneqq \{q\}
repeat
     P' := P
     for each q \in P' do
                                                                                      // expansion
           foreach q in q do
                for
each inclusion axiom I in \mathcal{T} do
                     if I is applicable to q then
                       P \coloneqq P \cup \{q[g/\operatorname{grE}(g, I)]\}
                for
each equation axiom E in \mathcal{T} do
                     if q = U^{\operatorname{adn}(g)}(x, y) is an (adorned) attribute atom and
                       vars(E) \cap adn(q) = \emptyset then
                          P \coloneqq P \cup \left\{ q[g/\operatorname{expand}(g, E)] \right\}
until P' = P
return P
```

Algorithm 4.2: grE(*q*, *I*)

if g = A(x) then if $I = A_1 \sqsubseteq A$ then return $A_1(x)$ else if $I = \exists P \sqsubseteq A$ then return $P(x, _)$ else if $I = \exists P^- \sqsubseteq A$ then return $P(_, x)$ else if $I = \exists U \sqsubseteq A$ then return $U(x, _)$ else if g = P(x, y) and $I = P_1 \sqsubseteq P$ then return $P_1(x, y)$ else if $g = U^{\operatorname{adn}(g)}(x, y)$ and $I = U_1 \subseteq U$ then return $U_1^{\operatorname{adn}(g)}(x, y)$

The actually new part of PerfectRefE that reformulates attribute atoms in terms of equation axioms is in lines 9–11. In order to avoid infinite expansion of equation axioms during the rewriting, the algorithm "adorns" attribute atoms in a conjunctive query by a set of attribute names. That is, given an attribute atom U(x, z) and a set of attribute names $\{U_1, \ldots, U_k\}$ we call $g = U^{U_1, \ldots, U_k}(x, z)$ an *adorned attribute atom* and write $adn(g) = \{U_1, \ldots, U_k\}$ to denote the set of adornments. For an unadorned g = U(x, z), obviously $adn(g) = \emptyset$. Accordingly, we call an *adorned conjunctive query* a CQ where adorned attribute atoms are allowed.

For $g = U^{\operatorname{adn}(g)}(x, y)$ and $E' : U = f(U_1, \ldots, U_n)$ being the *U*-variant of *E* the function expand(*g*, *E*) returns the following CQA:

$$U_1^{\operatorname{adn}(g)\cup\{U\}}(x,y_1)\wedge\ldots\wedge U_n^{\operatorname{adn}(g)\cup\{U\}}(x,y_n)\wedge y=f(y_1,\ldots,y_n)$$

where y_1, \ldots, y_n are fresh variables. Here, the condition $vars(E) \cap adn(g) = \emptyset$ ensures that *U* is not "re-used" during expansion to compute its own value recursively. The adornment thus prohibits infinite recursion.

We note that we leave out the *reduction* step of the original PerfectRef algorithm from Algorithm 2.1, since it does not lead to any additional applic-

ability of inclusion axioms in the restricted Description Logic DL_{RDFS}^{E} . As we may extend PerfectRefE to more expressive DLs as part of future work, this step may need to be re-introduced accordingly.

Finally, just as we previously defined how to translate a SPARQL BGP *P* to a conjunctive query, we translate the result of PerfectRefE(q_P, \mathcal{T}) back to SPARQL by means of a recursive translation function tr(PerfectRefE(q_P, \mathcal{T})). That is, for PerfectRefE(q_P, \mathcal{T}) = { q_1, \ldots, q_m } and each q_i being of the form $\bigwedge_{i=0}^{k_i} atom_j$, we define tr as follows:

$$tr(\{q_1, \dots, q_m\}) = \{tr(q_1)\} \cup NION \dots \cup NION\{tr(q_m)\}$$
$$tr(\bigwedge_{j=0}^{k_i} atom_j) = tr(atom_1) \dots tr(atom_{k_i})$$
$$tr(A(x)) = tr(x) rdf:type A$$
$$tr(P(x, y)) = tr(x) \lor tr(y)$$
$$tr(U(x, y)) = tr(x) \cup tr(y)$$
$$tr(y = f(y_1, \dots, y_n)) = BIND(f(tr(y_1), \dots, tr(y_n)) \land Str(y))$$
$$tr(x) = x, \text{ for } x \in V$$
$$tr(x) = x, \text{ for } x \in I$$
$$tr(x) = "x"^{ooultrained}, \text{ for } x \in \mathbb{Q}$$

The following proposition follows from the results in Calvanese, De Giacomo et al. [2007], since PerfectRefE is a restriction of the original PerfectRef algorithm as long as no equation axioms are allowed, and any DL_{RDFS}^{E} KB is consistent.

Proposition 4.1. Let q be a conjunctive query without assignments and $\mathcal{K} = (\mathcal{T}, \mathcal{A})$ be a $DL_{\text{RDFS}}^{\text{E}}$ KB without equation axioms. Then PerfectRefE is sound and complete, i.e.

 $\operatorname{ans}(q, \mathcal{K}) = \operatorname{ans}(\operatorname{PerfectRefE}(q, \mathcal{T}), (\emptyset, \mathcal{A}))$

The following corollary follows similarly.

Corollary 4.1. Let q be a conjunctive query without assignments and without attribute axioms and let $\mathcal{K} = (\mathcal{T}, \mathcal{A})$ be an arbitrary $DL_{\text{RDFS}}^{\text{E}}$ KB. Then PerfectRefE is sound and complete.

As for arbitrary DL_{RDFS}^E knowledge bases, let us return to Example 4.2.

Example 4.4. Given the knowledge base $\mathcal{K}_1 = (\mathcal{T}_1, \mathcal{A}_1)$ and query *q* from Example 4.2. The query PerfectRefE(*q*, \mathcal{T}) is

$$\{q(x) \leftarrow u_1(o_1, x), q(x) \leftarrow u_2^{u_1}(o_1, x_2), u_3^{u_1}(o_1, x_3), x = x_2 + x_3\}$$

which only has the certain answers x = 1 and x = 2, showing that PerfectRefE is incomplete in general. As a variant of \mathcal{K}_1 , lets consider $\mathcal{K}_2 = (\mathcal{T}_1, \mathcal{A}_2)$ with the modified ABox $\mathcal{A}_2 = \{u_1(o_1, 2), u_2(o_1, 1), u_3(o_1, 1)\}$. In this case, PerfectRefE delivers complete results for \mathcal{K}_2 , i.e.,

$$\operatorname{ans}(q, \mathcal{K}_2) = \operatorname{ans}(\operatorname{PerfectRefE}(q, \mathcal{T}_1), (\emptyset, \mathcal{A}_2))$$

 \diamond

with the single certain answer x = 2. Finally, the rewritten version of the SPARQL query in Example 4.3 is

```
SELECT ?X WHERE {{ { :01 :u1 ?X } UNION
        { :01 :u2 ?X2 . :01 :u3 ?X3 . BIND(?X2+?X3 AS ?X) } }
FILTER ( ?X > 1 ) }
```

In order to capture a class of DL_{RDFS}^{E} KBs, where completeness can be retained, we will use the following definition.

Definition 4.9. An ABox \mathcal{A} is *data-coherent* with \mathcal{T} , if there is no pair of ground atoms U(x, d'), U(x, d) with $d \neq d'$ entailed by $\mathcal{K} = (\mathcal{T}, \mathcal{A})$

The following result is obvious.

Lemma 4.1. Whenever \mathcal{A} is data-coherent with \mathcal{T} , any conjunctive query q has a finite number of certain answers.

Proof. Assume that the certain answers to q are infinite. From Corollary 4.1 we can conclude that infiniteness can only stem from distinguished variables that occur as attribute value y in some attribute atom U(x, y) in the query. However, that would in turn mean that there is at least one x with an infinite set of findings for y, which contradicts the assumption of data-coherence. \Box

The following stronger result (which for our particular use case of BGP matching in SPARQL we only consider for non-distinguished-variable-free conjunctive queries) states that data-coherence in fact implies completeness.

Theorem 4.1. If \mathcal{A} is data-coherent with \mathcal{T} , the for any non-distinguishedvariable-free conjunctive query q PerfectRefE is sound and complete.

Proof. The idea here is that whenever \mathcal{A} is *data-coherent* with \mathcal{T} for any fixed x, any certain value y for U(x, y) will be returned by PerfectRefE: assuming the contrary, following a shortest derivation chain U(x, y) can be either: (i) be derived by only atoms $U_i(x, y_i)$ such that any U_i is different from U, in which case this chain would have been "expanded" by PerfectRefE, or (ii) by a derivation chain that involves an instance of U(x, z). Assuming now that $z \neq y$ would violate the assumption of data-coherence, whereas if z = y then U(x, y) was already proven by a shorter derivation chain.

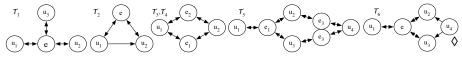
In what follows, we will define a fragment of DL_{RDFS}^E KBs where data-coherence can be checked efficiently. First, we note that a data-coherent ABox alone, such as for instance in \mathcal{K}_2 in Example 4.4 above, is in general not a guarantee for data-coherence. To show this, let us consider the following additional example.

Example 4.5. Consider the TBox $\mathcal{T}_2 = \{e : u_1 = u_2 + 1, u_2 \sqsubseteq u_1\}$ As can be seen, any ABox containing an attribute assertion for either u_1 or u_2 is data-incoherent with \mathcal{T}_2 .

The example also shows that only considering equation axioms is not sufficient to decide data-coherence, as we also need to consider attribute inclusion axioms. Following this intuition, we define a dependency graph over \mathcal{T} as follows.

Definition 4.10. A *TBox dependency graph* $G_{\mathcal{T}} = (N, E)$ is constructed from nodes for each attribute and each equation axiom $N = \{e \mid e \text{ is an equation} axiom in \mathcal{T}\} \cup I_U$. There exist edges (e, v) and (v, e) between every equation eand its variables $v \in \text{vars}(e)$. Furthermore there exists an edge (u, v) for each attribute inclusion axiom $u \sqsubseteq v$. If G contains no (simple) cycle with length greater than 2, then we call \mathcal{T} *attribute-acyclic*.

Example 4.6. Given $\mathcal{T}_1, \mathcal{T}_2$ from Examples 4.2 and 4.5, let further $\mathcal{T}_3 = \{e_1 : u_1 = u_2 + 1, e_2 : u_2 = u_1 + 1\}$, $\mathcal{T}_4 = \{e_1 : u_1 = u_2 + 1, e_2 : u_2 = u_1 - 1\}$, and $\mathcal{T}_5 = \{e_1 : u_1 = u_2 - u_3, e_2 : u_4 = u_2 e_3 : u_4 = u_3\}$ $\mathcal{T}_6 = \{e : u_1 = u_2 - u_3, u_4 \sqsubseteq u_2 u_4 \sqsubseteq u_3\}$ then the resp. dependency graphs are as follows where the graphs for $\mathcal{T}_2 - \mathcal{T}_5$ are cyclic.



Notably, since e_2 is a variant of e_1 in \mathcal{T}_4 , \mathcal{T}_4 is actually equivalent to an acyclic TBox (removing either e_1 or e_2), whereas this is not the case for \mathcal{T}_3 . More refined notions of acyclicity, which we leave for future work, might capture this difference. Furthermore, there is a subtle difference between \mathcal{T}_5 and \mathcal{T}_6 . In \mathcal{T}_5 , when e_1-e_3 are viewed as an equation system, partially solving this system would result in the new equation $u_1 = 0$, independent of the ABox. Since PerfectRefE does not solve any equation systems (but only instantiates equations with values from the ABox), it would not detect this. On the contrary, in \mathcal{T}_6 , only when a concrete "witness" for u_4 is available in the ABox, this constrains the value of u_1 to be 0, which could be correctly detected by means of PerfectRefE: for attribute-acyclic TBoxes, data-coherence (finitely) depends on the ABox, and we can define a procedure to check data-coherence (and thus completeness) by means of PerfectRefE itself.

Proposition 4.2. Let \mathcal{T} be an attribute-acyclic TBox, and $I_U = \{u_1, \ldots, u_m\}$. Then the following SPARQL query $Q_{check}^{\mathcal{T}}$

$$\begin{aligned} \mathsf{ASK} \; & \{ \{ \mathrm{tr}(\mathrm{PerfectRefE}(q_{P_1},\mathcal{T})) \; \mathsf{FILTER}(\mathsf{?Y} \mathrel{!=} \mathsf{?Z}) \} \\ & \quad \mathsf{UNION} \; \dots \; \mathsf{UNION} \\ & \{ \mathrm{tr}(\mathrm{PerfectRefE}(q_{P_m},\mathcal{T})) \; \mathsf{FILTER}(\mathsf{?Y} \mathrel{!=} \mathsf{?Z}) \} \} \end{aligned}$$

where $P_i = \{?X \ u_i \ ?Y \ . ?X \ u_i \ ?Z\}$, determines data-coherence in the following sense: an ABox \mathcal{A} is data-coherent with \mathcal{T} if $Q_{check}^{\mathcal{T}}$ returns "false".

The idea here is that since \mathcal{T} is attribute-acyclic, and due to the restriction that each variable occurs at most once in simple equations, finite witnesses

for data-incoherences can be acyclically derived from the ABox, and thus would be revealed by PerfectRefE.⁹

4.4 Implementation Approaches

Our approach relies on standard SPARQL 1.1 queries and runs on top of any off-the-shelf SPARQL 1.1 implementation by first extracting the TBox and then rewriting BGPs in each query according to the method described in the previous section. In order to compare this rewriting to alternative approaches, we have looked into DL reasoners as well as rule-based reasoners, namely, Racer [Haarslev and Möller 2001], Pellet [Sirin et al. 2007] and Jena Rules [Apache Jena 2017(b)]. We discuss the feasibility of using each of these for query answering under DL^E_{RDFS} separately.

Racer [Haarslev and Möller 2001] does not provide a SPARQL interface but uses its own functional query language *new Racer Query Language* (nRQL). The system allows for modelling some forms of equation axioms, cf. modelling unit conversions in Haarslev and Möller [2003], but Racer only uses these for satisfiability testing and not for query answering. This is orthogonal to our approach, as due to the lack of negation there is no inconsistency in DL_{RDFS}^{E} .

SWRL [Horrocks and Patel-Schneider 2004; Horrocks, Patel-Schneider et al. 2004] implementations like Pellet [Sirin et al. 2007] handle DL-safe rules [Motik, Ulrike Sattler and Studer 2005], that is, rules where each variable appears in at least one non-DL-Atom. We discussed potential modelling of equation axioms as SWRL rules in Example 4.1: as previously noted, rules for *each variant* of each equation axiom must be added to enable query answering for DL_{RDFS}^{E} . Taking this approach, experiments with Pellet showed that queries over certain data-coherent ABoxes were answered correctly; despite—to our reading—rules like (4.1) and (4.2) are not DL-safe in the strict sense. However, we still experienced termination problems when using the data and query in Example 4.1, since strictly speaking, the data for dbr:Vienna is not data-coherent (due to rounding errors). Due to the finite nature of our rewriting, our approach always terminates and is thus sufficiently robust for such—strictly speaking—incoherent data; Section 4.5 will give more details.

Jena¹⁰ provides rule-based inference, on top of its native RDF storage backend TDB, in a proprietary rule language with built-in predicates. Similar to SWRL, we have to encode *all* variants of equation axioms. Jena allows the execution of rules in backward- and forward-chaining mode, where backward execution does not terminate for our rules due to the recursive nature of rules encoding all variants for each equation; this limitation includes empty ABoxes. Forward execution suffers from similar non-termination problems as mentioned in Example 4.1 for incoherent data, whereas forward execution for data-coherent ABoxes might terminate—given no significant rounding er9 As an aside, it suffices to apply the query from Proposition 4.2 to only those attributes u_i appearing in a particular CQ q for determining completeness of the results in this query.

10 http://jena.apache.org/

rors occur during query evaluation. Jena offers hybrid rule-based reasoning where pure RDFs inferencing is executed in a backward-chaining manner, but can still be combined with forward rules. This approach was incomplete in our experiments, because property inclusion axioms did not "trigger" the forward rules modelling equation axioms correctly.

4.5 A Practical Use Case and Experiments

For a prototypical application to compare and compute base indicators of cities—required for studies like Siemens' Green City Index [The Economist Intelligence Unit 2012] as already discussed in Section 1.1—we collected open data about cities from several sources (e.g. DBPEDIA, Eurostat) over several years. When integrating these sources into a joint RDF dataset, various problems such as incoherences, incomplete data or incomparable units along the lines of the extract in Example 4.1 occurred. Most indicators (such as demography, economy, or climate data) comprise numeric values, where functional dependencies modelled as equation axioms are exploitable to arrive at more complete data from the sparse raw values.

For an initial experiment to test the feasibility of the query answering approach presented in this chapter, we assembled a dataset containing an ABox of 254 o81 triples for a total of 3 162 city contexts (i.e., when we speak of a "city", we actually mean one particular city in a particular year) along with the following (attribute-acyclic) TBox:

dbo:tempHighC = $(dbo:tempHighF - 32) \cdot 5/9$	(4.3)
dbo:populationRateMale = dbo:populationMale/dbo:population	(4.4)
dbo:populationRateFemale = dbo:populationFemale/dbo:population	(4.5)
dbo:area_km2 = dbo:area_m2/1000000	(4.6)
dbo:area_km2 = dbo:area_mile2/2.589988110336	(4.7)
dbo:populationDensity = dbo:population/dbo:area_km2	(4.8)
dbo:City \sqsubseteq dbo:Location	
foaf:name ⊑ rdfs:label	
dbo:name ⊑ rdfs:label	

Our prototype system, an early predecessor of the Open City Data Pipeline presented later in Chapter 5, consists of a triple store (Jena TDB), several scripts to crawl, transform and integrate the data from different sources and a simple Web UI to browse the dataset (see Bischof, Polleres and Sperl [2013] for more details on this early prototype).¹¹ The RDF attribute equation rewriter is a separate application, implemented in Java, which takes as inputs a SPARQL query and an ontology, and produces a SPARQL query as output. We use the Jena API to manipulate SPARQL queries and rely on Maxima for the implementation of the solve function.

11 http://citydata.wu.ac.at/KPI-DataPipeline/ Next, we serialise the RDF attribute equations given in Equations (4.3)

to (4.8) to their RDF representation:

```
dbo:tempHighC definedByEquation "(dbo:tempHighF)-32*5/9".
dbo:populationRateMale definedByEquation "dbo:populationMale/dbo:population".
dbo:populationRateFemale definedByEquation "dbo:populationFemale/dbo:population".
dbo:area_km2 definedByEquation "dbo:area_m2/1000000".
dbo:area_km2 definedByEquation "dbo:area_mile2/2.589988110336".
dbo:populationDensity definedByEquation "dbo:population/dbo:area_km2".
```

Moreover, we use the following four queries for our experiments:

Q1 Return the population density of all cities:

```
SELECT ?C ?P
WHERE { ?C rdf:type : City . ?C dbo:populationDensity ?P . }
```

Q2 Select cities with a maximum annual temperature above 90°F:

Q3 Select locations with a label that starts with "W" and a population over 1 million:

Q4 Select places with a higher female than male population rate:

Experimental results are summarized in Table 4.1. For the reasons given in Section 4.4, we compare our approach only to Jena Rules. Experiments were run on the dataset using Jena and ARQ 2.9.2 (with an in-memory RDF graph). We first encoded the essential RDFs rules plus all variants of equation axioms in a straightforward manner as forward rules ("Jena naive"), leading to the expected non-termination problem with data-incoherent data ("Full ABox "). Since the (forward) materialization did not terminate, evaluating query response behaviour was impossible. To circumvent this problem, we created a

Data-coherent ABox Full ABox Our System Jena naive Jena noValue Our System Jena noValue Qı 6.5 >600 30.7 7.3 30.1 Q2 5.8 >600 32.7 5.731.3 Q3 7.8 >600 32.5 8.2 29.0 6.9 >600 Q4 7.9 32.4 34.3

Table 4.1: Response times of queries Q1-Q4 in seconds

data-coherent sample of our dataset ABox (253 114 triples) by removing triples leading to possible incoherences, however still reaching a timeout of 10min for all 4 queries. As an alternative approach, we used Jena's negationas-failure built-in noValue which returns sound but incomplete results, in that it fires a rule only if no value exists for a certain attribute (on the inferences so far or in the data); similar to our approach, this returns complete results for data-coherent datasets and always terminates. As an example of encoding the variants of an axiom in Jena Rules, we show the encoding of equation (4.8) (which is identical to the naive encoding except the noValue predicates). Possible divisions by 0 for an arbitrary division a/b, which we do not need to care about in our SPARQL rewriting, since BIND filters them out (see Section 2.2), are caught by notEqual(b, 0) predicates.

[(? city :area ?ar) (? city :population ?p) notEqual(?ar, 0)
quotient(?p, ?ar, ?pd) noValue(? city : populationDensity)
-> (? city :populationDensity ?d)]
[(? city :area ?ar) (? city :populationDensity ?pd)
product(?ar, ?pd, ?p) noValue(? city : population)
-> (? city :population ?p)]
[(? city :populationDensity ?pd) (? city :population ?p)
notEqual(?pd, 0) quotient(?p, ?pd, ?ar) noValue(? city : area)
-> (? city :area ?ar)]

Overall, while this experiment was primarily a feasibility study of our query-rewriting approach, the results as shown in Table 4.1 are promising: we clearly outperform the only rule-based approach we could compare to.

4.6 Related Work

OWL ontologies for measurements and units such as QUDT [Ralph Hodgson 2011] and OM [Rijgersberg, Assem and Top 2013] provide means to describe units and—to a certain extent—model conversion between these units, though without the concrete machinery to execute these conversions in terms of arbitrary SPARQL queries. Our approach is orthogonal to these efforts in that: (i) it provides not only a modelling tool for unit conversions, but integrates attribute equations as axioms in the ontology language and (ii) allows for a wider range of use cases, beyond conversions between pairs of units only. It would be interesting to investigate whether ontologies like QUDT and OM can be mapped to the framework of DL_{RDFS}^{E} or extensions thereof.

While there exists an extension of OWL with linear equations [Parsia and Uli Sattler 2012], it suffers from the same limitations as Racer's nRQL: the computed values are not available for instance retrieval or querying.

IN SUMMARY, RDF attribute equations provide an ontology language to represent dependencies between numerical indicators and a backward-chaining reasoning approach to compute implicit numerical attributes. In the next Part we will refine this idea in our main use case and explore more approaches to enrich numerical data with different methods. In particular we develop a forward-chaining approach in Chapter 6, with a termination condition similar to the way adornments were used to ensure termination for reasoning with RDF attribute equations in this chapter. To complement the symbolic equations approach, we use statistical methods to further enrich our datasets in Chapter 7. But first, in Chapter 5, we introduce our main use case of collecting and enriching statistical open city data.

PART III

APPLICATION

Open City Data Pipeline

5

In this chapter we introduce the practical motivation for this thesis. We describe the consumed datasets and explain how statistical data is modelled in our system, the *Open City Data Pipeline* (OCDP). Parts of this chapter have been published as Bischof, Harth et al. [2017] and Bischof, Martin et al. [2015a].

Section 5.1 introduces our main use case and, to some extent, details practical motivation for this thesis. Section 5.2 gives an overview of the Open City Data Pipeline architecture, including a description of the data sources and a description of how the resulting dataset is made available in a reusable and sustainable manner via a web interface, a Linked Data interface and a public SPARQL endpoint. Section 5.3 explain data modelling assumptions and decisions necessary for the following chapters.

5.1 Introduction

The public sector collects large amounts of statistical data. For example, the United Nations Statistics Division provides regularly updated statistics about the economy, demographics and social indicators, environment and energy, and gender on a global level.¹ The statistical office of the European Commission, Eurostat, provides statistical data mainly about EU member countries.² Some of the data in Eurostat has been aggregated from the statistical offices of the EU member countries. Several larger cities provide data in on their own open data portals, e.g., Amsterdam,³ Berlin,⁴ London⁵ or Vienna.⁶ Increasingly, such data can be downloaded free of charge and used under open licences.

Open data from these sources can benefit public administrations, citizens and enterprises. The public administrations can use the data for decision support and back policy decisions in a transparent manner. Citizens can be better informed about government decisions, as publicly available data can help to raise awareness and underpin public discussions. Finally, companies could develop new business models and offer tailored solutions to their customers based on such open data. As an example for making use of such data, consider Siemens' Green City Index (GCI) [The Economist Intelligence Unit 2012], which assesses and compares the environmental performance of cities. In order to compute the KPIS used to rank cities' sustainability, the GCI used

- 1 http://unstats.un.org/unsd/
- 2 http://ec.europa.eu/eurostat/
- 3 http://data.amsterdam.nl/
- 4 http://daten.berlin.de/
- 5 http://data.london.gov.uk/
- 6 http://data.wien.gv.at/

qualitative and also quantitative indicators about city performance, such as for instance co_2 emissions or energy consumption per capita. Although many of these quantitative indicators are openly available, the datasets had to be collected, integrated, and checked for integrity violations because of the following reasons: *Heterogeneity*: ambiguous data published by different Open Data sources in different formats, *Missing data*: data that needed to be added or estimated by manual research and, *Outdated data*: soon after the GCI had been published in 2012, its results were likely already obsolete.

Inspired by this concrete use case of the GCI, the goal of the present work is on collecting, integrating, and enriching quantitative indicator data about cities including basic statistical data about demographics, socio-economic factors, or environmental data, in a more automated and integrated fashion to alleviate these problems.

Even though there are many relevant data sources which publish such quantitative indicators as open data, it is still cumbersome to use data from multiple sources in combination, and to keep this data up-to-date. The system we present in this chapter, the Open City Data Pipeline, thus contributes by addressing all of the three above challenges in a holistic manner:

Heterogeneity All this data is published in different formats such as csv, JSON, XML, proprietary formats such as XLS, just as plain HTML tables or within PDF files—and so far to a much lesser degree only as RDF or even as Linked Data [Neumaier, Umbrich and Polleres 2016]. Also, the specifications of the individual data fields—how indicators are defined and how they have been collected—are often implicit in textual descriptions only and have to be processed manually for understanding whether seemingly identical indicators published by different sources are indeed comparable.

We present a systematic approach to integrate statistical data about cities from different sources as *Statistical Linked Data* [Kämpgen, O'Riain and Harth 2012] as a standardised format to publish both the data and the metadata. We build a small ontology of core city indicators, around which we can grow a statistical Linked Data cube: we use standard Linked Data vocabularies such as the RDF Data Cube vocabulary (QB) [Cyganiak, Reynolds and Tennison 2014] to represent data of statistical data cubes, as well as the PROV vocabulary [Lebo, McGuinness and Sahoo 2013] to track the original sources of the data, and we create an extensible pipeline of crawlers and Linked Data wrappers collect this data from the sources.

Missing values Data sources like Eurostat Urban Audit cover many cities and indicators. However, for reasons such as cities providing values on a voluntary basis, the published datasets show a large ratio of missing values. The impact of missing values is aggravated when combining different datasets, due to either covering different cities or using different, non-overlapping sets of indicators.

Our assumption-inspired also by works that suspect the existence of quantitative models behind the working, growth, and scaling of cities [Bettencourt et al. 2007]—is that most indicators in such a scoped domain as cities have their own structure and dependencies, from which we can build statistical prediction models and ontological background knowledge in the form of equations.7 We have developed and combined integrated methods to compute missing values on the one hand using statistical inference, such as different standard regression methods, and on the other hand rule-based inference based on background knowledge in the form of equations that express knowledge about how certain numerical indicators can be computed from others.⁸ While this new method is inspired by our own prior work on using statistical regression methods [Bischof, Martin et al. 2015a] and equational knowledge in isolation [Bischof and Polleres 2013], as we can demonstrate in our evaluation, the combination of both methods outperforms either method used alone. We re-publish the imputed/estimated values, adding respective PROV records, and including error estimates, as Linked Data.

Updates and changes Studies like the GCI are typically outdated soon after publication since reusing or analysing the evolution of their underlying data is difficult. To improve this situation, we need regularly updated, integrated data stores which provide a consolidated, up-to-date view on data from relevant sources.

The extensible single data source wrappers—based on the work around rule-based linked data wrappers by Stadtmüller et al. [2013]—are crawling each integrated source regularly for new data. The crawler are thus keeping the information as up-to-date as possible, while at the same time re-triggering the missing value prediction methods and thereby continuously improving the quality of our estimations for missing data: indeed we can show in our evaluations, later in Chapter 7, that the more data we collect in our pipeline over time, the better our prediction models for missing values get.

IN SUMMARY, the contribution for our main use case is twofold, both in terms of building a practically deployed, concrete system to integrate and enrich statistical data about cities in a uniform, coherent and reusable manner, and contributing novel methods to enrich and assess the quality of Statistical Linked Data:

- 1. As for the former, we present the Open City Data Pipeline which is based on *a generic, extensible architecture* and how we integrate data from multiple data sources that publish numerical data about cities in a modular and extensible way, which we re-publish as Statistical linked data.
- 2. As for the latter, we first describe a novel method to exploit equational knowledge for the case of multidimensional datasets in Chapter 6 by extending RDF attribute equations from Chapter 4, and then combine this

7 We sometimes refer to "predicting" instead of "imputing" values when we mean estimating indicator values for cities and temporal contexts where they are not available. These predictions may be confirmed or refuted, when additional data becomes available. 8 Such equational knowledge could be also understood as "mapping" between indicators, which together with manually crafted equality mappings between indicators published by different data sources can be exploited for enrichment, e.g. if one source publishes the population and area of a city, but not the population density, then this missing value, available for other cities directly from other sources, could be computed by an equation.

86

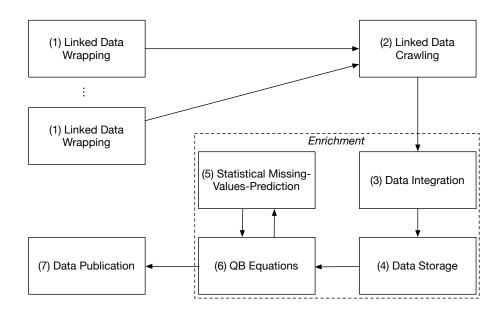


Figure 5.1: Open City Data Pipeline workflow

with statistical regression methods, in order to impute and estimate missing values in Chapter 7.

We also *evaluate* our approach in terms of measuring the errors (by evaluating the estimated root mean square error rate (RMSE) per indicator) of such estimates, demonstrating that firstly, the combination of statistical inference with equations indeed pays off, and secondly, the regular update and collection of additional data through our pipeline contributes to improve our estimations for missing values in terms of accuracy (see also Chapter 7). Note that the method of enrichment by QB equations cannot only be used for imputing missing values, but also be used to assess the quality of ambiguous values from different data sources: by "rating" different observed values for the same indicator, year and city from different sources against their distance to our estimate, we have means to return confidence in different sources in such an integrated system.

5.2 Overview and System Architecture

The workflow of the Open City Data Pipeline (OCDP) is illustrated in Figure 5.1 and consists of the following series of steps:

- 1. Data is provided as Statistical Linked Data via wrappers which have to be created once per source in the "Wrapping step".
- 2. A crawler collects data regularly (currently, weekly) from different sources in the "Crawling" step through the wrappers.
- 3. In the "Data Integration" step the data is integrated into the global cube,

Year(s)	Cities	Indicators	Available	Missing	Missing Ratio (%)
1990	131	88	1 799	9 641	84.27
2000	433	163	6 420	63 996	90.88
2005	598	168	20 460	79 836	79.60
2010	869	193	56 528	110 996	66.26
2015	310	69	2 0 3 0	19 291	90.48
2004-2016	879	207	437 565	1 331 250	75.26
1990–2016	966	209	506 854	2 257 171	81.66

Table 5.1: Values of the Eurostat Dataset

where data is enriched by links and heterogeneities resolved.

- 4. In the "Data Storage step", the data is loaded into a triple store.
- 5. A further enrichment step applies statistical methods for missing values prediction.
- 6. Another enrichment step exploits equational background knowledge in the form of QB equations.
- 7. Finally, in the "Data publication" step, the resulting enriched Linked data is made accessible.

5.2.1 Data Sources

Many statistical data sources, interesting for data analysis, are nowadays openly available. Many indicators in these data sources are provided on a *country* level and only a subset of indicators are available on the *city* level. We have identified the following potential providers of statistical data concerning cities:

- DBPEDIA⁹
- Wikidata¹⁰
- Eurostat with Urban Audit
- United Nations Statistics Division (UNSD) statistics
- US Census Bureau statistics
- Carbon Disclosure Project¹¹
- individual city data portals

In particular, we use statistical data from the UN and from Eurostat, which are integrated and enriched by the OCDP. While the data sources contain data ranging from the years 1990 to 2016, most of the data concerns the years after 2000. Further, not every indicator is covered over all years, where the highest coverage of indicators is between 2004 and 2015 (see Tables 5.1 and 5.2). Most European cities are contained in the Eurostat datasets. The UNSD contains the capital cities and cities with a population over 100 000 from all over the world, all listed in the UN Demographic Yearbook.¹²

The previous version of the OCDP by Bischof, Martin et al. [2015a] contained data from 1990 to 2013 with 638 934 values from Eurostat and 69 772 9 http://dbpedia.org/10 http://wikidata.org/

11 https://www.cdp.net

12 http: //unstats.un.org/unsd/demographic/ products/dyb/dyb2012.htm

Year(s)	Cities	Indicators	Available	Missing	Missing Ratio (%)
1990	5	3	8	7	46.67
2000	1 078	61	3 861	61 836	94.12
2005	777	61	2 1 1 0	45 226	95.54
2010	1 525	64	5 866	91 670	93.99
2015	216	3	568	77	11.94
2004–2016 1990–201)	2 095 3 381	64 64	28 849 40 532	511 759 685 548	94.66 94.42

Table 5.2: Values of the United Nations Dataset

values from the UN data source. Due to some reorganisation in the Eurostat and UN datasets, the Eurostat datasets contain now 506 854 values and the UN provides 40 532 values. Regarding indicators, we now have 209 instead of 215 Eurostat and 64 instead of 154 UN indicators. The reason for the drop in indicators is due to the fact that the UN publishes fewer datasets. The same effect can be seen for the cities, where we have 966 instead of 943 Eurostat and 3 381 instead of 4 319 UN cities. Due to the smaller size of the datasets (see Tables 5.1 and 5.2), we now have an improved missing values ratio of 81.7% (before 86.3%) for Eurostat, respectively 94.4% (before 99.5%) for the UN dataset.

We now describe each of the data sources in detail.

Eurostat Eurostat¹³ offers various datasets concerning different EU statistics. 13 http://ec.europa.eu/eurostat The data collection is conducted by the national statistical institutes and Eurostat itself. Of particular interest is the Urban Audit (UA) collection,¹⁴ which started as an initiative to assess the quality of life in European cities. UA aims to provide an extensive look at the cities under investigation, since it is a policy tool to the European Commission: "The projects' ultimate goal is to contribute towards the improvement of the quality of urban life" [Office for Official Publications of the European Communities 2004]. In the meantime [Eurostat 2016] the goals for UA were aligned with the Europe 2020 strategy¹⁵ which in turn is aligned with the UN 2030 Agenda's Sustainable Development Goal #11: "Make cities and human settlements inclusive, safe, resilient and sustainable" [United Nations 2015a]. Currently, data collection takes place every three years (last survey published in 2015) and is published via Eurostat Urban Audit.¹⁶ All data is provided on a voluntary basis which leads to varying data availability and missing values in the collected datasets. At the city level, Urban Audit contains over 200 indicators divided into the categories Demography, Social Aspects, Economic Aspects, and Civic Involvement. Currently, we extract the datasets that include data for the following topics:

population by structure, age groups, sex, citizenship, and country of birth

- fertility and mortality
- living conditions and education

14 http: //ec.europa.eu/eurostat/web/cities

15 http://ec.europa.eu/europe2020/

16 http: //ec.europa.eu/eurostat/web/cities

- culture and tourism
- labour market, economy, and finance
- transport, environment, and crime

United Nations Statistics Division (UNSD) The UNSD offers data on a wide range of topics such as education, environment, health, technology and tourism for cities worldwide. The focus of the UNSD is usually on the country level, but there are datasets on cities available as well. Our main source is the UNSD Demographic and Social Statistics, which is based on the data collected since 1948 annually by questionnaires to national statistical offices.¹⁷ Currently we use the datasets on the city level that include the following topics:

- population by age distribution, sex, and housing
- households by different criteria (e.g., type of housing)
- occupants of housing units/dwellings by broad types (e.g., size, lighting)
- occupied housing units by different criteria (e.g., walls, waste)

The full UNSD Demographic and Social Statistics data has over 650 indicators, wherein we kept a set of 64 coarse-grained indicators and dropped the most fine-grained indicator level. For example, we keep *housing units total* but drop *housing units 1 room*. We prefer more coarse-grained indicators to avoid large groups of similar indicators which are highly correlated.

5.2.2 Pipeline Components

In order to realise these steps, the architecture of the OCDP system implements several components. Figure 5.2 gives a high level overview of the architecture with a triple store being the central part. The data enrichment workflow uses various methods to improve data quality and enrich the data.

Linked Data Wrappers Currently, none of the mentioned data sources publishes statistical data as Statistical Linked Data upfront. Thus, we use a set of wrappers which publish the data from these sources according to the principles listed in Chapter 2. Appendix B.1 below explains these wrappers in more detail.

Linked Data Crawler A Linked Data crawler starts with a seed list of IRIS and crawls relevant connected Linked Data. The resulting RDF data is collected in one big RDF file and eventually loaded into the triple store. Appendix B.3 explains the linked data crawler in more detail.

Triple Store We use a standard Virtuoso 7 triple store as a central component to store data at different processing stages. For data loading we use the Virtuoso SQL console which allows faster data loading. For all other data access we rely on Virtuoso's SPARQL 1.1 interface which allows us not only to



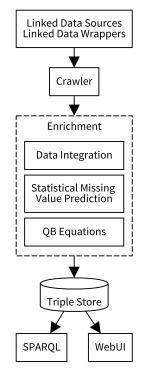


Figure 5.2: Open City Data Pipeline architecture

query for data, but also insert new triples with SPARQL Update (cf. [Gearon, Passant and Polleres 2013]).

Enrichment Component In an iterative approach, we improve data quality of the crawled raw data. This component covers steps (4)-(6) in the workflow shown in Figure 5.1: in this configurable workflow we use several different sub-components corresponding to these steps. Each workflow component first reads input data (=observations) from the triple store via SPARQL queries, processes the data accordingly and inserts new triples into the triple store either via SPARQL Insert queries or the Virtuoso bulk loader facility (the first option is more flexible—it allows the execution of the workflow on a different machine—the second usually allows faster data loading).

The workflow currently uses three different subcomponents corresponding to steps (4), (5) and (6), respectively:

- The Data Integration sub-component, corresponding to step (3), performs linking and data integration steps and materialises the global cube in a separate named graph. This linking and materialisation effectively resolves different types of heterogeneity found in the raw data: (i) different IRIS for members, (ii) different IRIS for dimensions (iii) different DSDS (although the DSDS must be compatible to some extent for the integration to make sense). Eventually, the global cube provides a unified view over many datasets from several sources. This component is implemented with SPARQL Update queries and supplied background knowledge for the integration. The exact process of linking statistical data and the materialisation will be described in more detail in Appendix B.2.
- The Statistical Missing Values Prediction sub-component for missing value prediction, corresponding to step (5), extracts the whole global cube generated by the materialisation as one big data matrix, which is then used for applying different statistical regression methods to train models for missing value prediction. This component is implemented as a set of R scripts which extract the data with SPARQL queries. We then train and evaluate the models for each of the indicators. If the selected model delivers predictions in a satisfactory quality we apply the model and get estimates for the indicators. Finally the component exports the statistical data together with error estimates to one RDF file which is then loaded into the triple store with the Virtuoso bulk load feature and added to the global cube. Chapter 7 explains this component in more detail.
- The *QB Equations* sub-component, corresponding to step (6), uses equations from different sources to infer even more data. To this end, we introduce QB equations. These QB equations provide an RDF representation format for equational knowledge and a rule-based semantics, as well as a forward-chaining implementation to infer new values. QB equations are implementation

ted in a naive rule engine which directly executes SPARQL INSERT queries on the triple store. Chapter 6 introduces the concept of QB equations with syntax, semantics and implementation.

Lastly, in Section 7.3, we will explain the interplay between the Data Enrichment sub-components in more detail. In summary, however, after cleansing and linking in component (4), we first run the QB equations component (6) once, to compute any values by equations that can be derived from the raw factual data alone, then approximate the remaining missing values by the statistical missing values prediction component (5), after which finally we run the QB equations component (6) again to improve predictions from (5) iteratively. As we will see in a detailed evaluation in Section 7.3, this iterative combination indeed performs better than using either (5) or (6) alone.

5.2.3 Data Publication

Eventually, after the data is crawled and loaded into the triple store, improved and enriched by our workflow, the resulting global cube is available for consumption.

We provide a SPARQL endpoint¹⁸ based on Virtuoso, where the global cube is stored in a named graph.¹⁹ The prefix names used in the examples above are already preset in Virtuoso, thus no prefix declarations are necessary for SPARQL queries.

We also provide a simple user interface to query values for a selected indicator and city in the global cube.²⁰ Queries are directly executed on the triple store during loading of the website using a JavaScript library "Spark"²¹; thus one can have a look at the SPARQL queries in the source code. We show all predicted values for transparency reasons. We simply order by the error value, i.e., the most trustworthy value per year is always shown first.

5.3 Unified View over Statistical Linked Data

As the different data sources use different identifiers (and the wrappers use different IRIS), we need to link the varying IRIS before we can do an integrated querying of the data. As the foundation for efficiently querying Statistical Linked Data—and in turn enriching the data as described in Chapters 6 and 7—we define a unified view of all crawled datasets about cities in a simplified version of the global cube [Kämpgen, Stadtmüller and Harth 2014]. In the following, we describe the structure of the global cube.

We define the unified view as the basis for querying as follows. The qb:Observations (consisting of dimensions and measures) have the following structure, starting with the dimensions: 18 http://citydata.wu.ac.at/ocdp/sparql19 http://citydata.wu.ac.at/qb-materialised-global-cube

20 http://kalmar32.fzi.de/indicatorcity-query.php21 https: //km.aifb.kit.edu/sites/spark/

- For the time dimension we use dcterms:date.
- For the time dimension values we use single years represented as String values such as "2015".
- For the geospatial dimension we use sdmx-dimension:refArea, which is recommended by the QB standard.
- For the geospatial dimension values we use instances of dbr:City, such as dbr:Vienna.
- For the indicator dimension we use cd:hasIndicator.
- For the indicator dimension values we use instances of cd:Indicator, such as cd:population_female. For the indicator dimension values, we defined the CDP ontology as the main hub of indicator IRIS to link to since no list existed with common indicator values.

Most data sources follow the practice of using an unspecific measure dimension sdmx-measure:obsValue and a dimension indicating the measured variable, e.g. estatwrap:indic_na. For the unified view, we thus also assume data cubes to have only one general measure, sdmx-measure:obsValue. Please note that there are different alternative (but equivalent) representations of the same information. Specifically for measure properties, in QB there is a choice for the structuring of the observations. Either use a single observation value property and a dedicated indicator dimension, or encode the indicator in the measure property. To sum up: in-line with established usage, we use a single measure property, but that structure contains all the information that would also be present in the alternative representation.

If we want to pose queries over the two datasets, we have two options. Either specifically write the query to consider possibly different identifiers (i.e., need to know all identifiers) or 2) assume existing links and reasoning. Then, if we query for values for the canonical identifiers (as for any other identifier in the equivalence class), we also get the values for the respective other identifiers. In this chapter, we assume reasoning to allow for flexible addition of new sources without the need to change the queries for each new data source.

As an example, assume we want to query all values of the indicator "population" of the area "Vienna", in the year "2010" over data from both datasets. The indicator would be expressed as a dimension, with a IRI representing "population" as dimension value. The area would be expressed with a dimension, with a IRI representing "Vienna" as dimension value. The query looks like the following:

```
SELECT ?city ?year ?value
WHERE {
?obs cd: hasIndicator cd:population ;
sdmx-dimension:refArea dbr:Vienna ;
dcterms:date ?year ;
sdmx-measure:obsValue ?value .
}
```

Our unified view uses the basic modelling features of the QB vocabulary. In particular, we model indicators in a way that include what otherwise might be encoded as separate dimensions. In the more complex modelling, we would need to use the union of all dimensions of the source datasets, which would lead to introducing an ALL dimension value for those dimensions that are not distinguished by the particular dataset (see [Kämpgen, Stadtmüller and Harth 2014] for details on this more normalised representation). However, all the newly introduced dimensions per dataset would need to be considered in querying which complicates the queries. Rather than adding a dimension sex to encode gender, we create separate indicator IRIS, for example for population, population male and population female. A benefit of the relatively simple structure is that queries and rules operating on the unified view are also simple.

We have published the data structure definition of the global cube using the QB vocabulary. Besides the general measure (sdmx-measure:obsValue), the qb:DataStructureDefinition of the global cube uses the mentioned dimensions dcterms:date, sdmx-dimension:refArea and cd:hasIndicator. Also, we have defined instances of qb:AttributeProperty for cd:estimatedRMSE (for describing the error), cd:preferredObservation (for linking an observation to a more reliable observation), prov:wasGeneratedBy (for describing provenance information) and prov:generatedAtTime (for the time of generation) that help to interpret and evaluate the trustworthiness of values.

Please note that data sources use different identifiers for dimensions and dimension IRIS. In the global cube, we use canonical IRIS to represent resources from different data sources.

IN SUMMARY, we have defined the global cube, from freely available statistical open data sources, which can be queried in subsequent steps. We give detailed description of the first three workflow components, namely (1) Linked Data Wrappers, (2) Crawling and (3) Integration, in Appendix B. Next, we continue with workflow step (6) QB Equations, by applying the foundational ideas of RDF attribute equations to the multidimensional data model introduced in this chapter.

6

QB Equations

The method of RDF attribute equations introduced in Chapter 4 are not directly applicable to data modelled according to a multidimensional database as introduced in Chapter 5 and commonly used for statistical data. With *QB equations*, this chapter transfers the idea of RDF attribute equations to a multidimensional data model and extends the approach with provenance tracking and error propagation. Parts of this chapter have been published as Bischof, Harth et al. [2017].

Section 6.1 gives an detailed introduction into the motivation of QB equations. Section 6.2 introduces the RDF-based syntax for QB equations. Section 6.3 gives a rule-based semantics for QB equations. Section 6.4 describes the implementation of QB equations in the OCDP. Section 6.5 lists relevant related works.

6.1 Introduction

OWL 2 gives only little support for reasoning with literal values. Although knowledge about the relations of different numeric literals (equational knowledge) exists in ontologies, for example the QUDT ontology [Ralph Hodgson 2011], it cannot be used to infer new literal values by an OWL reasoner, since OWL 2 in general cannot compute new (numeric) literals. For statistical data, especially statistical linked data, equational knowledge can be interesting to compute derived indicators or fill in the gaps of missing values. Examples for useful equational knowledge include unit conversion, indicator definitions, or linear regression models. With QB equations (QBE) we introduce a framework to exploit equational knowledge to infer numerical data using Semantic Web technologies, with fine-grained provenance tracking and error propagation for inaccurate values. Both before and after applying the machine learning prediction methods (described in detail in Chapter 7) in the OCDP workflow, the QBEs generate observations from the whole combined dataset. The resulting observations are used for evaluation, consistency checking and are published if they are new or better than any existing observation with the same dimension members.

Example 6.1. The Eurostat indicator "Women per 100 men" is defined as an

equation as follows:

women_per_100_men =
$$\frac{\text{population_female}}{\text{population_male}} \cdot 100$$

The approach of QBEs presented in this chapter is a combination and extension of two earlier approaches "RDF attribute equations" and "complex correspondences". RDF attribute equations (see Chapter 4) use equational knowledge and give an RDF syntax and a Description Logic semantics to derive numerical OWL data properties from other such properties. The approach was implemented in a backward-chaining manner for SPARQL queries. QBES however, operate on QB observations instead of OWL data properties, and are implemented in a forward-chaining manner and provide error propagation and fine-grained provenance tracking. Complex correspondences [Kämpgen, Stadtmüller and Harth 2014] define rules, with numerical functions, to compute QB observations from other QB observations. They transfer the concept of correspondences over relational data to the Semantic Web data model using the QB vocabulary. In contrast to complex correspondences, QBEs are given in an RDF syntax and is more generic since it uses (more general) equations instead of functions resulting in more computed values without the need to (manually) create one rule for each variable in the equation.

6.2 QB Equations RDF Syntax

We express QBEs in an RDF syntax. Since—to the best of our knowledge—no vocabulary exists for this purpose so far, we have to introduce a new vocabulary expressing QBEs and QB rules.

Each QBE is identified by a IRI and consists of two parts: (i) representation of a mathematical equation using (arithmetic) functions and variables and (ii) a mapping of observations to variables using observation specifications. Figure 6.1 gives an overview of the QB equations ontology showing all the introduced classes, properties and datatypes as well as reuse of the QB ontology. When encoded in RDF we call these relationships *QB equations* or *QB rules*. QBEs specify relationships between observations which can be reformulated into different "directions" while QB rules are valid only in one direction.

Representation of the Equation or Function One possibility to represent equations in RDF would be building an operator tree in RDF similar to MathML [Carlisle and Miner 2014], an XML representation of mathematical concepts, including equations. The SWRL RDF syntax also uses such a verbose syntax, for example for predefined mathematical functions.

To keep the representation simple and still human-readable without a custom UI, we define the core of the QBES, which is the equation itself, as a literal that directly reuses SPARQL's arithmetic expression syntax,¹ i.e., we

1 cf. http://www.w3.org/TR/sparql11query/#rNumericExpression

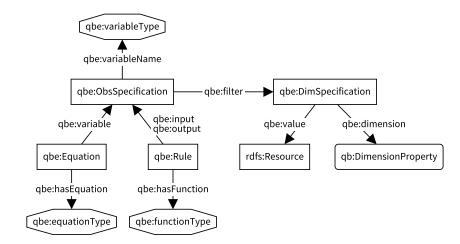


Figure 6.1: QB equations ontology

use a datatype literal with the datatype qbe:equationType, the lexical space of which is defined by the following grammar rule (in the syntax and referring to non-terminal symbols of the SPARQL grammar):

equationType := Var '=' NumericExpression

This choice enables standard SPARQL parsers, or other standard libraries for mathematical expressions, to process these equations and allows straightforward implementations by SPARQL engines. As an example we use the equation for the Eurostat indicator definition of "Women per 100 men":

"?women_per_100_men = ?population_female * 100 / ?population_male"^^qbe:equationType

The property qbe:hasEquation relates an instance of qbe:Equation to such an equation literal. The lexical space of datatype qbe:variableType is—analogous to qbe:equationType—defined by the SPARQL grammar non-terminal 'Var'.

Observation Specification The second part maps observation values to the variables used in the equation. When querying a QB dataset, observations are specified by giving values for all of the dimensions. This approach would be too constraining and might lead to multiple representations of essentially the same equation. Instead, an observation specification only needs values for some of the dimensions. In an example of unit conversions, one would only specify the value of the unit dimension because the equation should be applicable to any kind of observation given in that unit, regardless of the values of the other dimensions. Intuitively the values of all other unspecified dimensions must be the same among all specified observations.

Example 6.2. The following example shows the complete definition of the QBE for the Eurostat indicator "Women per 100 men". The QBE defines a variable ?women_per_100_men which binds to all observations for which the member of the dimension cd:hasIndicator is set to cd:women_per_100_men (see

lines 2–6). The other two variables ?population_male and ?population_female are defined analogously, in lines 7–11 and 12–16. Eventually the QBE represents the equation relating the variables, as a qbe:equationType-typed literal in the last line.

1	ex:women-per-100-men a qbe:Equation ;
2	qbe:variable [a qbe:ObsSpecification ;
3	qbe: filter [a qbe:DimSpecification ;
4	qb:dimension cd:hasIndicator ;
5	<pre>qbe:value cd:women_per_100_men];</pre>
6	qbe:variablename "?women_per_100_men"^^qbe:variableType] ;
7	qbe:variable [a qbe:ObsSpecification ;
8	qbe: filter [a qbe:DimSpecification ;
9	qb:dimension cd:hasIndicator ;
10	<pre>qbe:value cd:population_male] ;</pre>
11	<pre>qbe:variablename "?population_male"^^qbe:variableType] ;</pre>
12	qbe:variable [a qbe:ObsSpecification ;
13	qbe: filter [a qbe:DimSpecification ;
14	qb:dimension cd:hasIndicator ;
15	<pre>qbe:value cd:population_female] ;</pre>
16	<pre>qbe:variablename "?population_female"^^qbe:variableType];</pre>
17	qbe:hasEquation "?women_per_100_men = ?population_female * 100 / ?population_male"^^
	qbe:equationType.

The type declarations are only given for completeness and are not necessary in practice.

QBES can be evaluated in multiple directions, essentially creating a function to compute a value for each of the variables from all the other variables. Using the example above, we could infer new observations for each of the three indicators cd:women_per_100_men, cd:population_female and cd:population_male from the other two. Obviously this works only for invertible functions including the usual arithmetic operators: addition, subtraction, multiplication and division.² In fact, we reuse the definition of *simple equations* in Definition 4.1.

Equations of this form can be easily transformed into an equivalent form $x_i = f'(x_1, \ldots, x_{i-1}, x_{i+1}, \ldots, x_n)$ for each appearing variable $x_i, 2 \le i \le n$. For instance, in our example the equation can likewise be used to compute cd:population_female:

"?women_per_100_men * ?population_male / 100 = ?population_female"^^qbe:equationType

These equivalent transformations can be easily computed by standard mathematical libraries (as already discussed in Section 4.2) which we will use in our implementation, see Section 6.4 below). A central piece of this transformation is a function solve with two parameters: the equation as string and the name of the target variable to solve for. The solve function algebraically solves an equation for a variable and returns a function. For example solve(a = b/c, c) would return the function b/a whereas solve(a = b/c, b) would return a^*c . The function solve is implemented in every computer al-

2 while we have to take care of division by zero, for details cf. Chapter 4 gebra system-for example in Maxima. That is, we could write

~ /

$$f'(x_1, \ldots, x_{i-1}, x_{i+1}, \ldots, x_n) = \text{solve}(x_1 = f(x_2, \ldots, x_n), x_i)$$

Analogously to qbe:equationType, we define a datatype qbe:functionType describing an arithmetic function or expression whose lexical space is again defined via a SPARQL grammar non-terminal rule:

functionType := NumericExpression

Following the example for equationType a *function* for computing "Women per 100 men" is the following:

"population_female * 100 / ?population_male"^^qbe:functionType

QB rules (or functions) are similar to equations but can be evaluated only in one direction. Thus QB rules do not specify generic variables, but one or more input variables and exactly one output variable. These variables are specified in the same way as the variables in QBES, while the output variable does not need a gbe:variableName.

Example 6.3. A QB rule to convert the values for "Women per 100 men" to integer, using the function round to demonstrate a non-invertible function.

```
ex:qbrule1 a qbe:Rule ;
 qbe:input [
   gbe: filter [
     qbe:dimension cd:hasIndicator ;
     gbe:value cd:women_per_100_men];
    qbe:variablename "?women_per_100_men"^^qbe:variableType];
  gbe:output [
   qbe: filter [
     qbe:dimension cd:hasIndicator ;
     qbe:value cd:women_per_100_men_approx]];
  qbe:function "round(?women_per_100_men)"^^qbe:functionType.
```

٥

6.3 Rule-Based Semantics for QB Equations

We define the semantics of QBES by rewriting to a rule language. In fact SPAR-QL INSERT queries can be seen as rules over RDF triple stores where the template of the INSERT clause is the rule head and the graph pattern in the WHERE clause is the rule body. We note that this idea is not new, and implements the same concept as interpreting CONSTRUCT statements as rules. For example, Polleres, Scharffe and Schindlauer [2007] defined a formal semantics for such rules based on the Answer Set Semantics for non-monotonic Datalog programs (ASP) with external (builtin) predicates and aggregates [Eiter et al. 2005]. Builtin predicates are introduced in SPARQL 1.1 through expressions and assignment (BIND AS) and non-monotonicity in SPARQL is introduced by features such as OPTIONAL and NOT EXISTS.

We define the semantics of QBEs in three steps: (i) normalisation of QBEs

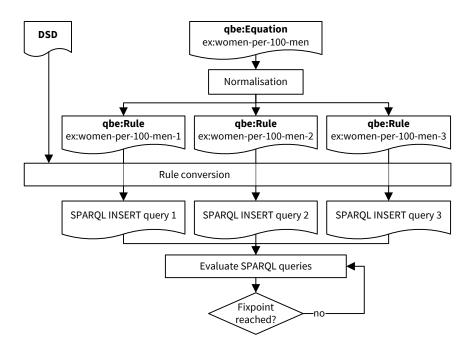


Figure 6.2: QB equation workflow with the example of a Eurostat indicator definition/equation

to QB rules (*n* QB rules generated from a QBE in *N* variables), (ii) conversion of QB rules (generated from QBEs or as input) to SPARQL INSERT queries (iii) a procedure to evaluate a program (a set of SPARQL INSERT queries) until a fixpoint is reached. See Figure 6.2 for an overview of the semantic steps along with the example of the Eurostat indicator "Women per 100 men" in three variables. Note, that in the general case, rules with the expressive power of ASP with external predicates do not have a unique finite fixpoint, but we will define suitable termination conditions.

6.3.1 Normalisation

A QBE in *n* variables can be viewed as a meta rule representing *n* rules: as discussed before, for each variable x_i , we can generate a rule to compute x_i from all the other variables in the equation *e*, by resolving the equation to $x_i = \text{solve}(e, x_i)$. To simplify the semantics specification we thus first normalise each QBE to *n* QB rules and then in the next step give the semantics for QB rules. That is, the QB rules generated in the normalisation, have x_i as the output variable, and the other (n - 1) variables as input variables with $f'(x_1, \ldots, x_{i-1}, x_{i+1}, \ldots, x_n)$ being the function to compute the output.

Algorithm 6.1 shows the main algorithm of the conversion. The function r in Algorithm 6.2 takes three parameters: the original QBE IRI, the name of the output variable and the function. The function sk(...), with a variable number of parameters is a Skolem function deterministically returning a unique IRI for each unique parameter combination.

```
Algorithm 6.1: qbr(G)
```

Input: RDF graph *G* containing QBES Output: RDF graph containing QB rules for all equations $R := \emptyset$ foreach (?e, ?eq) *in* [[?e rdf:type qbe:Equation; qbe:hasEquation ?eq]]_G do foreach (?v, ?vname) *in* [[?e qbe:variable ?v.?v qbe:variableName ?vname]]_G do f := solve(?eq, ?vname) $R := R \cup r(?e, ?vname, f)$ return *R*

```
Algorithm 6.2: r(G, e, o, f)
```

Input: RDF graph *G*, QBE IRI *e*, variable name *v*, function string *f* **Output:** RDF graph of one QB rule n := sk(e, v) $R := \{n \text{ rdf:type qbe:Rule; qbe:hasFunction } f; \text{prov:wasDerivedFrom } e; \text{qbe:output } o.\}$ **foreach** (?v, ?vname) *in* [[*e* qbe:variable ?v . ?v qbe:variableName ?vname]]_{*G*} **do** | **if** ?vname $\neq o$ **then** | $R := R \cup \{n \text{ qbe:input ?v}\}$ **return** *R*

Eventually, after applying Algorithm 6.1, we could replace all QBEs in an RDF graph with the generated QB rules, i.e. these two representations are equivalent. The remainder of our semantics only deals with rules.

Example 6.4. After normalisation, the QBE of Example 6.2 results in three QB rules, one for each of the three variables. The QB rule to compute the Eurostat "Women per 100 men" indicator is given below. Instead of variables we now have input and output and the equation was replaced by a function in the input variables.

```
ex:women-per-100-men-w a qbe:Rule;
  prov:wasDerivedFrom ex:women-per-100-men;
  gbe:input [
   gbe: filter [
     qb:dimension cd:hasIndicator ;
     gbe:value cd:population_male];
   gbe:variablename "?population_male"^^gbe:variableType];
  gbe:input [
   qbe: filter [
     gb:dimension cd:hasIndicator ;
     qbe:value cd:population_female];
   qbe:variablename "?population_female"^^qbe:variableType ] ;
  qbe:output [
   qbe: filter [
     qb:dimension cd:hasIndicator ;
     qbe:value cd:women_per_100_men]];
  qbe:hasFunction "?population_female * 100 / ?population_male"^^qbe:functionType.
```

For each of the other two indicators cd:population_female and cd:popula-

102

6.3.2 Rule Conversion

In this step QB rules are converted to SPARQL INSERT queries. The resulting query has to implement several tasks: retrieve the input observations, compute the output observations, generate several IRIS, perform error propagation and provenance tracking and ensure termination when evaluated repeatedly.

Compared to other rule languages, SPARQL queries provide more complex features, but, as shown earlier by Polleres and Wallner [2013] and Angles and Gutierrez [2008], can be compiled to—essentially—non-recursive Datalog with negation, wherefore INSERT queries, read as rules, have the same expressivity.

Without loss of generality, we repeat two assumptions we made in Chapter 5—which could be easily checked in a pre-processing step:

- there is always only a single measure per observation
- the measure predicate that holds the measure value is fixed to sdmx-measure:obsValue

On a high level, the INSERT queries corresponding to QB rules have the following structure:

INSERT { output observation template - with PROV annotations to describe the generation by \qbe rules - error estimation }
WHERE {
one pattern for each input observation
 – with all dimensions as specified in the DSD and error estimate
BIND patterns for IRI creation for — the newly generated observation — the prov: Activity
BIND patterns to – assign current time to variable for PROV annotation – compute measure value of target observation – estimate error of target observation
Termination condition }

We now explain the different parts of this SPARQL query in detail.

Output Observation The output observation is set in the head with the fixed dimensions from the DSD and fixed dimension values if specified in the observation specification of the QB rule. The other dimension values are taken from the input variables. The rule head for Example 6.4 would look like the following query fragment, incorporating the PROV annotations:

?obs qb:dataSet globalcube:global-cube-ds; cd:hasIndicator cd:women_per_100_men; dcterms:date ?year ; sdmx-dimension:refArea ?city ; sdmx-measure:obsValue ?value ; prov:wasDerivedFrom ?population_male_obs, ?population_female_obs ; prov:wasGeneratedBy ?activity ; prov:generatedAtTime ?now ; cd:estimatedRMSE ?error .

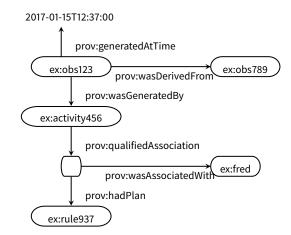
It is important to note that the SPARQL INSERT application is *idempotent*, i.e., repeated applications of a generated SPARQL INSERT query will not add any more triples after the first application. Idempotence would be lost if blank nodes are used in the head, because they would create a fresh blank node for every application of a SPARQL query, even if the SPARQL query returns only a single result. Furthermore, we have to ensure that all values generated by the query are completely determined by the variable bindings of the WHERE clause.

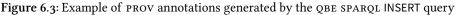
Input Observations For each input observation one set of triple patterns which asks for one observation is generated for the SPARQL WHERE clause. For each qbe:DimSpecification a dimension value is fixed. For all the other dimensions a fixed variable is used in all input observations. In the example below, again generated from Example 6.4 the query contains for all dimension value variables, except for cd:hasIndicator which is fixed to cd:population_male and cd:population_female as specified by the QB rule input dimension specification. Furthermore, the observation value and the estimated error are retrieved.

```
?population_male_obs qb:dataSet globalcube:global-cube-ds;
cd:hasIndicator cd:population_male;
dcterms:date ?year;
sdmx-dimension:refArea ?city ;
sdmx-measure:obsValue ?population_male;
cd:estimatedRMSE ?population_male_error.
```

?population_female_obs qb:dataSet globalcube:global-cube-ds; cd:hasIndicator cd:population_female; dcterms:date ?year; sdmx-dimension:refArea ?city; sdmx-measure:obsValue ?population_female; cd:estimatedRMSE ?population_female_error.

Provenance Propagation For every new derived observation we record the provenance, i.e., each derived observation has a link to each input observation ?obsin₁, ..., ?obsin_N and to the rule or equation used for the computation ?equation. Firstly, this provenance information provides transparency: we know precisely how a derived observation was computed. Secondly, we use the provenance information during the derivation process to ensure termination. Furthermore, we record the time of the rule application and the





agent, which could be the script or person responsible for the query creation.

Figure 6.3 gives an example of a part of the derivation tree generated by this rule head fragment.

Value Creation with BIND Several SPARQL variables used for the output observation need to be computed using variables from the input observations. Most importantly, the output measure value has to be created using the function of the QB rule.

BIND(100.0*?population_female/?population_male AS ?value)

Several URIs have to be generated for the rule head. We use a Skolem function to generate these URIs. The inputs of this Skolem function are the IRI of the QB rule rule, the input variables var1, ... varN and a string "_static_" to differentiate the different variables in the head. We implement this Skolem function with string concatenation and a hash function.

```
BIND(IRI(CONCAT(STR(rule), MD5(CONCAT(STR(?var1), ..., STR(?varN))))) AS ?targetvar)
```

We have to generate two URIs: observation and PROV activity.

BIND(CONCAT("http://citydata.wu.ac.at/ocdp/eurostat-rules#", MD5(CONCAT("http://citydata. wu.ac.at/ocdp/eurostat-rules#28f3",STR(?population_male_obs),STR(? population_female_obs))))) AS ?skolem) BIND(IRI (CONCAT(?skolem, "_obs")) AS ?obs) BIND(IRI (CONCAT(?skolem, "_activity")) AS ? activity)

Furthermore we bind the current time to a variable to use in the provenance part of the head: BIND(NOW() as ?now). *Error Propagation* When a target value is computed based on values with an associated error, we also need an error estimate for the target value. The procedure to estimate an error for the new value is called *error propagatione* [Bevington and Robinson 2003; Ku 1966]. In our use case we do not promise precise statistical error quantifications, but just want to propagate an upper bound of the error estimations of the inputs to the computed output value. We chose a error propagation function which is simple to implement in standard sparqu. Other standard error propagation procedures, such as the ones proposed by Bevington and Robinson [2003] and Ku [1966], require the computation of square roots, which is not possible with standard sparqu. To this end, we incorporate a relatively naive error propagation function which can be adapted to more accurate estimations if necessary in the future. Most of the standard error propagation methods, as for example presented by Bevington and Robinson [2003] and Ku [1966], require the computation of square roots. Nuclease are estimations if necessary in the future. Most of the standard error propagation methods, as for example presented by Bevington and Robinson [2003] and Ku [1966], require the computation of square roots. Nuclease are estimations if necessary in the future. Most of the standard error propagation methods, as for example presented by Bevington and Robinson [2003] and Ku [1966], require the computation of square roots, which sparqu 1.1 does not support.³

The error values attached to the observations, for example from our predictions in the next chapter, intuitively characterise how far off, in absolute numbers, the actual value is on average, from our prediction. To compute a conservative estimate of how these errors "add up" when used in computations, we proceed as follows. Depending on the function f used for computing the output value, the n input variables x_1, \ldots, x_n and their associated indicators i_1, \ldots, i_n , we denote by e_1, \ldots, e_n the errors for these indicators. In Table 6.1 we define the propagated error (pe) of a computed observation, recursively over the operator tree of the function term $expr = f(x_1, \ldots, x_n)$. Intuitively, we assume here the following: if the real value x'_i for the indicator i_i lie e_i away—i.e., the estimated error above $(x'_i = x_i + e_i)$ or below $(x'_i = x_i - e_i)$ — from the predicted value x_i , we intend to estimate how much off would a value computed from these predicted values *maximally* be; here, *const* denotes a constant value and a, b are sub-expressions. Furthermore we assume that the error e_i is always less than the observed value x_i .

If now, for an equation $x_f = f(x_1, ..., x_n)$, the propagated estimated error $pe(f(x_1, ..., x_n))$ is smaller than the so far estimated error e_f for indicator i_f then we assume it potentially pays off to replace the predicted value so far with the newly computed value by the rule corresponding to the equation.

To cater for rounding errors during the computation we add a small ϵ of

Table 6.1: Computing the propagated error (pe) for a given expression (*expr*)

expr	pe(<i>expr</i>)
const	0
x_i	r _i
a + b	pe(a) + pe(b)
a - b	pe(a) + pe(b)
a/b	(a + pe(a))/(b - pe(b)) - a/b
a * b	(a + pe(a)) * (b + pe(b)) - a * b

3 To remain compatible with the SPARQL 1.1 specification, we avoid using implementation-specific extension functions, which might implement the square root function.

0.0001 to the error estimate. Additionally, this ϵ punishes each rule application and thus enables quicker termination later. Eventually, the following BIND expression will be generated to compute the propagated error as defined by pe and assign it to the corresponding variable used in the head of the rule.

BIND((ABS(100.0)+0.0)*(ABS(?population_female)+?population_female_error)*1.0/ (ABS(? population_male)-?population_male_error)-100.0*?population_female*1.0/? population_male + 0.0001 as ?error)

Termination So far we introduced triple patterns and BIND expressions into the rule body. As remarked above, the BIND expressions implement Skolem functions and thus avoid duplicating the same output observations over and over again, i.e., the generated SPARQL INSERT queries are *idempotent*. We now give two different termination conditions to ensure termination of the QB rules program.

To ensure termination of the whole SPARQL INSERT rule program, we use a similar termination condition as defined in Chapter 4: we block the repeated application of the same rule to derive a particular observation. With the PROV annotations, in fact, we create an equation-observation dependency graph. Given an observation o, a SPARQL path pattern o prov:wasDerivedFrom⁺ o' returns all the observations o' transitively used in the computation of o. Furthermore, the SPARQL path pattern o prov:wasDerivedFrom^{*} / prov:wasGeneratedBy/ prov:qualifiedAssociation / prov:hadPlan r gives all the rules r which were transitively used during the computation of o. So, in order to ensure termination, we define that a QB rule r is only *applicable* to materialise an observation o if r does not occur in the result of that path expression.

In the SPARQL INSERT query we can implement this condition by adding one of the following patterns for each input observation ?i to the WHERE clause, where r is the IRI of the rule (or equation) itself.

?i prov:wasDerivedFrom*/prov:wasGeneratedBy/prov:qualifiedAssociation/prov:hadPlan/prov: wasDerivedFrom?r}

In the worst case, the evaluation will be terminated by this condition after applying each rule *n* times, where *n* is the number of QB rules in the system, because after applying each rule once for the derivation of a single observation, no rule can be applicable anymore. An example of this worst case would be a chain of QB rules where $e_i = e_{i+1}$ and 0 < i < n and a single given observation for e_0 .

Another termination condition is based on the error propagation function. Intuitively, the condition ensures that an observation o from a computation is only materialised if no observation o' exists that (i) shares the same dimension values and (ii) has a lower or comparably low error estimate.⁴

sumx-unnension.reiArea ?city

4 That is, we add a *confidence threshold* that can be adapted, based on the confidence in the respective error propagation function, in order to only materialise new computed observations if we expect a *significant* improvement

FILTER NOT EXISTS {

[?]obsa qb:dataSet globalcube:global-cube-ds; dcterms:date ?year; sdmx-dimension:refArea ?city ;

cd: hasIndicator cd:women_per_100_men; sdmx-dimension:sex ?sex ; estatwrap:unit ?unit ; sdmx-dimension:age ?age ; cd:estimatedRMSE ?errora .

FILTER(?errora <= ?error * CT)

Here, the constant factor CT is a value greater than or equal to 1, that determines a *confidence threshold* of how much improvement with respect to the estimated error is required to confidently "fire" the computation of a new observation. Thus, we materialise only observations that we expect to be significantly (i.e., by a factor of CT) better with respect to error estimates. Since for any reasonable error propagation function the error estimates tend to increase with each rule application, consequently, together the two termination conditions can lead to faster termination.

For our naive error propagation function, CT = 30.0 turned out to be a reasonable choice, cf. the evaluation results in Section 7.3. Choosing CT = 1 would require an error propagation function with very high confidence, i.e., that never estimates a too low error, which we cannot guarantee for our naive estimation function.⁵

WE NOTE HERE that we really need *both* termination conditions, since relying on error estimates alone would need to ensure that the error propagation "converges" in the sense that application of rules does not decrease error rates. Our simple method for error propagation – in connection with *cyclic* rule application—does not guarantee this as demonstrated by the following, simple example:

Example 6.5. For two indicators *i* and *j* let two equations be i = j/2 and j = i/2. Essentially, this boils down to the (cyclic) equation i = i/4 where—in each application—we would derive smaller error estimates.

While this example is quite obviously incoherent—in the sense of rules being cyclic in terms of the rule dependency graph defined in Definition 4.10, we still see that with cyclic application of rules the convergence of error rates cannot be ensured in general. In practice such incoherent systems of equations are hardly useful, however the first termination condition would still serve its purpose of ensuring termination.

Example 6.6. Taking the observations in rows 1 and 2 of Table 6.2 we can compute the "No. of bed-places in tourist accommodation establishments" for Bolzano 2010 as 2 434.5 with an RMSE (computed with the propagated error function pe) of 56.6 (row 3). The QBE observation of row 3 is classified as "better" than the best predicted observation (row 4) because of the RMSE comparison with respect to the confidence threshold: $56.6 \cdot 30 < 3228.8$.

Similarly, the observations from row 5 and 6 are used by the QB equation

5 Note that this has also been the reason why we introduced the factor CT, as the earlier simpler condition FILTER(?errora <= ?error) produced too many over-optimistic—and in fact worse—observations. 108

Source	Indicator	Value	Error
Crawl (UN)	Population	103 582.0	0.0
Prediction	No. of available beds per 100 residents	23.5	0.55
QBE	No. of bed-places in tourist accomm. est.	2 434.5	56.6
Prediction	No. of bed-places in tourist accomm. est.	1 490.5	3 228.8
Crawl (UN)	Population male	49 570.0	0.0
Prediction	Population female	54 836.2	7 044.0
QBE	Women per 100 men	110.6	14.3
Crawl	Women per 100 men	109.0	0.0

 Table 6.2: Example data for Bolzano in the year 2010

of the running example to compute the observation in row 7. Since there already exists an observation from the crawl with a better RMSE (row 8), the computed QBE observation will be ignored in this case.

6.4 Implementation of QB Equations in the OCDP

As described in Section 6.3, we compile QBES into a semantically equivalent set of rules. Usually there are two strategies for query answering in rule based knowledge bases: forward or backward chaining. For the OCDP we decided to implement a forward-chaining approach to enrich the global data cube with the newly inferred observations. Forward-chaining approaches materialise as much as possible, thus allowing faster query evaluation times. On the other hand, forward-chaining approaches require more memory or disk space and updates lead to re-materialisation. For the OCDP the space requirements are manageable and updates are infrequent.

Our forward-chaining implementation approach relies on the iterative application of SPARQL INSERT queries (which implement the rules). Overall, QBEs infer and persist new observations in three steps: (Normalisation) convert all QBEs to QB rules, (Rule conversion) for each QB rule we create a SPAR-QL query and (Query evaluation) iteratively evaluate the constructed SPARQL INSERT queries until a fixpoint is reached (that is, no better observations can be derived).

Normalisation As described in the semantics definition above, in this first step we convert QBES to QB rules. The algorithm in Algorithm 6.1 already outlines our implementation. We implemented the algorithm using Python 2.7 and the libraries rdflib for RDF/SPARQL processing and sympy providing the solve function to algebraically solve an equation for a variable. The Python script reads the QBEs from an RDF file containing the QBEs,⁶ converts them to QB rules and publishes them again as Linked Data⁷ and in the triple store. This normalisation step could also be implemented by standard RDF-to-RDF tools such as XSPARQL [Bischof, Decker et al. 2012].

6 http://citydata.wu.ac.at/ocdp/ eurostat-equations.rdf 7 http://citydata.wu.ac.at/ocdp/ eurostat-rules.rdf *Creating SPARQL Queries* We create one SPARQL INSERT query for each QB rule. The listing in Appendix C gives a complete example of the SPARQL INSERT query resulting from converting one of the QB rules. Due to a serious performance problem with SPARQL INSERT queries applied on the Virtuoso triple store in a preliminary evaluation, we used SPARQL CONSTRUCT queries instead, and load the resulting triples into the triple store afterwards. The conversion from QB rules to SPARQL CONSTRUCT queries is analogous to the algorithm described in Section 6.3.2 above to convert a QB rule to a SPARQL INSERT query.

Evaluating Queries in Rule Engines In principle the rule engine naively evaluates SPARQL INSERT queries, or respectively, CONSTRUCT queries + re-loads, over and over again until a fixpoint is reached. A fixpoint is reached when the complete set of SPARQL INSERT queries is evaluated, and no new triple was added.

Apart from the termination conditions described in Section 6.3.2 we ensure that the repeated application of a rule on the same observations does not create any new triples by using Skolem constants instead of blank nodes (see also discussion on idempotency above). Thus, in order to check whether a fixpoint has been reached, it is enough to check in each iteration simply if the overall number of triples has changed or not. So, for a naive implementation we could simply use a SPARQL query to count the number of triples and compare it to the previous iteration.

Unfortunately, in our experiments, such a simple implementation solely based on "onboard" means of the SPARQL engines turned out to be infeasible due to performance reasons. Thus, for the time being, we resorted to just evaluating one iteration of all generated rules, in order to evaluate our conjecture that rules improve our prediction results.

Eventually, we may need to resort to (offline) using a native rule engine. Indeed, in practical applications, such rule/Datalog engines have shown to perform better than recursive views implemented directly on top of databases, for instance for computing RDFs closure, cf. Ianni et al. [2009]. We leave this to future work and resort, as mentioned, to a fixed number of iterations of rule applications. We postpone the practical evaluation of QBEs to Section 7.3, as part of the evaluation of the combined enrichment workflow.

6.5 Related Work

Modelling the actual numerical data and the structure of that data captures only a part of the knowledge around statistical data that can be represented in a machine-interpretable manner. Equations in particular are a rich source of knowledge in statistical data. Lange [2013] gives an extensive overview of representations of mathematical knowledge for the Semantic Web. We first 110

cover representation of equations for layout purposes, and then cover representations that permit the interpretation of the formulas by machines.

Representations of mathematical knowledge not based on RDF, including MathML [Carlisle and Miner 2014] and OpenMath [Buswell et al. 2004], use XML for serialisation, focus more on a semantic representation of mathematical entities and are not directly useful for reasoning. Although Geo-SPARQL [Perry and Herring 2012] uses MathML in XMLLiterals (a method to embed XML content into RDF graphs not used in this thesis) and OpenMath provides preliminary integration into RDF,⁸ these representations are hard to reuse for RDF tools and still are not suitable for an RDF QB setup.

The OWL ontologies QUDT [Ralph Hodgson 2011], OM [Rijgersberg, Assem and Top 2013] and SWEET [Raskin and M. J. Pan 2005] provide means to describe units and to some extent model conversion between these units, but do not specify a concrete machinery to perform these conversions. Our approach is orthogonal to these efforts in that it provides not only a modelling tool for unit conversions, but more general equations and also gives a semantics to automatically infer new values.

Semantic Web rule languages and systems often implement numerical functions—for example RIF uses numerical functions from XPath [Kay et al. 2010]. Other examples for rule languages and systems include swRL and Apache Jena rules. Converting equations to rules naively can lead to a set of recursive rules which often lead to non-termination even for one equation alone (cf. Chapter 4).

To add reasoning over numbers, Description Logics were extended with *concrete domains* (cf. Baader, Calvanese et al. [2007]). A concrete domain is a domain separate from the usual instance domain of the model based semantics. Examples for concrete domains include different sets of numbers or strings. A specific concrete domain extension defines predicates over the concrete domain, e.g., *greater than* for numbers, or *substring* for strings. Often, a limited set of functions (for computation) can be supplied. Racer [Haarslev and Möller 2001] implements concrete domains for numbers. But computed values are only used for reasoning tasks such as checking satisfiability or classification, but not available for instance retrieval or query evaluation. owL Equations [Parsia and Uli Sattler 2012], a concrete domain extension carried over to OWL, allows comparing numerical values—even computed values; however, the same limitations apply.

In general, frameworks using SPARQL as a rule language could also be used to straightforwardly implement QBES. Prominent examples are the SPAR-QL Inferencing Notation [Knublauch, J. A. Hendler and Idehen 2011] and, more recently, the (preliminary) advanced features of the Shapes Constraint Language (SHACL) [Knublauch, Allemang and Steyskal 2017]. The conversion from the equational knowledge, given as QBES, to SPARQL 1.1 queries is needed nonetheless.

8 http://www.openmath.org/cd/ contrib/cd/rdf.xhtml IN SUMMARY, QBES define an RDF syntax to represent declarative equational knowledge together with a rule-based semantics to compute new numerical values for multidimensional RDF datasets.

7

Equations and Statistical Methods Combined

With QB equations, as introduced in Chapter 6, we now have the necessary means to exploit equational knowledge to compute missing values based on the data presented in Chapter 5. However, QBEs depend on this equational knowledge and cannot detect hidden patterns in large datasets. In this chapter we now combine QBEs with statistical methods to produce more and higher quality data. Parts of this chapter have been published as Bischof, Harth et al. [2017] and Bischof, Martin et al. [2015a].

Section 7.1 reiterates and details the workflow components for enrichment of our use case in Chapter 5. Section 7.2 explains the missing data prediction process in more detail. Section 7.3 evaluates both the basic value imputation mechanism and the combination with QBEs and details our experience with the OCDP. Section 7.4 puts our approach in the context of related work.

7.1 Introduction

In this section we detail the workflow as introduced in Section 5.2.2. The workflow combines the QB equations specified in the last chapter, with statistical methods, and proceeds in three steps as follows:

1. *Materialisation of observations by application of* QBES *on the raw data*: in a first step we load the integrated and linked observations from the data integration step (4). Note here that each observation, in order to be considered in our rules, needs an cd:estimatedRMSE, which per default is set to 0 for factual observations. However, due to the linking of different data sources, we could potentially have several ambiguous observations for the same city, year and indicator in this raw data already, e.g. two or more different population values from different data wrappers materialised in the global cube. Let us say, we have for city C1 in the year 2017 three different population values in three different factual observations from UNdata, Eurostat and DBPEDIA, 1000 000, 980 000, an 1020 000 respectively. In principle, we take no preference among sources, so we proceed as follows in a preprocessing step: for such case we set the cd:estimatedRMSE to the difference from the average of all available ambiguous values (for the same

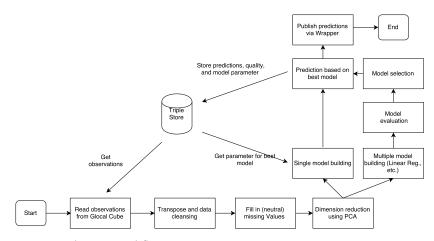


Figure 7.1: Prediction Workflow

indicator and city/year pair). That is, we set:

```
: obsUN estimatedRMSE 0.0 .
: obsEurostat estimatedRMSE 20000.0 .
: obsDbpedia estimatedRMSE 20000.0 .
```

After this preprocessing, we apply a first application of QB equations, in which case—obviously—the value from the UNdata observation would be preferred for any equation having cd:population as input indicator.

- 2. *Materialisation of observations by* statistical missing-value prediction: as a second step, we apply enrichment by *statistical regression methods* and computation of estimated RMSES per indicator as described in Section 7.2; these statistical regression methods can potentially benefit from derived additional factual knowledge from the prior step.
- 3. *Materialisation of further observations by re-application of QBES*: finally, using these predictions, we iteratively re-apply QBES wherever we expect (through error propagation) an improvement over the current RMSE by using computed values rather than statistical predictions only.

We remark that one could alternatively re-iterate steps 3. and 2. as well, i.e., by re-computing statistical models from step 2. based on the application of equations in step 3. again, and so on. However, for instance due to imprecise-ness of error estimations alone, this would be extremely prone to overfitting and—as expected—showed a quality decrease than improvement in some pre-liminary experiments we ran.

7.2 Imputation: Predicting Missing Values

As discussed in Sections 5.1 and 5.2.1, the filling in of missing values by reasonable predictions is a central requirement for the OCDP, since we discovered a large number of missing values in our datasets (see Tables 5.1 and 5.2).

The prediction workflow is given in Figure 7.1. The initial step performs

the loading, transposing and cleansing of the observations taken from the global cube. Then, for each indicator, we impute all the missing values with neutral values for the principal components analysis (PCA), and perform the PCA on the new matrix, which creates the principal components (PC) that are used as predictors. Next, the predictors are used for the model building step using a basket of statistical Machine learning methods such as multiple linear regression. Finally, we use the best model from the basket to fill in all missing values in the original matrix and publish them using the Missing Values wrapper.

In our earlier work [Bischof, Martin et al. 2015a], we evaluated two approaches to choose the predictors, one based on applying the base methods to complete subsets in the data and the other based on PCA. We only use the PCA-based approach, since, although it delivers slightly lower prediction accuracy, it allows us to cope more robustly with the partially very sparse data, such that we can also predict values for indicators that do not provide sufficiently large subsets of complete, reliable predictors.

7.2.1 Base Methods

Our assumption is that every indicator has its own statistical distribution (e.g., normal, exponential, or Poisson distribution), sparsity, and relationship to other indicators. Hence, we aim to evaluate different regression methods and choose the best fitting method to predict the missing values per indicator. In order to find this best fitting method, we measure the prediction accuracy by comparing the *root mean-square error* [Witten and Frank 2011] and the *normalised root mean-squared error* (NRMSE) of every tested regression method. For the predicted values $\vec{p} = (p_1, \dots, p_n)$ and the actual values $\vec{a} = (a_1, \dots, a_n)$, we define the two error measures as follows:

$$\operatorname{rmse}(\vec{a}, \vec{p}) \coloneqq \sqrt{\frac{\sum_{i=1}^{n} (p_i - a_i)^2}{n}}$$
$$\operatorname{nrmse}(\vec{a}, \vec{p}) \coloneqq \frac{\operatorname{rmse}(\vec{a}, \vec{p})}{\max(\vec{a}) - \min(\vec{a})}$$

While the RMSE gives us an error estimate in the same unit as the values and gives a better intuition of the error estimate of an indicator, the NRMSE allows us to compare models for different indicators.

While in the field of Data Mining (DM) [Hastie, Tibshirani and Friedman 2009; Witten and Frank 2011; Han 2012] numerous regression methods for missing value prediction were developed, we chose the following three standard methods for our evaluation due to their robustness and general performance:

K-Nearest-Neighbour Regression (KNN) is a wide-spread DM technique based on using a distance function to a vector of predictors to determine the target values from the training instance space. As stated in Han [2012], the algorithm is simple, easily understandable and reasonably scalable. KNN can be used in variants for clustering as well as regression.

Multiple Linear Regression (MLR) is a standard method to find a linear relationship between a target and several predictor variables. The linear relationship can be expressed as a regression line through the data points. The most common approach is *ordinary least squares* to measure and minimise the cumulated distances [Han 2012].

Random Forest Decision Trees (RFD) involve the top-down segmentation of the data into multiple smaller regions represented by a tree with decision and leaf nodes. Each segmentation is based on splitting rules, which are tested on a predictor. Decision nodes have branches for each value of the tested attribute and leaf nodes represent a decision on the numerical target. A random forest is generated by a large number of trees, which are built according to a random selection of attributes at each node. We use the algorithm introduced by Breiman [Breiman 2001].

7.2.2 Principal Component Analysis

All three of base methods need a complete data matrix as a basis for calculating predictions for the respective target indicator column. Hence, we need for each target indicator (to be predicted) a complete training data subset of predictor indicators. However, as discussed by Bischof, Martin et al. [2015a], when dealing with very sparse data, such complete subsets are very small and would allow us to predict missing values only for a small number of indicators and cities. Instead, we use the *regularised iterative PCA algorithm* [Roweis 1997] which works also on incomplete datasets. It uses an iterative approach where missing values are replaced by neutral values, with respect to the PCA. In general the PCA is a dimensionality reduction technique which reduces a high-dimensional input dataset (in our case the dimensions correspond to the indicators) to a sorted list of *principal components* [Han 2012] (PCs) which are subsequently used as predictors for the three base methods.

Before we can apply the PCA and subsequently the base regression methods we need to pre-process and prepare the data from the global cube to bring it into the form of a two-dimensional data matrix.

7.2.3 Preprocessing

Preprocessing starts with the extraction of the observations from the global cube. Since the described standard DM methods cannot deal with the hier-archical, multi-dimensional data of the global cube, we need to "flatten" the data. For this, we pose the following SPARQL query, with an increasing year range that is currently *2004–2017*.

```
SELECT ?city ?indicator ?year ?value
WHERE {
?obs dcterms:date ?year.
?obs sdmx-dimension:refArea ?city.
?obs cd: hasIndicator ?indicator .
?obs sdmx-measure:obsValue ?value.
FILTER(xsd: integer (?year) >= 2004)
}
```

The query flattens the multidimensional data to an input data table with tuples of the form: (*City, Indicator, Year, Value*). Based on the initial table, we perform a simple preprocessing as follows:

- Removing non-numerical columns and encode boolean values;
- Merging the dimensions year and city to one dimension, resulting in tuples of the form (*CityYear*, *Indicator*, *Value*) that is, we further flatten the dataset
- Finally, we unfold the indicator and value dimension to a two-dimensional data matrix with one row per city/year-pair and one column per indicator, resulting in tuples of the form (*CityYear*, *Value*₁, ..., *Value*_n) for the list of indicators (*Indicator*₁, ..., *Indicator*_n)
- From this large matrix, we delete columns (indicators) and rows (city/years) which have a missing values ratio larger than 99%, that is, we remove city-year pairs or indicators that have too many missing values to make reasonable predictions, even when using PCA.

Our initial dataset from merging Eurostat and UNSD contains 1961 cities with 875 indicators. By merging city and year and transposing the matrix we create 12 008 city/year rows. After deleting the cities/year-pairs and indicators with a missing values ratio larger than 99%, we have the final matrix of 6 298 rows (city/year) with 212 columns (indicators).

Note that the flattening approach and deletion of too sparse rows and columns are generic and could obviously still be applied if we added more data sources, but our experiments herein focus on the Eurostat and UNSD data.

7.2.4 Prediction using PCA and the Base Regression Methods

Next, we are ready to perform PCA on the data matrix created in the previous subsection. That is, we *impute* all the missing values with *neutral* values for the PCA, according to the *regularised iterative PCA algorithm* described in [Roweis 1997]. In more detail, the following steps are evaluated having an initial dataset A_1 as a matrix and a predefined number of predictors n (we test this approach also on different n's):

- 1. Select the target indicator I_T ;
- 2. Impute the missing values in A_1 using the regularised iterative PCA algorithm resulting in matrix A_2 and remove the column with I_T ;

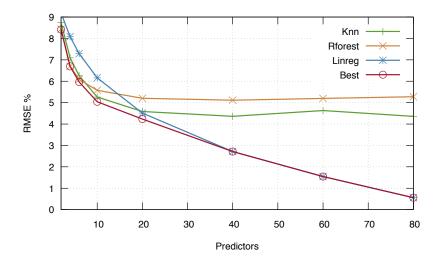


Figure 7.2: Prediction results using PCA

- 3. Perform the PCA on the A₂ resulting in a matrix A₃ of a maximum of 80 PCs;
- 4. Append the column of I_T to A_3 creating A_4 and calculate the correlation matrix A_C of A_4 between I_T and the PCs;
- 5. Create the submatrix A_5 of A_4 on the selection of the PCs with the highest absolute correlation coefficients and limit them by n;
- Create submatrix A₆ of A₅ for validation by deleting rows with miss. values for I_T;
- 7. Apply stratified tenfold cross-validation on A_6 . which results in the best performing model M_{Best} ;
- 8. Use the method for M_{Best} to build a new model on A_5 (not A_6) for predicting the missing values of I_T .

7.2.5 Evaluation and Publishing

Figure 7.2 shows the results for the median NRMSE with an increasing number of predictors (selected from the 80 PCs) and compares the performance of KNN, RFD, MLR and the selection of the best method. Clearly, for 80 predictors MLR performs best with a median NRMSE of 0.56%, where KNN (resp. RFD) has a median NRMSE of 4.36% (resp. 5.27%). MLR is the only method that improves steady up to 80 predictors. KNN provides good results for a lower number of predictors, but starts flattening with 20 predictors. Contrary to MLR, the parameter of KNN and MLR have to be adjusted according to number of predictors, hence optimising the number of clusters for KNN could improve the result. The red line in Figure 7.2 shows the median NRMSE with the best regression method chosen. Up to 60 predictors, the overall results improves by selecting the best performing method (for each indicator). The best median NRMSE of 0.55% is reached with 80 predictors, where MLR is predominant and only 5 out of 232 indicators are predicted by KNN. We emphasise that, compared to the result of our earlier experiments in [Bischof, Martin et al. 2015a], the median NRMSE improved from 1.36% to 0.55%, which is mainly related to the lower sparsity of the datasets.

Finally, we note again why we added PCA, as opposed to attempting predictions based on complete subsets: in our preliminary evaluations, based on the comparison of the two approaches in [Bischof, Martin et al. 2015a], by picking the best performing regression method per indicator with ten predictors from the raw data based on complete subsets the median NRMSE was 0.25%. However, due to the low occurrence of complete subsets of reasonable size for ten predictors, only one third of the missing values could be imputed compared to using PCA. We acknowledge that this comes at a cost, as the median NRMSE goes up to 0.55% with 80 predictors, when using PCA. However, due to the sparsity in the data we decided to trade better completeness for accuracy of the prediction.

We publish the predicted values created by the combination of PCA and selecting the best regression method per indicator, where we apply a threshold of NRMSE of 20% as a cut off. This leads to no removal of any indicator in our evaluation. Following our strategy of using statistical linked data wrappers, we publish the predicted values using the *Missing Values wrapper*,¹ which provides a table of content, a structure definition and datasets that are created for each prediction execution.

7.2.6 Workflow and Provenance

The full prediction workflow of our statistical prediction for missing values is shown in Figure 7.1. The *data preprocessing and transposing* for the input data matrix is written in Python, but all other steps such as *PCA*, *model building*, and *model evaluation* are developed in R [R Core Team 2017] using its readily available "standard" packages (another advantage of relying on standard regression methods). All the scripts and their description are available on the website of the *Missing Values wrapper*. We conducted an evaluation of the execution time on our Ubuntu Linux server with 2 cores, 2.6 GHz and 16 GB of main memory. A single prediction run requires approximately 10 min for each indicator (approximately 3 min. for each method) resulting in a total time of about 35 hours for all indicators.

Looking back to Figure 7.1, one can see that the workflow branches after four steps, where we distinguish two cases. In the case of no previous executions, we perform the full prediction steps as described in the previous section. In the case of previous executions, we already have provenance information available in our triple store, which describes the last execution and the related model provenance information (for each indicator). The model provenance includes for each indicator the number of PCs, the number of predictors used from these PCs, the chosen prediction base method, method parameters (i.e., 1 http://citydata.ai.wu.ac.at/MV-Predictions/ the number of clusters in the KNN) and the NRMSE.

In summary, we keep provenance for our predictions on three levels:

- For each execution, we publish the median NRMSE over all indicators, number of predictors, creation date and the creation agent;
- For each indicator, we publish the model provenance data;
- For each predicted value published as a qb:Observation, we provide the overall absolute RMSE (using the predicate cd:estimatedRMSE) and the estimated NRMSE (using the predicate cd:estimatedNormalizedRMSE). Further, we point to better observations (published with an lower NRMSE) using the predicate cd:preferredObservation which might occur if another approach such as a different base method or QB equations (discussed in Chapter 6) improve the predicted values.

For describing the model provenance, we use the *MEX vocabulary*, which is lightweight compared to other vocabularies (i.e., DMOP [Keet et al. 2015]) and designed for exchanging machine learning metadata [Esteves et al. 2015]. We use the *MEX Algorithm* layer to describe our prediction method and its parameter and the *MEX Performance* layer to describe the NRMSE. Further, we describe each execution using attributes of *MEX Execution*.

Example 7.1. The following example gives an intuition into reading the data about missing value predictions.

cvmv:predDS1 rdf:type qb:DataSet . cvmv:predDS1 prov:wasGeneratedBy cvmv:runP1. cvmv:predDS1 dc: title "A3_2004-2016_ncp80_seed_100_pred_80". cvmv:runP1 rdf:type mexc:Execution; prov: Activity . cvmv:runP1 cdmv:prediction\pc{}s 80 . cvmv:runP1 mexp:rootMeanSquaredError 1.0705. cvmv:runP1 mexc:endsAt "2017-07-31T10:52:02Z"^^xsd:dateTime . cvmv:runP1 cvmv:hasPredicted cvmv:runP1_1. cvmv:runP1_1 mexc:datasetColumn cd:no_bedplaces_in_tourist__accommodation_establishments . cvmv:runP1_1 mexc:hasAlgorithmConfig mexa:Regression. cvmv:runP1_1 cd:estimatedAbsoluteRMSE 3228.8726. cvmv:runP1_1 cd:estimatedNormalizedRMSE 1.78259. cvmv:runP1_1 cdmv:size 2737 . cdmv:obs1 rdf:type cd:PredictedObservation. cdmv:obs1cd:hasIndicator no_bed-places_in_tourist__accommodation_establishments . cdmv:obs1 sdmx-dimension:refArea dbr:Bolzano . cdmv:obs1 dcterms:date "2010" . cdmv:obs1 sdmx-measure:obsValue 1490.4485. cdmv:obs1 cd:estimatedAbsoluteRMSE 3228.8726. cdmv:obs1 cd:estimatedNormalizedRMSE 1.78259. cdmv:obs1 cd:preferredObservation cdmv:obs1. cdmv:obs1 qb:dataSet cvmv:predDS1.

The example shows a qb:DataSet of predicted values generated by a run

on 31 July 2017 using our PCA-based approach. We show one predicted value and its RMSES for the indicator no_bed-places_in_tourist__accommodation_establishments of the city of Bolzano in the year 2010. The best method for this indicator was MLR which is indicated by the triple: cvmv:runP1_1 mexc:hasAlgorithmConfig mexa:Regression.

The triple cdmv:obs1 cd:preferredObservation cdmv:obs1 states that there is no better prediction available, i.e., that this observation is itself the preferred (i.e., best) for the respective indicator for this city/year.

In summary, while with the availability of more and new raw data we could improve the prediction quality compared to Bischof, Martin et al. [2015a], this is—essentially, apart from the more structured workflow and publication using provenance information for all predictions—where we stopped missing value prediction in our earlier work in Bischof, Martin et al. [2015a].

7.3 Evaluation

In this section, we summarise experiments we conducted to evaluate both the performance of our crawls as well as the quality of enrichment.

The OCDP runs distributed over several components. The UNdata wrapper is a server component that runs at WU Vienna and the Eurostat wrapper is also a server component that runs in a cloud environment. The crawler and rule engine is a client component that dereferences the seed IRIS, follows links and performs the reasoning that lead to the unified global cube. The resulting files are then inserted into the SPARQL endpoint. From that point on, all further enrichment is carried out over the combined global cube via the SPARQL endpoint.

In Section 7.3.1 we first describe in more detail the process that leads to the global cube becoming accessible via the SPARQL endpoint. We then cover in Section 7.3.2 the enrichment process, consisting of statistical missing value prediction and calculating the values based on QBEs. The missing value prediction is performed asynchronously on a workstation on a regular basis, following the regular crawls of the crawler.

7.3.1 Crawling and Global Cube Materialisation

The machine that runs the crawling and rule engine Linked Data-Fu is equipped with two eight-core Intel Xeon E5-2670 CPUs running at 2.60GHz and 256 GB of main memory. Crawling and integration runs separately for Eurostat and UNdata. The result is one N-Quads file containing the Eurostat portion of the global cube and one N-Quads file containing the UNdata portion of the global cube. We separately run the "rapper" RDF parser over the files to ensure that subsequent SPARQL loading steps do not fail with syntax errors. The crawling and rule application requires around 6 minutes for Eurostat and around 24 minutes for UNdata. For the 1666 379 observations of Eurostat, 473 RDF documents containing 10 751 759 triples are dereferenced (567 MB). The rule application derives 1666 619 triples. For the 128 693 observations of UNdata, 4 505 RDF documents containing 1 690 231 triples are dereferenced (152 MB). The rule application derives 1 002 135 triples. While accessing UNdata yields less triples than accessing Eurostat, the UNdata data is distributed over many more files and requires more HTTP requests.² Thus, the UNdata access takes much longer than the Eurostat access.

Loading the global cube into the Virtuoso SPARQL endpoint requires 190 seconds. Filtering and skolemisation takes 20 minutes.

7.3.2 Statistical Missing-Values-Prediction

In Section 7.2 we reported on evaluation of the missing values prediction in detail. Recall that we perform PCA to reduce the number of dimensions, which allows us to impute all the missing values with neutral values for the PCA and then evaluate the quality of the predictions using different (the respectively best one per indicator) base statistical regression methods.

As for runtime performance, our current statistical prediction runs need on a Ubuntu Linux server with 2 cores and 2.6 GHz approximately 35 hours for all indicators and testing all base methods. The run time might grow slightly with the number of indicators, hence we aim to optimise the predictions runs by using our model provenance information, and evaluate only the best base method, which should reduce the runtime by factor three.

As mentioned in Section 7.2, we have identified two main goals for filling in missing values:

- 1. It is important to build models which are able to predict many (preferably all) missing values.
- Second, the prediction accuracy of the models is essential, so that the Open City Data Pipeline can fulfil its purpose of publishing high-quality, accurate data and predictions.

Median prediction accuracy in our approach is 0.55%RMSE over all indicators for the years 2004–2017, which allows us to predict new 608 848 values on top of the existing 693 684. Recall that despite the use of PCA, this difference occurs, since we drop too sparse rows/columns in the data matrix before PCA, in order to accept at an acceptably low overall median %RMSE, so we cannot predict anything for very sparse areas of the data matrix. Still, while we already discussed in Section 7.2 that the accuracy has improved considerably since our prior work in [Bischof, Martin et al. 2015a], however, as mentioned beforehand, our main goal was to improve these predictions further by the combination with QBES, i.e. to both improve the quality of predictions and enable to predict more missing values overall.

2 We wait 500 ms between requests to not overload the server providing data. Next we quantify the results of the considered QBEs themselves and their evaluation performance, and then report on the correctness of and improvements by the combination of QBEs with statistical regression methods.

7.3.3 QB Equations

Section 6.4 described the implementation of QBES in the OCDP. In this section we give some results about the behaviour of the QBES part of the OCDP system³ and some evaluation of the QB evaluation themselves and how they improve the results of the whole OCDP.

Normalisation The normalisation to generate QB rules from QBEs took 25 seconds to normalise 61 QBEs from Eurostat into 267 QB rules.⁴ Appendix C contains a complete example QBE from Eurostat and one of the normalised QB rules.

Creating SPARQL Queries First we filter out 76 QB rules for which at least one input variable matches no existing observation. Such rules can never deliver any results and evaluating them is thus needless. Virtuoso could generally not evaluate 44 QB rules which contain seven or more input variables. Eventually we created 147 SPARQL CONSTRUCT queries in five seconds. Appendix C shows a complete example of a SPARQL CONSTRUCT query together with the corresponding QB rule.

Evaluating Queries in Rule Engines This one iteration of evaluating all generated 147 SPARQL CONSTRUCT queries took 28 minutes (time-outs for 12 queries) and inserted 1.8M observations (46M triples) into the global cube.

From the different data sources the OCDP crawler collects 991k observations. The statistical missing-values prediction returns 522k observations which are better than any QBE observation (if existing). The QBEs return 230k observations better than any other prediction or QBE observation (if existing); additionally, 232k new observations computed by QBEs were actually not predictable at all (due to bad quality) with the statistical regression methods. Eventually the whole OCDP dataset contains 1975k observations.

Apart from these overall numbers, we provide more details on particular aspects on the correctness of and improvements by the combination of statistical regression methods and QBEs for predicting missing values in the rest of this section.

7.3.4 Correctness of Generated QB Observations

Firstly, to show the correctness of the QBE approach on raw data (first step of the workflow described in Section 7.1, we compared the observations derivable by QBEs only from crawled observations with the corresponding crawled

3 for more details see http://citydata.wu.ac.at/ocdp/import

4 the Eurostat indicator definition for the population change over 1 year is the only indicator not expressible in QBES observations. We made the following observations: in the sources we currently consider, equations had already been applied in the raw data before import, and thus applying them beforehand in Step 1 of the workflow in Section 7.1 did not have a notable effect. This can mainly be explained by the fact that our considered equations stem from Eurostat's indicator definitions, and therefore from within *one* dataset, where they are already pre-computed. That is, in the cases of consistent input observations (no more than one observation per city-year-indicator combination) the QBES computed consistent results with respect to the crawl.

Notably, however, for the cases of inconsistent/ambiguous input observations in the raw data, the QBEs also possibly compute ambiguous resulting observations. In fact, we discovered 48 643 such cases of inconsistent/ambiguous observations, that is, multiple observations per city-year-indicator combination. While again, as described in Section 7.1, Step 1, we do not resolve these inconsistencies in the raw data, we "punish" them in the computation by assigning inconsistent input observations with an estimated RMSE corresponding to the deviation from the average above all the inconsistent observations for a single city-year-indicator combination.

We note that using QBEs could also be used to aid consistency checking, for instance our experiments unveiled a missing constant factor in one of the Eurostat indicator definitions⁵ as well as wrongly mapped cities and indicators during the development process.

In general, it makes sense to evaluate the QBEs based on the crawled data and thus enrich the crawled dataset to achieve better results in the following application of statistical regression methods. However, in our experiments which focused in the UN and Eurostat datasets, the prior application had only marginal effects: in our case almost half of the new observations (10 178 of 26 452) that could be generated in this way were for the indicator "Women per 100 men", because this is the only Eurostat indicator for which the UN dataset contained both necessary base indicators (population male and population female); the other cases could again be traced back to inconsistencies in the source data.

7.3.5 Quality Increase of the Combination Approach

To test the quality increase of the combined method, we tested which ones were the best observations, comparing statistically predicted observations, with QB-equation-generated observation depending on the estimated RMSE associated with each observation, with real factual observations. As described in Chapter 6 a QBE observation is only computed if the estimated RMSE multiplied by the confidence threshold (CT) is smaller than the estimated RMSE of any other corresponding observation. Through experimentation during the development of the OCDP we found a confidence threshold of 30 being a good compromise between data quality without sacrificing too many good

5 the indicator "Women per 100 men—aged 75 years and over" is missing a factor 100 observations. We got the same or a better RMSES for 80 of the 82 tested indicators: these 82 indicators are those for which overlapping indicators from the statistical predictions and QBES were available together with actual observed values from the crawl.

We have summarised the results of this analysis in Table 7.1 for detailed RMSES for the predicted and the QBE observations of all 82 tested indicators. For each indicator, the tables lists in the first three columns the numbers of crawled, predicted and QBE computed predictions. The next three columns list the accuracy in terms of actual RMSE (i.e. not estimated, but comparing real existing observations with values generated through predictions or through QBEs): we see here that, in combination the two methods performed better or equal than statistical predictions alone in most cases (indicated in bold face values in the "Combined" column), i.e., we got as mentioned above the same or better RMSE for 80 out of the tested 82 indicators.

Finally, an important property of the combined method is how precise/accurate the propagated error computation is, since this propagated estimated error (RMSE in our case) is used to decide which observation is classified as the best observation for a given city-year-indicator combination. We thus model this as a binary classification task: for a fixed city-year-indicator combination, given the corresponding prediction observation and the best observation generated by a QBE, both with error estimates, is the QBE observation value nearer to the actual value than the predication observation value? In this case we are more interested in a minimal number of false positives (QBE observation wrongly selected as better) even at the cost of a higher number of false negatives (better QBE observation wrongly not selected as better). Of the usual measures to quantify the quality of classification tasks we thus are mainly interested in precision. We get an average precision of 90.8% for a confidence threshold of 30, while we miss quite some true positives (significantly lower accuracy). See Table 7.1 for detailed results ("precision" and "accuracy") of all 82 indicators.

As we can demonstrate, even an incomplete materialisation of equations allows us to predict a significant amount of new or improved observations, that could not be predicted with equal accuracy solely with the statistical methods.

7.4 Related Work

In this section, we explain how our work distinguishes itself from the related work in the areas of modelling, integrating and querying of numerical data using web technologies, of predicting/imputing missing values and of using declarative knowledge for inferencing of numeric information.

The work of Santos et al. [2017] describes a methodology to describe city data for automatic visualisation of indicators in a dashboard. The work is

Table 7.1: Evaluation results 82 indicators (for which crawled, predicted and QBE observations existed). The "Observation source" lists how many chosen best observations which of the three sources contributed. The "RMSE" columns give the RMSEs of Predictions and QBEs as well as the combined system. The quality measures, especially the precision, give an indication how well the error propagation classified better observations. In the cases marked with a * no improvements were observed by the QBEs, i.e., the statistical predictions were better than any possible QBE.

		ervation sour	ce	RMSE			Quality measures	
Indicator	Crawled	Prediction	QBE	Prediction	QBE	Combined	Precision	Accuracy
average size of households	3 463	3 194	0	0.04	0.08	0.04	*	0.63
crude birth rate per 1 000 inhabitants	6 739	1 079	194	10.19	0.38	10.19	*	0.36
crude death rate per 1 000 inhabitants	6 4 1 7	1 273	59	9.30	0.28	9.30	*	0.31
economically active population female	4 5 1 7	3 0 2 5	104	3 083.12	9 636.50	3 083.12	*	0.72
economically active population male	4 520	3 0 2 5	104	2 887.80	12 171.77	2 887.80	*	0.78
economically active population total	4 750	2 765	108	4 581.38	6 596.52	4 581.38	*	0.49
employment jobs in agriculture fishery nace rev 2 a	3 2 4 4	3 003	729	231.26	1 044.50	228.71	1.00	0.45
employment jobs in construction nace rev 2 f	3 4 4 7	2 294	1 317	775.68	1 378.20	775.62	1.00	0.24
employment jobs in mining manufacturing energy nace rev 2 b-e	3 4 4 2	2 511	1 105	2 042.92	6 692.59	2 042.89	1.00	0.40
eu foreigners	4 268	774	2 3 4 1	2 777.38	597.50	2 746.81	0.91	0.29
eu foreigners as a proportion of population	4 209	2 840	306	0.65	0.42	0.65	*	0.25
foreign-born	2 149	246	3 96 1	18 408.69	3 095.48	18 305.70	0.98	0.19
foreign-born as a proportion of population	2 136	4 074	134	2.94	1.52	2.94	*	0.43
foreigners	3 290	389	2 748	13 187.75	1 394.98	13 176.48	0.98	0.22
foreigners as a proportion of population	3 261	2 914	238	1.65	0.89	1.65	*	0.38
households owning their own dwelling	2 624	1 449	3 036	3 998.24	50 431.29	3 998.24	*	0.26
households with children aged 0 to under 18	4 0 2 3	967	2 3 4 1	1 952.82	6 703.39	1 952.77	1.00	0.14
infant mortality per year	5 2 1 4	1 383	1 062	1.61	7.98	1.61	*	0.28
infant mortality rate per 1 000 live births	5 083	2 046	418	0.58	1.01	0.58	*	0.42
lone parent households per 100 househ. with children aged $0-17$	3 0 3 7	4 0 4 2	107	0.73	3.33	0.73	*	0.78
lone parent private households with children aged 0 to under 18	3 180	282	3 774	674.46	341.52	674.46	1.00	0.13
lone pensioner above retirement age households	3 609	2 849	766	88.58	4 590.84	88.58	*	0.26
nationals	5 569	1 1 2 2	1 056	73 639.26	12 052.11	73 355.72	1.00	0.22
nationals as a proportion of population	5 531	1 733	457	116.24	2.92	116.24	0.94	0.33
native-born	2 1 5 9	350	3 8 4 5	99 075.25	8 725.38	99 075.25	*	0.18

126

		Observation source			RMSE	Quality measures		
Indicator	Crawled	Prediction	QBE	Prediction	QBE	Combined	Precision	Accuracy
native-born as a proportion of population	2 146	3 999	197	23.54	2.84	23.54	*	0.58
no available beds per 1 000 residents	3 836	3 4 3 7	30	57.56	397.42	57.56	*	0.63
no bed-places in tourist accomm. establishments	4 2 2 6	3	3 4 4 3	166 966.67	3 349.37	166 948.07	0.98	0.67
no children 0–4 in day care or school	4 051	3 1 1 3	503	579.63	522.03	579.62	0.91	0.47
no children o –4 in day care publ and priv per 1 000 children o –4 $$	3 3 2 3	3 556	93	20.92	610.03	20.91	1.00	0.74
no cinema seats per 1 000 residents	2 283	3 0 2 7	1 336	33.37	1.82	33.37	1.00	0.15
no cinema seats total capacity	2 660	2 0 3 5	2 278	822.75	633.30	798.6	0.99	0.18
no deaths in road accidents	5 574	668	1 044	2.42	1.86	2.42	*	0.20
no households living in apartments	2 1 1 5	1 261	3 369	6 103.92	32 588.96	6 103.92	*	0.27
no households living in houses	2 1 5 3	2 0 2 7	2 5 4 2	10 502.07	24 758.61	10 498.78	0.88	0.26
no live births per year	6 974	231	987	476.76	156.75	489.98	0.08	0.23
no private cars registered	4 693	856	1 814	43 201.98	4 490.18	43 047.54	0.83	0.25
no registered cars per 1 000 population	4 549	2 264	464	562.66	18.06	562.59	0.90	0.31
no tourist overnight stays in reg accomm. per year per resident	4 821	2 674	54	13.10	0.79	13.10	*	0.14
non-eu foreigners	4 2 5 0	377	2 730	7 884.07	1 085.92	7 858	0.97	0.23
non-eu foreigners as a proportion of population	4 191	2 902	236	1.40	0.35	1.40	*	0.31
one person households	4 2 3 4	231	2 982	3 901.77	14 048.54	3 900.09	1.00	0.14
people killed in road accidents per 10 000 pop	5 1 7 2	1 765	37	0.33	0.02	0.33	*	0.19
persons unemployed female	5 741	2 105	7	734.71	387.00	734.71	*	0.28
persons unemployed male	5 798	2 054	7	808.36	342.44	807.88	1.00	0.22
persons unemployed total	5 262	2 402	14	450.51	523.96	450.51	*	0.51
population	17 058	50	99 081	746 087.75	746 119.20	746 256.30	0.19	0.34
population female	14 181	580	4 380	76 682.77	75 971.54	76 682.77	*	0.50
population living in private househ. excl. institutional househ.	3 602	2 498	614	55 048.78	25 328.24	55 048.78	*	0.25
population male	14 183	4 838	122	71 411.92	71 769.93	71 411.92	*	0.48
population on the 1st of january 10–14 years total	4 9 1 4	272	1 546	3 831.38	656.61	3 831.38	*	0.23
population on the 1st of january 25–34 years total	6 4 1 6	276	666	13 231.20	1 064.67	13 2 1 4.86	1.00	0.21
population on the 1st of january 35–44 years total	6 46 1	194	724	7 044.37	1 020.55	7 018.79	1.00	0.21
population on the 1st of january 45–54 years total	6 435	366	551	6 395.69	838.57	6 352.97	1.00	0.20

	Observation source			RMSE			Quality measures	
Indicator	Crawled	Prediction	QBE	Prediction	QBE	Combined	Precision	Accuracy
population on the 1st of january 5–9 years total	4 866	211	1 629	4 084.84	717.81	4 084.84	*	0.22
population on the 1st of january 55–64 years total	8 379	134	140	5 172.41	808.54	5 091.16	1.00	0.27
population on the 1st of january 65–74 years total	8 401	124	123	4 870.38	590.66	4 837.58	1.00	0.25
population on the 1st of january 75 years and over female	6 860	1 140	*	471 071.80	22 798.19	114 272.33	0.72	0.71
population on the 1st of january 75 years and over male	6 889	1 1 2 9	*	12 645.78	279 859.81	12 645.78	*	0.72
population on the 1st of january 75 years and over total	8 4 1 3	55	195	5 594.77	539.03	5 577.07	1.00	0.20
private households excl. institutional households	5 1 3 0	3	2 468	6 759.09	51 025.85	6672.43	0.96	0.37
proportion households that are lone-pensioner households	3 508	3 700	*	0.08	0.12	0.08	*	0.48
proportion of employment in agriculture fishery	3 1 7 2	3 525	253	0.26	25.71	0.26	*	0.55
proportion of employment in construction nace rev11 f	3 386	3 550	98	0.35	7.71	0.35	*	0.7
proportion of employment in industries nace rev11 c-e	3 384	3 3 2 5	325	1.66	9.79	1.66	*	0.60
proportion of households living in apartments	1 867	4 494	265	1.97	4.67	1.97	*	0.6
proportion of households living in houses	1 929	4 2 1 4	482	1.80	3.08	1.80	*	0.5
proportion of households living in owned dwellings	2 299	4 308	333	1.75	21.97	1.75	*	0.6
proportion of households that are 1-person households	4 1 2 8	3 2 5 4	51	0.87	3.06	0.87	*	0.7
proportion of households that are lone-parent households	3 065	4 088	66	0.18	0.57	0.18	*	0.6
proportion of households with children aged 0–17	3 9 1 7	3 345	54	0.52	2.20	0.52	*	0.79
proportion of population aged 0–4 years	8 328	313	0	0.08	1.00	0.08	*	0.9
proportion of population aged 10–14 years	4 893	1 817	8	1.16	0.13	1.16	*	0.62
proportion of population aged 15–19 years	8 341	272	0	0.10	6.72	0.10	*	0.9
proportion of population aged 20–24 years	8 326	259	26	0.15	9.05	0.15	*	0.9
proportion of population aged 25–34 years	6 337	771	190	10.25	0.47	10.25	*	0.3
proportion of population aged 35–44 years	6 382	781	156	9.27	0.50	9.27	*	0.3
proportion of population aged 45–54 years	6 356	672	264	10.43	0.48	10.43	*	0.2
proportion of population aged 5–9 years	4 845	1 847	0	1.15	0.14	1.15	*	0.6
proportion of population aged 65–74 years	8 384	183	72	8.86	0.29	8.86	*	0.3
proportion of population aged 75 years and over	8 396	198	60	6.71	0.25	6.71	*	0.3
proportion of total population aged 55–64	8 362	208	74	13.61	0.40	13.61	*	0.2

different from our work in several regards. Our work directly reuses w3c standardised vocabularies PROV and QB as well as common Linked Data wrappers and crawlers and as such is more widely applicable. Our work makes use of a pre-existing carefully handcrafted list of common statistical indicators (city data ontology) that was mainly inspired from the Eurostat urban audit but also takes into account other city data sources; the ISO 37120:2014 used by Santos et al. [2017] only lists 100 roughly defined indicators whereas urban audit uses over 200 indicators with available numbers and for some of these indicators also provides computation formulas. The work of Santos et al. [2017] focuses on automatic selection of suitable data for indicators using Prolog inferences and automatically selecting the right visualisation; this was demonstrated with only one indicator bicycle "trips per station". Our work instead focuses on the combination of declarative knowledge and machine learning for deriving/predicting new values from integrated datasets and for that presents a widely-applicable data integration, enrichment and publication pipeline evaluated on a set of more than 200 indicators.

7.4.1 Numerical Data in Databases

Siegel, Sciore and Rosenthal [1994] introduce the notion of semantic values numeric values accompanied by metadata for interpreting the value, e.g., the unit—and propose conversion functions to facilitate the exchange of distributed datasets by heterogeneous information systems.

Diamantini, Potena and Storti [2013] suggest uniquely defining indicators (measures) as formulas, aggregation functions, semantics (mathematical meaning) of the formula and recursive references to other indicators. They use mathematical standards for describing the semantics of operations (Math-ML, OpenMath) and use Prolog to reason about indicators, e.g., for equality or consistency of indicators. In contrast, we focus on heterogeneities occurring in terms of dimensions and members, and allow conversions and combinations.

As a basis for sharing and integration of numerical data, XML is often used [J. M. Pérez et al. 2008]. XML standards such as XCube fulfil requirements for sharing of data cubes [Hümmer, Bauer and Harde 2003] such as the conceptual model of data cubes, the distinction of data (observations) and metadata (dimensions, measures), a network-transportable data format, support for linking and inclusion concepts, extensibility, conversion capability and OLAP query functionality. Other advantages of XML include schema definitions (XML Schema), there are data modification and query languages for XML such as XSLT and XQuery, and there are widely-used XML schemas for representing specific information, e.g., XBRL for financial reports, SDMX for statistics, DDI⁶ for research studies. Another XML-based exchange standard for ETL transformations and data warehouse metadata is the Common Warehouse Metamodel (CWM)⁷ by the Object Management Group (OMG).

6 http://www.ddialliance.org/

7 http://www.omg.org/spec/CWM/

However, the integration of data across different standards is still an unresolved issue. CWM—but also other interfaces and protocols to share multidimensional datasets such as XML for Analysis and OLE DB—lack a formal definition making it more difficult to use such formalism as a basis for integration [Vassiliadis and Sellis 1999]. XML schemas are concerned with defining a syntactically valid XML document representing some specific type of information. Yet, XML schemas do not describe domain models; without formal domain models, it is difficult to derive semantic relationships between elements from different XML schemas [Klein et al. 2001]. Often, the domain model for an XML schema is represented in a semi-formal way using UML documents and free text. In contrast, schemas described as an OWL or RDFS ontology such as QB have a formal domain model based on logics.

In theoretical data integration we distinguish global-as-view and localas-view approaches [Lenzerini 2002]. In the global-as-view (GAV) approach also known as source-based integration—the global schema is represented in terms of the data sources. In the local-as-view (LAV) approach, sources are defined as views over the global schema. We use the GAV approach and define the global cube in terms of single data cubes using the drill-across operation. With GAV, queries over the global schema can easily be translated to queries over the data sources [Calì, Calvanese et al. 2002]. The advantage of LAV is that the global schema does not need to change with the addition of new data sources. The advantage of GAV is that queries over the global schema can easily be translated to queries over the data sources.

7.4.2 RDF Data Pipelines

Within the Semantic Web community there is extensive work around triplification and building data pipelines and Linked Data wrappers for publicly available data sources on the web, where for instance the LOD2 project has created and promoted a whole stack of tools to support the life cycle of Linked Data, i.e. creating maintainable and sustainable mappings/wrappers of existing data sources to RDF and Linked Data, a good overview is provided in the book chapter by Ngomo et al. [2014] and Auer et al. [2012]. All this work could likewise be viewed as an application of the classical ETL (Extract-Transform-Load) [Golfarelli and Rizzi 2009] methodology extended to work on the web, based on open standards and Linked Data principles [Berners-Lee 2006]. Our work is not much different in this respect, with the difference that we apply a tailored architecture for a set of selected sources around a focused topic (city data), where we believe that a bespoke combination of rule-based reasoning methods in combination with statistical machine learning can provide added value in terms of data enrichment. This is a key difference to the abovementioned methods that focus on entity linkage and object consolidation in terms of semantic enrichment. However, this focused approach is also different from generic methods for reasoning over Linked Data on the web (cf. e.g. [Aidan Hogan 2011] and references therein for an overview), solely based on OWL and RDFS which (except very basic application of owl:sameAs (for consolidating different city identifiers across sources) and rdfs:subPropertyOf reasoning (for combining overlapping base indicators occurring within different sources).

Other work tries to automatically derive new from existing data. Ambite and Kapoor [2007] present Shim Services providing operations for accessing remote data, integrating heterogeneous data and deriving new data. Workflows of operations are automatically created based on semantic descriptions of operators. Subsumption reasoning is included to match inputs of services to outputs of other services. To avoid the infinite execution of operations, a limit is defined to the depth of nested operations of the same type. In contrast to the automatically constructed workflows, our pipeline consists of a fixed set of processing steps. Instead of "shim services" that act as stand-alone components accessible via the network, we base the computation on local formulas and use a vocabulary to represent the formulas.

7.4.3 Data Modelling and Representation

Besides the QB vocabulary that we are using in this work, there are other vocabularies available to publish raw or aggregated multidimensional datasets. For instance, Niinimäki and Niemi [2009] list various OWL ontologies for representing multidimensional datasets. Also, several lightweight ontologies have been proposed, such as scovo [Hausenblas et al. 2009] and scovoLink [Vrandečić, Lange et al. 2010]. Other vocabularies for statistical data are the DDI RDF Vocabularies,⁸ several vocabularies inspired by the Data Documentation Initiative and the StatDCAT application profile⁹ (StatDCAT-AP) to express in a structured way the metadata of statistical datasets which are currently published by the different agencies in the European Union.

In comparison to these approaches, we see several reasons for choosing the QB vocabulary. QB, as a W3C recommendation, is an established standard for aggregating and (re-)publishing statistical observations on the web, with off-the-shelf tools to process and visualise QB data. QB's wide adoption is an important factor for data integration use cases, as sources already represented in QB can be integrated more easily than sources in other representations. Further, QB has shown applicability in various use cases [Kämpgen and Cyganiak 2013], and exhibits the necessary formality to allow efficient and flexible integration and analysis of statistical datasets. The multidimensional data model of QB allows explicit different dimension value combinations, e.g., _:obs cd:unit "km2". and _:obs dcterms:date "2010"., which is important for interpreting the semantics of values and for integration purposes [Vrandečić, Lange et al. 2010]. 8 http://www.ddialliance.org/ Specification/RDF 9 https://www.europeandataportal. eu/de/content/statdcat-ap-wgvirtual-meeting

7.4.4 Missing Value Imputation

Several reference works describe procedures on handling missing values from the perspective of statistics as well as from social sciences, e.g. cf. Buhi, Goodson and Neilands [2008] and Switzer and Roth [2008]. The statistical offices, for example Eurostat, already use these methods to impute missing values in their datasets [Office for Official Publications of the European Communities 2004]. Since our integrated dataset showed high missing-value ratios (see Tables 5.1 and 5.2), the statistical methods usually used for for missing-value imputation are not applicable anymore. Instead we rely on PCA, a method successfully used in recommender systems, which are designed to handle high missing-value ratios. For example, a method based on singular value decomposition (SVD), which is similar to PCA [Shlens 2014], eventually won the Netflix Prize in 2009 [Koren 2009]. Within the Semantic Web community, a main focus on value completion has been in the prediction of generic relations, and mainly object relations (i.e. link-prediction) on the object level rather than on numerical values, cf. Paulheim [2017] for an excellent survey on such methods. The usage of numerical values is a a rather recent topic in this respect. Along these lines, but complementary to the present work, Neumaier, Umbrich, Parreira et al. [2016] (as well as similar works referenced therein) have discussed methods to assign bags of numerical values to property-class pairs in knowledge graphs like DBPEDIA (tailored to finding out relations that, for instance, a certain set of numbers could possibly be "population numbers of cities in France"), but not specifically to complete/impute missing values. Our method instead, uses standard, robust and well-known methods (KNN, linear regression and random forest) for numerical missing value imputation based on principle components [Roweis 1997]. This could be certainly refined to more tailored methods in the future, for instance using time-series analysis; indeed our predicted values, while reasonably realistic in the value ranges often show some non-realistic "jumps" when raw data for a certain indicator is available over a certain sequence of years, but missing for only a few years in between. Since the missing value imputation component in our architecture is modularly extensible with new/refined methods, such refinements could be added as future work.

IN SUMMARY, with the combination of equational knowledge and statistical methods we could improve missing value quality when compared to the two methods alone.

PART IV

CONCLUSION

8

Summary and Discussion

More and more data interesting for data analysis is published on the Web along Semantic Web standards and Linked Data principles. To make these datasets usable, different problems of semantic heterogeneity have to be addressed. In this work we gave four contributions to approach these problems. This chapter concludes this work by summarising and evaluating these contributions before eventually giving an outlook of future work.

Section 8.1 summarises the four main contributions given in this work. Section 8.2 evaluates the main contributions with respect to the research questions stated in Chapter 1. Section 8.3 concludes this thesis be suggesting interesting directions of future work, extending and complementing the presented contributions.

8.1 Summary

This section summarises the main research contributions introduced in this thesis: (i) schema-agnostic rewriting with SPARQL 1.1 property paths (Chapter 3), (ii) RDF attribute equations (Chapter 4), (iii) QB equations (Chapter 6) (iv) Combination of equational knowledge and statistical methods (Chapter 7).

8.1.1 Schema-Agnostic Query Rewriting

To the best of our knowledge, our work in Chapter 3 is the first to present a query rewriting approach for ontology-based data access in OWL QL that is completely independent of the ontology. The underlying paradigm of schema-agnostic query rewriting appears to be a promising approach that can be applied in many other settings. Indeed, two previous works, nsparqL [J. Pérez, Arenas and Gutierrez 2010] and PSPARQL [Alkhateeb 2008], independently proposed query-based mechanisms for reasoning in RDFs. While these works have not considered SPARQL 1.1, OWL QL, or arbitrary conjunctive queries, they still share important underlying ideas. We think that a common name is very useful to denote this approach to query rewriting.

With schema-agnostic query rewriting, we focused on laying the foundations for this new reasoning procedure. An important next step is to study its practical implementation and optimization. Considering the size of some 136

of the queries we generate, one would expect them to be challenging for RDF stores. Future work will be concerned with developing further optimizations that can be used in practical evaluations.

8.1.2 RDF Attribute Equations

In Chapter 4 we presented a novel approach to model mathematical equations as axioms in an ontology, along with a practical algorithm for query answering using SPARQL over such enriched ontologies. To the best of our knowledge, this is the first framework that combines ontological reasoning in RDFs, inferencing about functional dependencies among attributes formulated as generic equations, and query answering for SPARQL. Experimental results compared to rule-based reasoning are encouraging. Given the increasing amount of published numerical data in RDF on the emerging Web of data, we strongly believe that this topic deserves increased attention within the Semantic Web reasoning community.

8.1.3 QB Equations

In order to transfer the theoretic results of Chapter 4 to the real-world use case of integrating statistical datasets about cities, introduced in detail in Chapter 5, we introduced QB equations in Chapter 6. QB equations allow us to express equational knowledge for multi-dimensional QB datasets and compute new values or estimate missing values. QB equations reuse and extend central definitions of RDF attribute equations from Chapter 4 and are conceptually related to Complex Correspondences by Kämpgen, Stadtmüller and Harth [2014]. We specifically provide an RDF syntax which allows expressing equational knowledge, equations and rules, independent of a concrete dataset description. Besides the automatic computation of new values, the rule-based semantics provides error propagation, for computations on uncertain values, and provenance tracking, already used in the termination condition. Termination is ensured by avoiding reapplication of an equation and aided by the supplied propagated error. Evaluation of QB equations as part of the Open City Data Pipeline in Section 7.3 showed that new values could be computed on real-world datasets. Furthermore, when compared to statistical missing value predictions alone, the combination of QB equations with statistical missing value methods produced more, and higher quality, observations.

8.1.4 Equations and Statistical Methods Combined

In Chapter 5 we presented the *Open City Data Pipeline*, an extensible platform for collecting, integrating, and enriching open city data from several data sources including Eurostat and UNdata. We developed several components

including wrappers, a data crawler, an ontology-based integration platform and a missing value prediction module, detailed in Chapter 7, which relies on both statistical regression methods and exploiting known equations with QB equations: given we deal with very sparse datasets, the prediction (or, as it is often referred to, imputation) of missing values is a crucial component.

As for the former, we predict target indicators from components calculated by Principal Component Analysis. We applied three basic regression methods and selected the best performing one.

As for the latter, we showed that the predictions computed this way can be further improved by exploiting equations, where we have estimated and verified the assumption that this combination improves prediction accuracy overall, in terms of the number of filled-in values and estimated errors.

The prediction values are fed back into our triple store and are accessible via our SPARQL endpoint or Web UI. Here, we additionally publish provenance information including the used prediction methods and QB equations, along with estimated prediction accuracy.

In the wrapper component, integrating cities and indicators for a new dataset (often csv tables) is still a slow, manual, process, and needs custom scripting. Particularly, entity recognition for cities can only partially be automated and needs manual adaptation for each wrapper. Also, mapping indicators is still a largely manual process, where in the future, we plan to apply instance based mapping learning techniques used in ontology matching (cf. Euzenat and Shvaiko [2013]). We emphasise here, that in fact such approaches could rely on and extend similar regression techniques as we used for imputing missing values.

As for combining missing value prediction techniques and QB equations, we improved the Open City Data Pipeline since Bischof, Martin et al. [2015a], not only refining our methods, but also by proving the conjecture that the more data we collect, the better the predictions actually get: by applying the PCA-based prediction approach, using standard regression techniques without customisation, we reach a good quality for predictions (overall NRMSE of 0.55%) and are able to fill large gaps of missing values, which can be further improved by the combination with QB equations.

The republication of our enriched dataset as Statistical Linked Data [Kämpgen, O'Riain and Harth 2012], using the standard QB format shall allow combining and integrating our dataset with other datasets of the Global Cube [Kämpgen, Stadtmüller and Harth 2014].

8.2 Critical Assessment of Research Questions

After recapitulating our contributions, we assess these contributions with respect to the motivating research questions given in Section 1.1.

Research question 1. Can we produce and effectively use rewritings of SPARQL queries which are independent of the ontology and avoid the exponential blowup of standard query rewriting techniques?

We addressed research question 1 in Chapter 3 where we showed in a series of formal proofs that we *can* rewrite SPARQL queries, independent of the ontology, for ontological querying: we showed that we can accommodate the OWL QL fragment of OWL, with the exception of owl:SymmetricProperty which can only be used in an alternative encoding. The resulting queries are, independent of the ontology, larger by a constant factor: type triple patterns *x* rdf:type *c* are rewritten to a UNION of 5 BGPs, whereas other triple patterns *x* p y for $p \in PRP$ are rewritten to a UNION of 3 BGPs. However, these BGPs comprise complex SPARQL path expressions. Still, we showed in a practical evaluation that schema-agnostic rewriting is a feasible approach for ontological querying. In some cases, the approach could reach comparable query evaluation times as the ontology-dependent rewriting system REQUIEM.

Research question 2. Can we express and effectively use equational knowledge about numerical values of instances along with RDFS and OWL to derive new values?

In Chapters 4 and 6 we introduced two approaches to address research question 2. The first approach, RDF attribute equations, target numerical data represented directly by *attributes* or OWL *datatype properties*. The second approach, QB equations, target a popular, more expressive multi-dimensional data model to represent statistical data.

In Chapter 4 we defined RDF attribute equations, to express and use equational knowledge for computing new numerical values. We chose a lightweight approach by extending the RDFs fragment of DL-Lite with equations by giving a suitable RDF encoding and a DL semantics. By implementing RDF attribute equations in a backward-chaining approach, we showed in a practical use case experiment, that RDF attribute equations can effectively be used to transparently compute numerical attributes during SPARQL query evaluation. Furthermore, we practically showed the combination of numerical computations with RDFS inferencing. Incorporating more expressive OWL QL reasoning remains part of future work. In a practical evaluation, our prototype outperformed a general-purpose rule-based reasoners working also in backward-chaining manner. Moreover, the compared backward-chaining reasoner would only terminate either, if non-monotonic termination predicates were used, or if the instance data was sufficiently restricted, i.e. the ABox is data-coherent. As expected, a forward-chaining reasoner showed termination problems, due to rounding errors occurring during the computations.

We transferred and extended the idea of RDF attribute equations by defining QB equations on top of a more expressive, multi-dimensional, data model in Chapter 6. We defined a concrete RDFs ontology to express equational knowledge for multi-dimensional data, specifically for data modelled with the QB vocabulary, and defined a rule-based semantics to allow automatic computation of new numerical values. In the evaluation in Section 7.3 we showed effective usage of QB equations using real-world equations derived from Eurostat indicator definitions. Furthermore, we used a forward-chaining implementation which reused the same termination condition as RDF attribute equations. We could avoid the termination problems of the rule-based forward-chaining reasoner, by exploiting the increased expressivity of the multi-dimensional data model, to track the provenance of newly generated instances and thus avoid repeated application of the same equations on derived data. This increased expressivity also facilitated the definition of error propagation for uncertain values. Ontological reasoning was not considered explicitly, but could be delegated to reasoners already contained in standard SPARQL engines.

Research question 3. Can we combine statistical inference with OWL and equational knowledge to improve missing value imputation?

In Chapters 5 and 7 we address research question 3. We define a workflow to combine equational knowledge, which is provided by QB equations, with standard statistical methods for missing value imputation. We introduced our approach to statistical missing value imputation by combining three complementary regression methods: KNN, MLR and RFD. We defined an iterative approach to evaluate QB equations and statistical methods on a QB dataset. We collected and integrated statistical city data from Eurostat and UNdata. With this combined dataset, we evaluated our combined workflow to show an increased quality and number of missing value predictions. Nonetheless, for the combination of numerical inferences (in terms of statistical methods and QB equations) with OWL, using schema-agnostic rewriting, we still had to leave this question partially open. We will discuss examples and possible approaches to address the combined problem in Section 8.3.5 below.

8.3 Future Work

In this thesis we introduced complementary methods for enriching Linked Data as a step for data preparation for data analysis. We now give an outlook of different and—to us—interesting directions of future work grouped by the main contributions of this work.

8.3.1 Schema-Agnostic Query Rewriting

While the queries we obtain by our schema-agnostic rewriting might be challenging for current RDF stores, large parts of the queries are fixed and can thus be optimized for faster query evaluation. Our work thus reduces the problem of adding OWL QL reasoning support to RDF stores to a query optimization problem for SPARQL property paths. This can also guide future work in RDF stores such as GraphDB (formerly OWLIM), which implement reasoning with inference rules: rather than trying to materialize (part of) an infinite OWL QL chase [Bishop and Bojanov 2011], they could materialize (sub)query results to obtain a sound and complete procedure. This provides completely new perspectives on the use of OWL QL in areas that have hitherto been reserved to OWL RL and RDFS.

8.3.2 RDF Attribute Equations

We observed during our experiments that single Web sources tend to be coherent in the values they report for a single city, thus data-incoherences, i.e. ambiguous results in our queries for one city, typically stem from the combination of different sources considered for computing values through equations.

Moreover, in the realm of DL-Lite query rewriting, following the Perfect-Ref algorithm [Calvanese, De Giacomo et al. 2007] which we base our adaptation on, there has been a number of extensions and alternative query rewriting techniques proposed [Pérez-Urbina, Motik and Horrocks 2010; Rosati and Almatelli 2010; Rosati 2012; Kontchakov, Lutz et al. 2011; Gottlob and Schwentick 2012] which could likewise serve as a basis for extensions of RDF attribute equations. Another direction for further research is the extension to a more expressive ontology language than DL_{RDFS}^{E} . Whereas we have deliberately kept expressivity to a minimum for now, apart from further DL-Lite fragments we are also particularly interested in lightweight extensions of RDFs such as OWL LD [Glimm, Adian Hogan et al. 2012] which should be considered for future work.

Apart from query answering, this work opens up research in other reasoning tasks such as query containment of SPARQL queries over DL_{RDFS}^{E} . While containment and equivalence in SPARQL are a topic of active research [J. Pérez, Arenas and Gutierrez 2009; Schmidt, Meier and Lausen 2010; Chekol et al. 2012], we note that containment, in our setting, depends not only on the BGPs, but also on FILTERs. E.g., intuitively query Q4 in our setting would be equivalent to the following query (assuming :population > 0):

```
SELECT ?C WHERE { ?C :populationFemale ?F .
?C :populationMale ?M . FILTER( ?F > ?M ) }
```

While we leave closer investigation for future work, we note another possible connection to related work [Clément de Saint-Marcq et al. 2012] on efficient query answering under FILTER expression based in constraint-based techniques.

Lastly, we would like to point out that our approach could be viewed as more related to constraint-handling-rules [Frühwirth 2006] than to mainstream semantic Web rules approaches such as swRL; we aim to further in-

8.3.3 QB Equations

While the implementation of QB equations in the Open City Data Pipeline produced more and better observations, the resulting dataset potentially violates the QB integrity constraint IC-12: "no duplicate observations" [Cyganiak, Reynolds and Tennison 2014, §11]. While conformance with IC-12 can be restored easily by deleting all but the best of a set of duplicate observations in a post-processing step, a revised semantics considering the integrity constraints would be desirable.

As mentioned in Section 7.3, QB equations cannot directly express equations for indicators such as "Population change over one year" because no construct exists to express a relation between dimension members—in this example the relation of one year to another. Currently such an equation could be modelled by a set of n-1 QB equations and QB rules, where n is the number of years, in the following manner (where y is a variable binding to each year except the most recent):

Population change between y and y + 1 = Population(y + 1) - Population(i)Population change over one year \leftarrow Population change between y and y + 1

This unsatisfactory modelling, however, will result in n - 1 new intermediary indicators, where n depends on the number of used *dimension members*. To express such indicator equations satisfactorily, a standard means to represent at least the *order* of dimension members is necessary, in our example the representation of the order of years. In general, an explicit RDF representation of *levels of measurement*, for example the nominal, ordinal, interval and ratio levels introduced by Stevens [1946], for dimensions, could also be interesting for other problems such as more automated visualisation of statistical datasets (cf. [Thellmann et al. 2015]).

Another QB modelling feature arising from multi-dimensional modelling techniques used on OLAP data warehouses [Kimball and Ross 2013] and not addressed by QB equations are *dimension hierarchies*. State-of-the-art OLAP data warehouses allow the definition of *aggregation operators* in the dimension specification. However, aggregation operators are not included in the QB specification [Cyganiak, Reynolds and Tennison 2014], although extensions have been proposed, for example with QB40LAP [Varga et al. 2016]. QB equations could be extended to express such numerical aggregation operations and thus relate members at different hierarchical levels.

The QB vocabulary defines several constructs to allow a more compact representation of datasets, in particular *slices* to group related observations together and *abbreviated data cubes* to avoid unnecessary redundancy in dataset representation. Exploiting these features could lead to improved materialization and query performance. If query performance could be increased by these or similar measures, even a backward-chaining implementation could become feasible (the materialisation times of the evaluation shown in Section 7.3 suggests that backward-chaining is infeasible without significant efficiency improvements).

A practical analysis of real-world QB datasets collecting reused dimension and member IRIS could unveil more real-world use case scenarios for QB equations. QB equations can be used, not only for unit conversions and computing indicators, but also for evaluating linear regression models by using QB rules (in Bischof, Martin et al. [2015a] we already trained linear regression models on Open City Data Pipeline data).

Eventually, more expressive numerical functions and methods could be necessary depending on the use case.

8.3.4 Equations and Statistical Methods Combined

Our future work includes extensions of the presented datasets, methods and the system itself.

Currently, the data sources are strongly focused on European cities or demographic data. Hence, we intend to integrate further national and international data sources, in particular the US Census Bureau statistics and the Carbon Disclosure Project.

The US Census Bureau [U.S. Census Bureau 2007] offers two groups of tabular datasets concerning US statistics: *Table C-1 to C-6* of [U.S. Census Bureau 2007] cover the topics Area and Population, Crime and Civilian Labour Force for cities larger than 20 000 inhabitants; *Table D-1 to D-6* of [U.S. Census Bureau 2007] cover Population, Education, Income and Poverty for locations with 100 000 inhabitants and more. Contrary to the UNdata or Eurostat datasets, the US Census Bureau datasets have a low ratio of missing values ranging from 0% to 5% for a total of 1267 cities. The data includes 21 indicators, e.g., population, crime, and unemployment rate.

The Carbon Disclosure Project (CDP) is an organisation based in the UK aiming at "using the power of measurement and information disclosure to improve the management of environmental risk".¹ The *CDP cities* project has data collected on more than 200 cities worldwide. CDP cities offers a reporting platform for city governments using an online questionnaire covering climate-related areas like Emissions, Governance, Climate risks, Opportunities, and Strategies.

In addition to the above, many cities operate dedicated open data portals. The data from these individual city open data portals (e.g., New York, Vienna) could be added and integrated. However, a significant effort would be involved, as we would require a unified interface to many data portals. Either we would have to write wrappers for every city's portal, or standardisation efforts on how cities publish data would have to succeed.

Apart from that, we could include sources such as DBPEDIA or Wikidata

1 https://www.cdp.net/en-US/Pages/About-Us.aspx [Vrandečić and Krötzsch 2014] in a more timely fashion, for example by recording changes of values, through projects such as the DBPEDIA wayback machine [Fernández, Schneider and Umbrich 2015], to also collect historical data from DBPEDIA.

Compared to [Bischof, Martin et al. 2015a] we completely refurbished our crawling framework and architecture to automatically and regularly update the integrated sources dynamically. We therefore expect new lessons learnt from more regular updates; e.g.; Eurostat only recently updates its datasets monthly, instead of annually,² which we expect to benefit from.

We also plan to connect our platform to the Linked Geo Data Knowledge Base [Stadler et al. 2012] including OpenStreetMap (OSM) data. Based on such data, new indicators could be directly calculated, e.g., the size of public green space by aggregating all the parks and public green areas tagged respectively in OSM. Some preliminary works on integrating indicators extracted from OSM with our Open City Data Pipeline have been presented by Posada-Sánchez, Bischof and Polleres [2016].

As we integrate more sources and datasets, another future direction we should pursue is to revisit cross-dataset predictions of missing values in more detail,³ i.e., how predictions can be made from one data source to another. This is particularly important, as typically different data sources have only a handful (if any) overlapping indicators.

Furthermore, the integration of entities of different dimensions is an interesting research topic. For example, although it seems spatial entities are well defined, it turns out that different data providers use different definitions; for example city boundaries for cities, inner city, metropolitan area or larger urban zone/functional urban area [Office for Official Publications of the European Communities 2004]. Prominent examples for such differentlydefined cities are Paris, London or Brussels. This similarly applies to indicator definitions. While there exists a shared definition of basic indicators such as resident population or area of a country or city, the same is not true for many other basic or computed indicators. Economic indicators highlight this problem well: statistical offices define their own variant to measure economic impact or living standards between countries (and cities). For example the gross domestic product (GDP) can be computed using different approaches and can depend on differently collected data (see Coyle [2014] on history and development of the GDP). In Bischof, Martin et al. [2015a] we tested robust linear regression to find similar indicators in different datasets. Although these preliminary results were promising, more data and possibly more elaborate methods are needed for high quality indicator mappings between datasets.

We further aim to extend our suite of base regression methods with other well established methods. Promising candidates are Support Vector Machines [Sánchez A 2003], Neural Networks, and Bayesian Generalised Linear Models [West, Harrison and Migon 1985].

Moreover, we plan to publish more detail on the best regression methods

2 cf. Section 8.1 at http://ec.europa.eu/eurostat/cache/ metadata/de/urb_esms.htm: "From 2017 new data will be published the first day of every month."

3 Some preliminary work along these lines have been presented by Bischof, Martin et al. [2015a].

Property	Triples	Property	Triples
dbo:birthPlace	836 321	dbo:populationPlace	4 308
dbo:country	734 006	dbo:crosses	3 544
dbo:deathPlace	289 630	dbo:museum	3 2 3 5
dbo:location	245 009	dbo:countySeat	2 986
dbo:nationality	126 855	dbo:hubAirport	2 277
dbo:city	87 306	dbo:homeport	1 861
dbo:region	65 026	dbo:targetAirport	1 271
dbo:hometown	54 520	dbo:sourceRegion	1 193
dbo:residence	46 689	dbo:nationalAffiliation	1 1 2 0
dbo:state	42 580	dbo:placeOfBurial	1 100
dbo:stateOfOrigin	37 532	dbo:mouthRegion	1 009
dbo:headquarter	27 317	dbo:areaOfSearch	798
dbo:locatedInArea	24 161	dbo:mouthCountry	671
dbo:locationCountry	21074	dbo:europeanAffiliation	614
dbo:locationCity	20 868	dbo:restingPlacePosition	538
dbo:restingPlace	16 806	dbo:borough	325
dbo:broadcastArea	15 374	dbo:sourceConfluencePosition	245
dbo:place	13 571	dbo:wineRegion	205
dbo:mouthPlace	13 468	dbo:sourceConfluencePlace	188
dbo:mouthMountain	13 468	dbo:ruralMunicipality	177
dbo:sourceCountry	12 092	dbo:bodyDiscovered	143
dbo:mouthPosition	9 948	dbo:map	115
dbo:arrondissement	9 434	dbo:beltwayCity	72
dbo:county	8 879	dbo:capitalPosition	67
dbo:canton	8 802	dbo:sourceConfluenceRegion	44
dbo:foundationPlace	8 348	dbo:sourceConfluenceState	31
dbo:spokenIn	7 828	dbo:geneLocation	4
dbo:garrison	7 2 7 2	dbo:capitalRegion	3
dbo:campus	6 7 1 1	dbo:capitalCountry	2
dbo:sourceMountain	5 5 1 5	dbo:capitalMountain	1
dbo:sourcePlace	5 5 1 5	dbo:capitalPlace	1
dbo:sourcePosition	4 535		

 Table 8.1: List of the subproperties of dul:hasLocation used by DBPEDIA, ordered descending by number of triples

per indicator as part of our ontology: so far, we only indicate the method and NRMSE, whereas further details such as parameters used and regression models would be needed to reproduce and optimise our predictions. Ontologies such as DMOP [Keet et al. 2015] could serve as a starting point.

Furthermore, we are in the process of improving the user interface to make the Web application easier to use. For this we investigate several libraries for more advanced information visualisation.

8.3.5 Combining Schema-Agnostic Rewriting with Equations

We now discuss the combination of schema-agnostic rewriting with either RDF attribute equations or QB equations.

Combination with RDF attribute equations DBPEDIA defines 85 properties to relate individuals, to spatial entities: for example dbo:country is used to relate cities to their containing countries, or dbo:birthPlace relates persons to their birth place; see Table 8.1 for a list the 83 properties used by DBPEDIA. All of these 85 DBPEDIA properties are subproperties of the external property dul:hasLocation of the "DOLCE+DnS Ultralite" ontology.⁴ It would be desirable to use this general dul:hasLocation property instead of the 85 more specific DBPEDIA properties to find the location of a spatial entity. However, the DBPEDIA dataset does not contain the materialized triples for the superproperty dul:hasLocation. A combination of schema-agnostic rewriting with RDF Attribute equations would make queries like the following possible: "Get the population density of each populated place located in Austria. Use equational knowledge if possible." The corresponding SPARQL query could look like the following:

```
SELECT ?place ?popdens
WHERE {
    ?place rdf:type dbo:PopulatedPlace;
    dbo:populationDensity ?popdens;
    dul:hasLocation dbr:Austria .
}
```

Getting the intended results for this query would indeed be possible, with the contributions presented in this thesis, by a three step approach:

- 1. Apply the RDF attribute equations rewriting on the SPARQL query (using the same example RDF attribute equation for population density used previously in Chapter 4).
- 2. Apply the schema-agnostic query rewriting on the result of step 1.
- 3. Evaluate the query of step 2 on the DBPEDIA SPARQL endpoint.

However, the resulting query would be long and complex (in terms of the length and number of property path expressions).

A similar query, which might not be completely answerable by DBPEDIA alone, could be for example "Give me the unemployment rate of all us cities with a democratic (or republic) mayor". We see that this type of analytical query is hard to answer completely, but can be very interesting for different types of users. Therefore, a more integrated approach for effectively using ontological and equational knowledge would be desirable.

Combination with QB Equations The generalised combination of schemaagnostic rewriting with QB equations poses different *additional* challenges in terms of an actual implementation. Schema-agnostic rewriting can naively be combined with QB equations with two differences when compared to RDF attribute equations:

1. The data "entailed" by QB equations are (physically) materialized and not derived during query evaluation. Therefore, the QB observations and the

4 http: //www.ontologydesignpatterns.org/ ont/dul/DUL.owl 146

other background data, for example from DBPEDIA, must either be stored in one triple store or SPARQL federated queries (not discussed in this thesis) must be used.

2. Because of materialization, the rewritten queries would often be shorter than the queries generated by RDF attribute equations. However, we have to pay a price for the more expressive data modelling features provided by the QB vocabulary: QB datasets are harder to index by (general) triple store than datatype properties, leading to potentially slower query response times.

Addressing the first challenge means moving more data to a central location, or using federated queries. Both alternatives might incur other problems such as synchronizing updates or further performance hits. The second challenge could partly be alleviated by splitting the data between a special-purpose engine tailored to handle multi-dimensional data, and a triple store for the background knowledge. Also, in this case, a more integrated approach could be beneficial to query response times.

ALL THESE ASPECTS will impose further challenges when addressed in detail. The experiences in this thesis have shown that many of these practical challenges also mean hitting limitations of existing SPARQL engines. We leave them to others to explore, confident that the present thesis has opened the door for various further investigations and follow-up works.

es **e**s **e**s

IN THE END we can only hope to have *aided* satisfying our hunger for knowledge and *trust* we do not drown in the flood of information.

PART V

APPENDICES

RDF Prefixes



In the following table we list the used prefixes and corresponding IRIS.

Prefix	IRI
cd:	http://citydata.wu.ac.at/ns#
cdmv:	http://citydata.wu.ac.at/MV-Predictions/
dbr:	http://dbpedia.org/resource/
dbo:	http://dbpedia.org/ontology/
dcterms:	http://purl.org/dc/terms/
dul:	http://www.ontologydesignpatterns.org/ont/dul/DUL.owl#
ee:	http://citydata.wu.ac.at/ocdp/eurostat-rules
estatwrap:	http://ontologycentral.com/2009/01/eurostat/ns#
eurostat:	http://estatwrap.ontologycentral.com/
foaf:	http://xmlns.com/foaf/0.1/
mexa:	http://mex.aksw.org/mex-algo#
mexc:	http://mex.aksw.org/mex-core#
mexp:	http://mex.aksw.org/mex-perf/
owl:	http://www.w3.org/2002/07/owl#
prov:	http://www.w3.org/ns/prov#
qb:	http://purl.org/linked-data/cube#
qbe:	http://citydata.wu.ac.at/qb-equations#
rdf:	http://www.w3.org/1999/02/22-rdf-syntax-ns#
rdfs:	http://www.w3.org/2000/01/rdf-schema#
sdmx-dimension:	http://purl.org/linked-data/sdmx/2009/dimension#
sdmx-measure:	http://purl.org/linked-data/sdmx/2009/measure#

B

Data Conversion, Linking and Integration

We now explain our approach for data conversion, linking and integration used in the Open City Data Pipeline workflow as steps (1), (2) and (3) (see Chapter 5). The approach is modular and extensible in the sense that every new data source can be prepared for consideration separately and independently from other sources. The data integration pipeline can be re-run at any time and thus allow for up-to-date data. Parts of this chapter have been published as Bischof, Harth et al. [2017].

The approach consists of the following components: Appendix B.1 introduces Linked Data wrappers that publish numerical data from various data sources as Statistical Linked Data. Appendix B.2 describes semi-automatically generated links between Statistical Linked Data from different sources. Appendix B.3 explains a rule-based Linked Data crawler to collect the relevant data and creates the unified view (see Section 5.3).

B.1 Statistical Linked Data Wrappers

We use Linked Data as an interface to access and represent relevant data sources (e.g., Eurostat or UNSD), which are originally published in tabular form. The uniform Linked Data interface hides the specialities and structure of the original data source. When the wrapper receives an HTTP request for a particular dataset, it retrieves the data on-the-fly from the original source, transforms the tabular representation to RDF, using the RDF Data Cube vocabulary, and returns the RDF representation of the original tabular data.

The wrappers provide a table of contents with links to all available datasets (as a collection of qb:DataSet triples), including the data structure definition of the datasets (as qb:DataStructureDefinition). The individual data points are modelled as observations (as qb:Observation). The data structure definition includes the available dimensions (as qb:dimension) and concept schemes (as skos:ConceptScheme). We require a list of dataset and data structure definitions to be able to crawl the data.

Each wrapper coins IRIS for identifying the relevant resources, for example, indicators or locations. We use IRIS as unique identifiers for datasets, dimensions and dimension values from different data sources.

The data sources identify indicators differently. For example, UNSD pro-

vides population numbers in dataset "240", while Eurostat provides population numbers in dataset "urb_cpop1". We use the City Data Ontology to unify the various indicator identifiers. Similarly, locations have varying identifiers and sometimes varying names in the different data sources. For a relatively clear-cut example consider the city of Vienna: UNSD uses city code 001170 and label WIEN, whereas Eurostat uses code AT001C1 and label Wien. The wrappers generate an IRI for every city out of the unique identifiers in the original tabular data.

We use the following wrappers which provide access to the underlying data source via a Linked Data interface:

Eurostat Wrapper The Eurostat wrapper¹ makes the Eurostat datasets, originally available in tabular form at the Eurostat website, available as Linked Data. Eurostat provides several dictionary files in sDMX format; these files are used to construct a list of dimension values in the data structure definition and to generate IRIS for relevant entities (such as cities). All files are accessed from the original Eurostat server once the wrapper receives a HTTP request on the particular IRI, ensuring that the provided RDF data is up-to-date. Population data in the Eurostat wrapper² uses http://estatwrap.ontologycentral.com/ dic/indic_ur#DE1001V to identify "Population on the 1st of January, total". The indicator IRI is mapped to indicator IRIS from the City Data Ontology in a subsequent step.

UNSD Wrapper The UNSD wrapper³ makes the UNSD datasets, originally available in tabular form at the UNSD website, available as Linked Data. The UNSD wrapper provides a simple data structure definition describing the available dimensions and measure. In total, we cover 14 datasets ranging from population to housing data. Most indicators, e.g., population of the "240" dataset,⁴ are directly mapped to an indicator IRI from the City Data Ontology, namely http://citydata.wu.ac.at/ns#population.

B.2 Linking and Mapping Data

We start by explaining the required mappings for dimension IRIS, followed by explaining the required mappings for dimension value IRIS. In general, the data from the UNSD wrapper, due to the simpler representation in the original data source, requires less mappings than the data from the Eurostat wrapper.

The two data sources exhibit the three dimensions for dcterms:date (year), sdmx-dimension: refArea (city) and cd:hasIndicator (indicator). We map the following dimension IRIS of the global cube using rdfs:subPropertyOf:

 For the time dimension our wrappers directly use dcterms:date. The time dimension hence does not require any further mapping.

2 http://estatwrap.ontologycentral. com/id/urb_cpop1

//estatwrap.ontologycentral.com/

3 http://citydata.wu.ac.at/Linked-UNData/

4 http://citydata.wu.ac.at/Linked-UNData/data/240

1 http:

- For the geospatial dimension the UNSD wrapper uses sdmx-dimension:ref-Area. The Eurostat wrapper uses different representations for the geospatial dimension, such as eurostat:geo, eurostat:cities and eurostat:metroreg, which we link to sdmx-dimension:refArea.
- For the indicator dimension we use cd:hasIndicator. Again, the UNSD wrapper directly uses that IRI, while the data from the Eurostat wrapper requires links from eurostat:indic_na and eurostat:indic_ur to cd:hasIndicator.

The Eurostat site provides a quite elaborate modelling of dimensions, code lists and so on in SDMS files. The datasets from the Eurostat wrapper use various units such as :THS denoting "Thousand" and :COUNT denoting that the number was computed from a count operation. However, all other dimensions of datasets from Eurostat we consider in the pipeline, exhibit only one single possible dimension value (e.g., :THS), besides the three canonical dimensions of the global cube. Hence, we can assume that all other dimensions and their values are part of the indicator.

The UNSD site has a simpler structure than Eurostat. The modelling of different dimensions and code lists is less elaborate. Thus, for the UNSD wrapper, we have ensured on the level of the published RDF that each dataset only provides the canonical dimensions.

The two wrappers use different IRIS for the same dimensions, for example eurostat:geo and sdmx-dimension:refArea. The wrappers also use different IRIS for the same dimension values:

- For the time dimension values we use single years represented as String values such as "2015".
- For the geospatial dimension values we link to DBpedia IRIS from other representations such as http://estatwrap.ontologycentral.com/dic/cities#AT001C1 and http://citydata.wu.ac.at/resource/40/001170#000001.
- For the indicator dimension values we link to instances of cd:Indicator, such as cd:population and cd:population_male. The UNSD wrapper directly uses these values. For the IRIS used in the data from the Eurostat wrapper, we link to instances of cd:Indicator.

We now describe how we generated these links to map data from different sources to the canonical representation, starting with the dimension and dimension value IRIS. We manually created the rdfs:subPropertyOf triples connecting the Eurostat dimension IRIS with our canonical IRIS, and semi-automatically generated the indicator IRIS from an Excel sheet provided by Eurostat. We then created an RDF document with links from the newly generated IRIS to the IRIS of the Eurostat wrapper. We manually adapted the UNSD wrapper to use the newly generate IRIS as indicator IRIS.

We choose to have a one-to-one (functional) mapping of every city from our namespace to the English DBpedia IRI, which in our re-published data is encoded by owl:sameAs relations. We identify the matching DBpedia IRIs for multilingual city names and apply basic entity recognition, similar to Paulheim and Fürnkranz [2012], with three steps using the city names from UNSD data:

- Accessing the DBpedia resource directly and following possible redirects.
- Using the Geonames API⁵ to identify the resource.
- For the remaining cities, manually looked up the IRI on DBpedia.

The mappings of geospatial IRIS from the Eurostat wrapper were done in a similar fashion. All the mappings are published online as RDF documents that are accessed during the crawling step.

B.3 Data Crawling and Integration

The overall RDF graph can be published and partitioned in different documents. Thus, to access the relevant RDF documents, the system has to resolve the IRIS of entities related to the dataset. Related entities are all instances of QB-defined concepts that can be reached from the dataset IRI via QB-defined properties. For example, from the IRI of a qb:DataSet instance, the instance of qb:DataStructureDefinition can be reached via qb:structure. Similarly, instances of qb:ComponentProperty (dimensions/measures) and skos:Concept (members) can be reached via links.

Once all numeric data is available as Linked Data, we need to make sure to collect all relevant data and metadata starting from a list of initial IRIS. First, the input to the crawling is a seed list of IRIS of instances of qb:DataSets. One example of a "registry" or "seed list" of dataset IRIS is provided by the PlanetData wiki.⁶ A seed list of such datasets is published as RDF and considered as input to the crawling. We use two such seed lists: one with links to the relevant instances of qb:DataSet from the UNSD wrapper, and another one with links to the relevant instances of qb:DataSet from the Eurostat wrapper.

Then, Linked Data crawlers apply crawling strategies for RDF data where they resolve the IRIS in the seed list to collect further RDF and in turn resolve a specific (sub-)set of contained IRIS. An example Linked Data crawler is LD-Spider [Isele et al. 2010], which uses a depth-first or breadth-first crawling strategy for RDF data. Linked Data crawlers typically follow links without considering the type.

A more directed approach would apply a crawling strategy that starts with resolving and loading the IRIS of qb:DataSets relevant for the task, and then in turn resolves and loads instances of QB concepts that can be reached from the dataset IRIS.

To specify how to collect Linked Data, we use the Linked Data-Fu language [Stadtmüller et al. 2013] in which rule-based link traversal can be specified. For instance, to retrieve data from all qb:DataSets, we define the following rule:

6 http://wiki.planetdata.eu/web/Datasets

154

```
{
    ?ds rdf:type qb:DataSet.
} =>
{
    [] http:mthd httpm:GET.
    http:request\ iri ?ds .
} .
```

The head of a rule corresponds to an update function of an internal graph representation in that it describes an HTTP method that is to be applied to a resource. In our example, the head of a rule applies a HTTP GET method to the resource ?ds. The body of a rule corresponds to the condition in terms of triple patterns that have to hold in the internal graph representation. In our example, ?ds is defined as an instance of qb:DataSet.

Similarly, we retrieve instances of qb:DataStructureDefinition, qb:ComponentSpecification, qb:DimensionProperty, qb:AttributeProperty, qb:MeasureProperty, qb:Slice, qb:SliceKey and qb:ObservationGroup. Also, we access the list of possible dimension values (based on qb:codeList in data structure definitions) as well as each single dimension value. The only instances we do not resolve are observations, since these are usually either modelled as blank nodes or provided together with other relevant information with the RDF document containing qb:DataSet or qb:Slice.

Crawling may include further information, e.g., rdfs:seeAlso links from relevant entities or owl:sameAs links to equivalent IRIS. Assuming that the number of related instances of QB concepts starting from a QB dataset is limited and that links such as rdfs:seeAlso for further information are not crawled without restriction (e.g., only from instances of QB concepts), the directed crawling strategy terminates after a finite amount of steps.

As well as all the relevant data and metadata of qb:DataSets, we collect the following further information:

- The City Data Ontology⁷ (CDP ontology) that contains lists of common statistical indicators about cities.
- The QB equations ontology⁸ that contains the vocabulary to describe QB equations and is further detailed in Chapter 6.
- The Eurostat QB equations⁹ that contains a set of QB equations generated from formulas published by Eurostat as further detailed in Chapter 6.
- Background information¹⁰ that links indicators of Estatwrap to the CDP ontology.
- Background information providing additional owl:equivalentProperty links¹¹ between common dimensions not already provided by the wrappers such as between the different indicator dimension IRIS estatwrap:indic_ur, cd:has-Indicator and eurostat:indic_na.

Besides explicit information available in the RDF sources, we also materialise implicit information to: (i) make querying over the triple store easier and (ii) automatically evaluate relevant QB and OWL semantics. We execute the 7 http://citydata.wu.ac.at/ns

8 http://citydata.wu.ac.at/ocdp/qb-equations

9 http://citydata.wu.ac.at/ocdp/ eurostat-equations

10 http://kalmar32.fzi.de/triples/ indicator-eurostat-links.nt

11 http://kalmar32.fzi.de/triples/ dimension-property-links.nt 12 https://www.w3.org/TR/vocabdata-cube/#normalize-algorithm13 http://semanticweb.org/OWLLD/ QB normalisation algorithm¹² in case the datasets are abbreviated. Also, we execute entailment rules¹³ for OWL and RDFS. However, we only enable those normalisation and entailment rules that we expect to be evaluated quickly and to provide sufficient benefit for querying.

For instance, we evaluate rules about the semantics of equality, e.g., symmetry and transitivity of owl:sameAs. We again describe the semantics of such axioms using Linked Data-Fu. However, because we do not need the full materialisation of the equality, but only the canonical IRIS, we define custom rules that only generate the triples involving the canonical IRIS. Thus, the resulting dataset contains all the triples required to integrate and query the canonical representation, but not more.

The crawling and integration is specified in several Linked Data-Fu programs. The programs are executed periodically using the Linked Data-Fu interpreter¹⁴ in version 0.9.12. The interpreter issues HTTP requests to access the seed list, follows references to linked IRIS, and applies the derivation rules to materialise the inferences. The crawled and integrated data is then made available for loading into a triple store. Before loading the observations into the triple store we ensure for each observation that the correct dimension IRIS and member IRIS are used, filter out non-numeric observation values and mint a new observation IRI if a blank node is used. Finally, the filtered and skolemised observations are loaded into an OpenLink Virtuoso triple store (vo7) using the standard RDF bulk loading feature¹⁵.

14 https://linked-data-fu.github.io/

15 See http://citydata.wu.ac.at/ocdp/import for a collection of information about the loading process.

C

Complete Example of QB Equation Steps

An excerpt of the Eurostat indicator QB equations¹ in Turtle syntax as example for a QB equation: the Eurostat indicator definition for "Women per 100 men" is represented as a QB equation as follows:

<http:// citydata.wu.ac.at/ocdp/eurostat-equations#women_per_100_men> a qbe:Equation ;

1 http://citydata.wu.ac.at/ocdp/ eurostat-equations

qbe:variable [a qbe:ObsSpecification ; qbe: filter [a qbe:DimSpecification ; gb:dimension cd:hasIndicator ; qbe:value cd:women_per_100_men]; qbe:variablename "?women_per_100_men"^^qbe:variableType]; gbe:variable [a gbe:ObsSpecification ; gbe: filter [a gbe:DimSpecification ; qb:dimension cd:hasIndicator ; gbe:value cd:population_male]; qbe:variablename "?population_male"^^qbe:variableType] ; qbe:variable [a qbe:ObsSpecification ; qbe: filter [a qbe:DimSpecification ; qb:dimension cd:hasIndicator ; qbe:value cd:population_female]; qbe:variablename "?population_female"^^qbe:variableType] ; qbe:hasEquation "?women_per_100_men = ?population_female * 100 / ?population_male"^^ qbe:equationType.

In the first step this equation is normalised to the following three QB rules.²

```
ee:e4bb866b19a383a5c7ce88e853ff8bdad a qbe:Rule;
  prov:wasDerivedFrom <http://citydata.wu.ac.at/ocdp/eurostat-equations#
       women_per_100_men>;
  qbe:structure globalcube:global-cube-dsd;
  qbe:output [
    qbe: filter _:b4bb866b19a383a5c7ce88e853ff8bdad ];
  qbe:input [ qbe:variableName "?women_per_100_men"^^qbe:variableType;
    qbe: filter _:b4c56a2955372924bde20c2944b2b28f3 ];
  qbe:input [ qbe:variableName "?population_male"^^qbe:variableType;
    qbe: filter _:b7177d26053419667c2b7deb4569a82b9 ];
  qbe:hasFunction "?population_male*?women_per_100_men/100"^^qbe:functionType .
_:b4bb866b19a383a5c7ce88e853ff8bdad gbe:dimension cd:hasIndicator ; gbe:value cd:
     population_female.
ee:e4c56a2955372924bde20c2944b2b28f3 a qbe:Rule;
  prov:wasDerivedFrom <http://citydata.wu.ac.at/ocdp/eurostat-equations#
       women_per_100_men>;
  qbe:structure globalcube:global-cube-dsd;
  qbe:input [ qbe:variableName "?population_female"^^qbe:variableType;
```

2 http://citydata.wu.ac.at/ocdp/ eurostat-rules

```
qbe: filter _:b4bb866b19a383a5c7ce88e853ff8bdad ];
  qbe:output [
   qbe: filter _:b4c56a2955372924bde20c2944b2b28f3 ];
  qbe:input [ qbe:variableName "?population_male"^^qbe:variableType ;
   qbe: filter _:b7177d26053419667c2b7deb4569a82b9 ];
  qbe:hasFunction "100*?population_female/?population_male"^^qbe:functionType .
_:b4c56a2955372924bde20c2944b2b28f3 qbe:dimension cd:hasIndicator ; qbe:value cd:
     women_per_100_men.
ee:e7177d26053419667c2b7deb4569a82b9 a gbe:Rule;
 prov:wasDerivedFrom <http://citydata.wu.ac.at/ocdp/eurostat-equations#
       women_per_100_men>;
  gbe:structure globalcube:global-cube-dsd;
  qbe:input [ qbe:variableName "?population_female"^^qbe:variableType;
   qbe: filter _:b4bb866b19a383a5c7ce88e853ff8bdad ];
  qbe:input [ qbe:variableName "?women_per_100_men"^^qbe:variableType ;
   qbe: filter _:b4c56a2955372924bde20c2944b2b28f3 ];
  qbe:output [
   qbe: filter _:b7177d26053419667c2b7deb4569a82b9 ];
  qbe:hasFunction "100*?population_female/?women_per_100_men"^^qbe:functionType .
_:b7177d26053419667c2b7deb4569a82b9 gbe:dimension cd:hasIndicator ; gbe:value cd:
```

population_male. Next, the QB rules are converted to SPARQL INSERT queries. We give here the

SPARQL query for the second QB rule above, which computes the value for the indicator women_per_100_men:

```
INSERT {
  ?obs qb:dataSet globalcube:global-cube-ds;
   cd:hasIndicator cd:women_per_100_men;
   dcterms:publisher ?source ;
   dcterms:date ?year ;
   sdmx-dimension:refArea ?city ;
   sdmx-measure:obsValue ?value ;
   prov:wasDerivedFrom ?population_male_obs, ?population_female_obs;
   prov:wasGeneratedBy?activity ;
   prov:generatedAtTime ?now ;
   cd:estimatedRMSE ?error .
  ? activity a prov: activity ;
  prov: qualifiedAssociation [
   a prov: Association ;
   prov:agent cd:import.sh ;
   prov:hadPlan <http:// citydata .wu.ac.at/ocdp/eurostat-rules#
         e4c56a2955372924bde20c2944b2b28f3>].
WHERE { { SELECT DISTINCT * WHERE {
  ?population_male_obs qb:dataSet globalcube:global-cube-ds;
   cd:hasIndicator cd:population_male;
   dcterms:date ?year;
   sdmx-dimension:refArea ?city ;
   sdmx-measure:obsValue ?population_male;
   cd:estimatedRMSE ?population_male_error .
```

?population_female_obs qb:dataSet globalcube:global-cube-ds;

```
cd: hasIndicator cd:population_female ;
dcterms:date ?year;
sdmx-dimension:refArea ?city ;
sdmx-measure:obsValue ?population_female ;
cd:estimatedRMSE ?population_female_error .
```

```
BIND(CONCAT(REPLACE("http://citydata.wu.ac.at/ocdp/eurostat-rules#
e4c56a2955372924bde20c2944b2b28f3", "e4c56a2955372924bde20c2944b2b28f3", MD5
(CONCAT("http://citydata.wu.ac.at/ocdp/eurostat-rules#
e4c56a2955372924bde20c2944b2b28f3",STR(?population_male_obs), STR(?
population_female_obs))))) AS ?skolem)
BIND(IRI (CONCAT(?skolem, "_source")) AS ?source)
BIND(IRI (CONCAT(?skolem, "_obs")) AS ?obs)
BIND(IRI (CONCAT(?skolem, "_activity")) AS ? activity )
BIND(NOW() as ?now)
```

```
## computation and variable assignment
```

```
BIND(100.0*?population_female*1.0/IF (?population_male != 0, ?population_male, "err") AS 
?value)
```

```
## error propagation
```

```
BIND((ABS(100.0)+0.0)*(ABS(?population_female)+?population_female_error)*1.0/IF ((ABS(?population_male)-?population_male_error)!=0.0, (ABS(?population_male)-?population_male_error), "err")-100.0*?population_female*1.0/IF(?population_male!=
0, ?population_male, "err") + 0.1 as ?error)
```

FILTER(?error > 0.0)

```
## 1st termination condition:
## there exists no better observation with the same dimension values
FILTER NOT EXISTS {
    ?obsa qb:dataSet globalcube:global-cube-ds;
```

```
dcterms:date ?year;
sdmx-dimension:refArea ?city ;
cd:hasIndicator cd:women_per_100_men;
sdmx-dimension:sex ?sex ;
estatwrap:unit ?unit ;
sdmx-dimension:age ?age ;
cd:estimatedRMSE ?errora .
FILTER(?errora < ?error) }</pre>
```

2nd termination condition:

the same equation was not used for the computation of any source observation

- FILTER NOT EXISTS { ?population_male_obs prov:wasDerivedFrom*/prov:wasGeneratedBy/ prov:qualifiedAssociation/prov:hadPlan/prov:wasDerivedFrom? http://citydata.wu.ac. at/ocdp/eurostat-rules#e4c56a2955372924bde20c2944b2b28f3>. }
- FILTER NOT EXISTS { ?population_female_obs prov:wasDerivedFrom*/prov:wasGeneratedBy/ prov:qualifiedAssociation/prov:hadPlan/prov:wasDerivedFrom? http://citydata.wu.ac at/ocdp/eurostat-rules#e4c56a2955372924bde20c2944b2b28f3>. }

Bibliography

- Abdel Kader, Riham, Peter Boncz, Stefan Manegold and Maurice van Keulen (2009). "ROX: Run-time Optimization of XQueries". In: *Proceedings of the 2009 ACM SIGMOD International Conference on Management of Data (SIGMOD'09)*, pages 615–626. DOI: 10.1145/1559845.1559910 (cited on page 57).
- Abele, Andrejs, John P. McCrae, Paul Buitelaar, Anja Jentzsch and Richard Cyganiak (2017). *Linking Open Data cloud diagram*. URL: http://lod-cloud.net/ (visited on 12th Oct. 2017) (cited on page 23).
- Abiteboul, Serge, Richard Hull and Victor Vianu (1994). *Foundations of Databases*. Addison Wesley (cited on page 45).
- Alkhateeb, Faisal (2008). "Querying RDF(S) with Regular Expressions". Available at https://tel.archives-ouver tes.fr/tel-00293206. PhD thesis. Université Joseph Fourier Grenoble 1 (cited on page 135).
- Ambite, José Luis and Dipsy Kapoor (2007). "Automatically Composing Data Workflows with Relational Descriptions and Shim Services". In: *Proceedings of the 6th International Semantic Web Conference (ISWC'07)*. Volume 4825. Lecture Notes in Computer Science, pages 15–29. DOI: 10.1007/978-3-540-76298-0_2 (cited on page 131).
- Angles, Renzo and Claudio Gutierrez (2008). "The Expressive Power of SPARQL ". In: *Proceedings of the 7th International Semantic Web Conference (ISWC'08)*. Volume 5318. Lecture Notes in Computer Science, pages 114–129. DOI: 0.1007/978-3-540-88564-1_8 (cited on page 102).
- Apache Jena, editor (2017[a]). A Free and Open Source Java Framework for Building Semantic Web and Linked Data Applications. URL: http://jena.apache.org/ (visited on 12th Oct. 2017) (cited on page 55).
- (2017[b]). Reasoners and Rule Engines: Jena Inference Support. URL: https://jena.apache.org/documentation /inference/ (visited on 12th Oct. 2017) (cited on page 75).
- Arenas, Marcelo, Elena Botoeva, Diego Calvanese, Vladislav Ryzhikov and Evgeny Sherkhonov (2012). "Representability in DL-Lite_R Knowledge Base Exchange". In: *Proceedings of the 25th International Workshop on Description Logics (DL'12)*. CEUR Workshop Proceedings 846. URL: http://ceur-ws.org/Vol-846/paper_60.pdf (cited on page 68).
- Artale, Alessandro, Diego Calvanese, Roman Kontchakov and Michael Zakharyaschev (2009). "The DL-Lite Family and Relations". In: *Journal of Artificial Intelligence Research* 36.1, pages 1–69 (cited on page 20).
- Auer, Sören, Lorenz Bühmann, Christian Dirschl, Orri Erling, Michael Hausenblas, Robert Isele, Jens Lehmann, Michael Martin, Pablo N. Mendes, Bert Van Nuffelen, Claus Stadler, Sebastian Tramp and Hugh Williams (2012). "Managing the Life-Cycle of Linked Data with the LOD2 Stack". In: *Proceedings of the 11th International Semantic Web Conference (ISWC'12)*. Volume 7649. Lecture Notes in Computer Science, pages 1–16. DOI: 10.1007/978-3-642-35173-0_1 (cited on page 130).

- Baader, Franz, Diego Calvanese, Deborah McGuinness, Daniele Nardi and Peter Patel-Schneider, editors (2007). *The Description Logic Handbook: Theory, Implementation, and Applications*. 2nd edition. Cambridge University Press (cited on pages 18, 22, 110).
- Baader, Franz, Ian Horrocks, Carsten Lutz and Uli Sattler (2017). *An Introduction to Description Logic*. Cambridge University Press. DOI: 10.1017/9781139025355. URL: http://dltextbook.org/ (cited on pages 18, 22).
- Beckett, David, Tim Berners-Lee, Eric Prud'hommeaux and Gavin Carothers, editors (2014). *RDF 1.1 Turtle*. Available at https://www.w3.org/TR/turtle/. W3C Recommendation (cited on page 12).
- Berners-Lee, Tim (1989). *Information Management: A Proposal*. URL: https://www.w3.org/History/1989/proposal .html (visited on 10th Oct. 2017) (cited on page 3).
- (2006). Linked Data. URL: https://www.w3.org/DesignIssues/LinkedData.html (visited on 10th Oct. 2017)
 (cited on pages 3, 22, 130).
- Berners-Lee, Tim, James Hendler and Ora Lassila (2001). "The Semantic Web". In: *Scientific American*, pages 96–101 (cited on page 3).
- Bernstein, Abraham, James Hendler and Natalya Noy (2016). "A New Look at the Semantic Web". In: *Communications of the ACM* 59.9, pages 35–37. ISSN: 0001-0782. DOI: 10.1145/2890489 (cited on page 3).
- Bettencourt, Luís M. A., José Lobo, Dirk Helbing, Christian Kühnert and Geoffrey B. West (2007). "Growth, Innovation, Scaling, and the Pace of Life in Cities". In: *Proceedings of the National Academy of Sciences of the United States of America* 104.17, pages 7301–7306. DOI: 10.1073/pnas.0610172104 (cited on page 85).
- Bevington, Philip R. and D. Keith Robinson (2003). *Data Reduction and Error Analysis for the Physical Sciences*. 3rd edition. McGraw-Hill (cited on page 105).
- Bienvenu, Meghyn, Diego Calvanese, Magdalena Ortiz and Mantas Šimkus (2014). "Nested Regular Path Queries in Description Logics". In: arXiv: 1402.7122 [cs.L0] (cited on page 44).
- Bienvenu, Meghyn and Magdalena Ortiz (2015). "Ontology-Mediated Query Answering with Data-Tractable Description Logics". In: *Reasoning Web International Summer School (RW'15)*. Volume 9203. Lecture Notes in Computer Science, pages 218–307. DOI: 10.1007/978-3-319-21768-0_9 (cited on pages 5, 22).
- Birbeck, Mark and Shane McCarron, editors (2010). *CURIE Syntax 1.0*. Available at https://www.w3.org/TR/cur ie/. W3C Working Group Note (cited on page 12).
- Bischof, Stefan, Stefan Decker, Thomas Krennwallner, Nuno Lopes and Axel Polleres (2012). "Mapping between RDF and XML with XSPARQL". In: *Journal on Data Semantics* 1.3, pages 147–185. DOI: 10.1007/s13740-012-0008-7 (cited on page 108).
- Bischof, Stefan, Andreas Harth, Benedikt Kämpgen, Axel Polleres and Patrik Schneider (2017). "Enriching Integrated Statistical Open City Data by Combining Equational Knowledge and Missing Value Imputation".
 In: *Journal of Web Semantics: Special Issue on Semantic Statistics*. Preprint available at http://www.websem anticsjournal.org/index.php/ps/article/view/509. DOI: 10.1016/j.websem.2017.09.003 (cited on pages 8, 83, 95, 113, 151).
- Bischof, Stefan, Markus Krötzsch, Axel Polleres and Sebastian Rudolph (2014a). "Schema-Agnostic Query Rewriting in SPARQL 1.1". In: *Proceedings of the 13th International Semantic Web Conference (ISWC'14)*. Volume 8796. Lecture Notes in Computer Science, pages 584–600. DOI: 10.1007/978-3-319-11964-9_37 (cited on pages 7, 29, 32, 44, 45).
- (2014b). Schema-Agnostic Query Rewriting in SPARQL 1.1: Technical report. Available at http://stefanbisch of.at/publications/iswc14/ (cited on page 29).
- (2015). "Schema-Agnostic Query Rewriting for OWL QL". In: Proceedings of the 28th International Workshop on Description Logics (DL'15). CEUR Workshop Proceedings 1350. URL: http://ceur-ws.org/Vol-1350/pa per-12.pdf (cited on page 7).

- (2017). "Schema-Agnostic Query Rewriting in SPARQL 1.1". In preparation (cited on page 7).

- Bischof, Stefan, Christoph Martin, Axel Polleres and Patrik Schneider (2015a). "Collecting, Integrating, Enriching and Republishing Open City Data as Linked Data". In: *Proceedings of the 14th International Semantic Web Conference (ISWC'15) Part II*. Volume 9367. Lecture Notes in Computer Science, pages 57–75. DOI: 10.1007/978-3-319-25010-6_4 (cited on pages 8, 83, 85, 87, 113, 115, 116, 119, 121, 122, 137, 142, 143).
- (2015b). "Open City Data Pipeline: Collecting, Integrating, and Predicting Open City Data". In: *Proceedings* of the 4th Workshop on Knowledge Discovery and Data Mining Meets Linked Open Data. CEUR Workshop Proceedings 1365. URL: http://ceur-ws.org/Vol-1365/paper3.pdf (cited on page 8).
- Bischof, Stefan and Axel Polleres (2013). "RDFS with Attribute Equations via SPARQL Rewriting". In: *Proceedings of the 10th ESWC (ESWC'13)*. Volume 7882. Lecture Notes in Computer Science, pages 335–350. DOI: 10.1007/978-3-642-38288-8_23 (cited on pages 7, 65, 85).
- Bischof, Stefan, Axel Polleres and Simon Sperl (2013). "City Data Pipeline A System for Making Open Data Useful for Cities". In: *Proceedings of the I-SEMANTICS 2013 Posters & Demonstrations Track*. CEUR Workshop Proceedings 1026, pages 45–49. URL: http://ceur-ws.org/Vol-1026/paper10.pdf (cited on page 76).
- Bishop, Barry and Spas Bojanov (2011). "Implementing OWL 2 RL and OWL 2 QL Rule-Sets for OWLIM". In: *Proceedings of the 8th International Workshop on OWL: Experiences and Directions (OWLED'11)*. CEUR Workshop Proceedings 796. URL: http://ceur-ws.org/Vol-796/owled2011_submission_3.pdf (cited on page 140).
- Bizer, Christian, Jens Lehmann, Georgi Kobilarov, Sören Auer, Christian Becker, Richard Cyganiak and Sebastian Hellmann (2009). "DBpedia A crystallization point for the Web of Data". In: *Journal of Web Semantics* 7.3, pages 154–165 (cited on page 12).
- Breiman, Leo (2001). "Random Forests". In: *Machine learning* 45.1, pages 5–32. DOI: 10.1023/A:1010933404324 (cited on page 116).
- Brickley, Dan and R.V. Guha, editors (2014). *RDF Schema 1.1*. Available at https://www.w3.org/TR/rdf-schema/. W₃C Recommendation (cited on pages 17, 22).
- Buhi, Eric R., Patricia Goodson and Torsten B. Neilands (2008). "Out of Sight, Not Out of Mind: Strategies for Handling Missing Data". In: *American Journal of Health Behavior* 32.1, pages 83–92. DOI: 10.5993/AJHB.32
 .1.8 (cited on page 132).
- Buswell, Stephen, Olga Caprotti, David P. Carlisle, Michael C. Dewar, Marc Gaetano and Michael Kohlhase, editors (2004). *The OpenMath Standard 2.o.* Available at http://www.openmath.org/standard/om20. The OpenMath Society (cited on page 110).
- Cabena, Peter, Pablo Hadjinian, Rolf Stadler, Jaap Verhees and Alessandro Zanasi (1998). *Discovering Data Mining: From Concept to Implementation*. Prentice-Hall. ISBN: 0-13-743980-6 (cited on page 3).
- Calì, Andrea, Diego Calvanese, Giuseppe De Giacomo and Maurizio Lenzerini (2002). "Data Integration Under Integrity Constraints". In: *Information Systems* 29.2. DOI: 10.1007/3-540-47961-9_20 (cited on page 130).
- Calì, Andrea, Georg Gottlob and Thomas Lukasiewicz (2012). "A General Datalog-based Framework for Tractable Query Answering over Ontologies". In: *Journal of Web Semantics* 14. Special Issue on Dealing with the Messiness of the Web of Data, pages 57–83. DOI: 10.1016/j.websem.2012.03.001 (cited on page 20).
- Calì, Andrea, Georg Gottlob and Andreas Pieris (2012). "Towards More Expressive Ontology Languages: The Query Answering Problem". In: *Artificial Intelligence* 193, pages 87–128. DOI: 10.1016/j.artint.2012.08.002 (cited on page 43).
- Calvanese, Diego, Giuseppe De Giacomo, Domenico Lembo, Maurizio Lenzerini, Antonella Poggi, Mariano Rodriguez-Muro and Riccardo Rosati (2009). "Ontologies and Databases: The DL-Lite Approach". In: *Reas*-

oning Web International Summer School (RW'09), pages 255–356. DOI: 10.1007/978-3-642-03754-2_7 (cited on page 22).

- Calvanese, Diego, Giuseppe De Giacomo, Domenico Lembo, Maurizio Lenzerini and Riccardo Rosati (2007). "Tractable Reasoning and Efficient Query Answering in Description Logics: The DL-Lite Family". In: *Journal of Automated Reasoning* 39.3, pages 385–429. DOI: 10.1007/s10817-007-9078-x (cited on pages 5, 18, 20, 21, 29, 43, 69, 70, 72, 140).
- Calvanese, Diego, Maurizio Lenzerini and Daniele Nardi (1998). "Description Logics for Conceptual Data Modeling". In: *Logics for Databases and Information Systems*. Springer US, pages 229–263. ISBN: 978-1-4615-5643-5. DOI: 10.1007/978-1-4615-5643-5_8 (cited on page 18).
- Carlisle, David and Patrick Ionand Robert Miner, editors (2014). *Mathematical Markup Language (MathML) Version 3.0.* 2nd edition. Available at http://www.w3.org/TR/MathML3/. W3C Recommendation (cited on pages 96, 110).
- Chekol, Melisachew Wudage, Jérôme Euzenat, Pierre Genevès and Nabil Layaïda (2012). "SPARQL Query Containment Under *SHI* Axioms". In: *Proceedings of the 26th AAAI Conference on Artificial Intelligence* (AAAI'12), pages 10–16 (cited on page 140).
- Clément de Saint-Marcq, Vianney le, Yves Deville, Christine Solnon and Pierre-Antoine Champin (2012). "Castor: A Constraint-Based SPARQL Engine with Active Filter Processing". In: *Proceedings of the 9th Extended Semantic Web Conference (ESWC'12)*. Volume 7295. Lecture Notes in Computer Science, pages 391– 405. DOI: 10.1007/978-3-642-30284-8_33 (cited on page 140).
- CloudFlower (2016). *Data Science Report 2016*. URL: http://visit.crowdflower.com/rs/416-ZBE-142/images/CrowdF lower_DataScienceReport_2016.pdf (cited on page 3).
- Coyle, Diane (2014). *GDP: A Brief but Affectionate History*. Princeton University Press. ISBN: 9780691156798 (cited on page 143).
- Cyganiak, Richard, Dave Reynolds and Jeni Tennison, editors (2014). *The RDF Data Cube Vocabulary*. Available at https://www.w3.org/TR/vocab-data-cube/. W3C Recommendation (cited on pages 7, 23–25, 84, 141).
- de Bruijn, Jos, Enrico Franconi and Sergio Tessaris (2005). "Logical Reconstruction of Normative RDF". In: *Proceedings of the OWLED 2005 Workshop on OWL: Experiences and Directions*. CEUR Workshop Proceedings 188. URL: http://ceur-ws.org/Vol-188/sub24.pdf (cited on page 45).
- de Bruijn, Jos and Stijn Heymans (2007). "Logical Foundations of (e)RDF(S): Complexity and Reasoning". In: *Proceedings of the 6th International Semantic Web Conference (ISWC'07)*. Volume 4825. Lecture Notes in Computer Science, pages 86–99. DOI: 10.1007/978-3-540-76298-0_7 (cited on pages 31, 68).
- Di Pinto, Floriana, Domenico Lembo, Maurizio Lenzerini, Riccardo Mancini, Antonella Poggi, Riccardo Rosati, Marco Ruzzi and Domenico Fabio Savo (2013). "Optimizing Query Rewriting in Ontology-Based Data Access". In: *Proceedings of the 16th International Conference on Extending Database Technology (EDBT'13)*. ACM, pages 561–572. DOI: 10.1145/2452376.2452441 (cited on page 29).
- Diamantini, Claudia, Domenico Potena and Emanuele Storti (2013). "A Logic-Based Formalization of KPIs for Virtual Enterprises". In: *Advanced Information Systems Engineering Workshops*. Volume 148. Lecture Notes in Business Information Processing. DOI: 10.1007/978-3-642-38490-5_26 (cited on page 129).
- DuCharme, Bob (2013). *Learning SPARQL: Querying and Updating with SPARQL 1.1.* 2nd edition. O'Reilly Media. ISBN: 1449371434 (cited on page 17).

- Eiter, Thomas, Giovambattista Ianni, Roman Schindlauer and Hans Tompits (2005). "A Uniform Integration of Higher-Order Reasoning and External Evaluations in Answer-Set Programming". In: *Proceedings of the 19th International Joint Conference on Artificial Intelligence (IJCAI'05)*, pages 90–96 (cited on page 99).
- Ermilov, Ivan, Jens Lehmann, Michael Martin and Sören Auer (2016). "LODStats: The Data Web Census Dataset". In: *Proceedings of the 15th International Semantic Web Conference Part II (ISWC'16)*. Volume 9982. Lecture Notes in Computer Science, pages 38–46. DOI: 10.1007/978-3-319-46547-0_5 (cited on page 23).
- Esteves, Diego, Diego Moussallem, Ciro Baron Neto, Tommaso Soru, Ricardo Usbeck, Markus Ackermann and Jens Lehmann (2015). "MEX Vocabulary: a Lightweight Interchange Format for Machine Learning Experiments". In: *Proceedings of the 11th International Conference on Semantic Systems, (SEMANTICS'15)*, pages 169–176. DOI: 10.1145/2814864.2814883 (cited on page 120).

Eurostat (2016). *Urban Europe: Statistics on Cities, Towns and Suburbs*. DOI: 10.2785/91120 (cited on page 88). Euzenat, Jérôme and Pavel Shvaiko (2013). *Ontology Matching*. 2nd edition. Springer (cited on page 137).

- Fernández, Javier D., Patrik Schneider and Jürgen Umbrich (2015). "The DBpedia Wayback Machine". In: Proceedings of the 11th International Conference on Semantic Systems, (SEMANTICS'15), pages 192–195. DOI: 10.1145/2814864.2814889 (cited on page 143).
- Frühwirth, Thom W. (2006). "Constraint handling rules: the story so far". In: Proceedings of the 8th International ACM SIGPLAN Conference on Principles and Practice of Declarative Programming (PPDP'06), pages 90– 107. DOI: /10.1007/3-540-59155-9_6 (cited on page 140).
- Gandon, Fabien and Guus Schreiber, editors (2014). *RDF 1.1 XML Syntax*. Available at http://www.w3.org/TR/r df-syntax-grammar/. W₃C Recommendation (cited on page 12).
- Gearon, Paula, Alexandre Passant and Axel Polleres, editors (2013). SPARQL 1.1 Update. Available at http://www.w3.org/TR/sparql11-update/. W3C Recommendation (cited on page 90).
- Glimm, Birte, Adian Hogan, Markus Krötzsch and Axel Polleres (2012). "OWL: Yet to arrive on the Web of Data?" In: *WWW 2012 Workshop on Linked Data on the Web*. CEUR Workshop Proceedings 937. URL: http://ceur-ws.org/Vol-937/ldow2012-paper-16.pdf (cited on pages 23, 140).
- Glimm, Birte and Chimezie Ogbuji, editors (2013). *SPARQL 1.1 Entailment Regimes*. Available at http://www.w 3.org/TR/sparql11-entailment/. W3C Recommendation (cited on pages 29, 44).
- Golfarelli, Matteo and Stefano Rizzi (2009). *Data Warehouse Design: Modern Principles and Methodologies*. McGraw-Hill (cited on page 130).
- Gottlob, Georg and Thomas Schwentick (2012). "Rewriting Ontological Queries into Small Nonrecursive Datalog Programs". In: *Proceedings of the 13th International Conference on Principles of Knowledge Representation and Reasoning (KR'12)*, pages 254–263 (cited on page 140).
- Gray, Jim, Surajit Chaudhuri, Adam Bosworth, Andrew Layman, Don Reichart, Murali Venkatrao, Frank Pellow and Hamid Pirahesh (1997). "Data Cube: A Relational Aggregation Operator Generalizing Group-By, Cross-Tab, and Sub-Totals". In: *Data Mining and Knowledge Discovery* 1.1, pages 29–53. DOI: 10.1023/A:100 9726021843 (cited on page 23).
- Guo, Yuanbo, Zhengxiang Pan and Jeff Heflin (2005). "LUBM: A benchmark for OWL knowledge base systems". In: *Journal of Web Semantics* 3.2. Selected Papers from the International Semantic Web Conference 2004, pages 158–182. DOI: 10.1016/j.websem.2005.06.005 (cited on page 56).
- Gutierrez, Claudio, Carlos Hurtado and Alberto O. Mendelzon (2004). "Foundations of Semantic Web Databases". In: *Proceedings of the 23rd Symposium on Principles of Database Systems (PODS'04)*, pages 95–106. DOI: 10.1145/1055558.1055573 (cited on pages 17, 45).

- Haarslev, Volker and Ralf Möller (2001). "RACER System Description". In: *Proceedings of the 1st International Joint Conference on Automated Reasoning (IJCAR'01)*. Volume 2083. Lecture Notes in Computer Science, pages 701–705. DOI: 10.1007/3-540-45744-5_59 (cited on pages 75, 110).
- (2003). "Description Logic Systems with Concrete Domains: Applications for the Semantic Web". In: *Proceedings of the 10th International Workshop on Knowledge Representation meets Databases (KRDB'03)*. CEUR Workshop Proceedings 79. URL: http://ceur-ws.org/Vol-79/haarslev.pdf (cited on page 75).
- Han, Jiawei (2012). *Data Mining: Concepts and Techniques*. 3rd edition. Morgan Kaufmann Publishers Inc. ISBN: 9780123814791 (cited on pages 3, 4, 115, 116).
- Harris, Steve and Andy Seaborne, editors (2013). *SPARQL 1.1 Query Language*. Available at http://www.w3.or g/TR/sparql11-query/. W₃C Recommendation (cited on pages 13, 14, 22, 29, 45, 46).
- Hastie, Trevor, Robert Tibshirani and Jerome Friedman (2009). The Elements of Statistical Learning. Data Mining, Inference, and Prediction. 2nd edition. Springer Series in Statistics. Springer. DOI: 10.1007/978-0-3 87-84858-7 (cited on page 115).
- Hausenblas, Michael, Wolfgang Halb, Yves Raimond, Lee Feigenbaum and Danny Ayers (2009). "SCOVO: Using Statistics on the Web of Data". In: *Proceedings of the 6th European Semantic Web Conference (ESWC'09)*. Volume 5554. Lecture Notes in Computer Science, pages 708–722. DOI: 10.1007/978-3-642-02121-3_52 (cited on page 131).
- Hayes, Patrick, editor (2004). *RDF Semantics*. Available at http://www.w3.org/TR/rdf-mt/. W₃C Recommendation (cited on page 67).
- Heath, Tom and Christian Bizer (2011). *Linked Data: Evolving the Web into a Global Data Space.* Synthesis Lectures on the Semantic Web. Morgan & Claypool Publishers. DOI: 10.2200/S00334ED1V01Y201102WBE001 (cited on pages 3, 25).
- Hitzler, Pascal, Markus Krötzsch, Bijan Parsia, Peter F. Patel-Schneider and Sebastian Rudolph, editors (2009). *OWL 2 Web Ontology Language: Primer*. Available at http://www.w3.org/TR/owl2-primer/. W3C Recommendation (cited on pages 18, 31).
- Hitzler, Pascal, Markus Krötzsch and Sebastian Rudolph (2009). *Foundations of Semantic Web Technologies*. Chapman & Hall/CRC (cited on pages 13, 17).
- Hogan, Aidan (2011). "Exploiting RDFS and OWL for Integrating Heterogeneous, Large-Scale, Linked Data Corpora". Available from http://aidanhogan.com/docs/thesis/. PhD thesis. Digital Enterprise Research Institute, National University of Ireland, Galway (cited on page 131).
- Horridge, Matthew and Sean Bechhofer (2011). "The OWL API: A Java API for OWL Ontologies". In: *Semantic Web Journal* 2.1. Special Issue on Semantic Web Tools and Systems, pages 11–21. DOI: 10.3233/SW-2011-0025 (cited on page 57).
- Horrocks, Ian and Peter F. Patel-Schneider (2004). "A Proposal for an OWL Rules Language". In: *Proceedings* of the 13th International Conference on World Wide Web (WWW'04), pages 723–731. DOI: 10.1145/988672.9 88771 (cited on page 75).
- Horrocks, Ian, Peter F. Patel-Schneider, Harold Boley, Said Tabet, Benjamin N. Grosof and Mike Dean, editors (2004). SWRL: A Semantic Web Rule Language. Available at http://www.w3.org/Submission/SWRL/. W3C Member Submission (cited on pages 66, 75).
- Hümmer, Wolfgang, Andreas Bauer and Gunnar Harde (2003). "XCube: XML for Data Warehouses". In: *Proceedings of the 6th ACM International Workshop on Data Warehousing and OLAP (DOLAP'03)*. DOI: 10.114 5/956060.956067 (cited on page 129).

- Ianni, Giovambattista, Alessandra Martello, Claudio Panetta and Giorgio Terracina (2009). "Efficiently Querying RDF(S) Ontologies with Answer Set Programming". In: *Journal of Logic and Computation* 19.4, pages 671– 695. DOI: 10.1093/logcom/exn043 (cited on page 109).
- Isele, Robert, Jürgen Umbrich, Christian Bizer and Andreas Harth (2010). "LDspider: An open-source crawling framework for the Web of Linked Data". In: Proceedings of the 9th International Semantic Web Conference (ISWC'10) Posters and Demos. CEUR Workshop Proceedings 658, pages 29–32. URL: http://ceur-ws.org/Vol-658/paper495.pdf (cited on page 154).
- Janowicz, Krzysztof, Frank van Harmelen, James A Hendler and Pascal Hitzler (2015). "Why the Data Train Needs Semantic Rails". In: *AI Magazine* 36.1, pages 5–14. DOI: 10.1609/aimag.v36i1.2560 (cited on page 3).
- Kaminski, Mark, Egor V. Kostylev and Bernardo Cuenca Grau (2017). "Query Nesting, Assignment, and Aggregation in SPARQL 1.1". In: *ACM Transactions on Database Systems* 42.3, 17:1–17:46. DOI: 10.1145/3083898 (cited on page 17).
- Kämpgen, Benedikt and Richard Cyganiak, editors (2013). *Use Cases and Lessons for the Data Cube Vocabulary*. Available at https://www.w3.org/TR/vocab-data-cube-use-cases/. W3C Working Group Note (cited on page 131).
- Kämpgen, Benedikt, Seán O'Riain and Andreas Harth (2012). "Interacting with Statistical Linked Data via OLAP Operations". In: *Proceedings of the 9th Extended Semantic Web Conference (ESWC'12)*. Volume 7295. Lecture Notes in Computer Science, pages 87–101. DOI: 10.1007/978-3-662-46641-4_7 (cited on pages 84, 137).
- Kämpgen, Benedikt, Steffen Stadtmüller and Andreas Harth (2014). "Querying the Global Cube: Integration of Multidimensional Datasets from the Web". In: *Proceedings of the 19th International Conference on Knowledge Engineering and Knowledge Management (EKAW'14)*, pages 250–265. DOI: 10.1007/978-3-319-13704-9 _20 (cited on pages 91, 93, 96, 136, 137).
- Kay, Michael, Norman Walsh, Ashok Malhotra and Jim Melton, editors (2010). XQuery 1.0 and XPath 2.0 Functions and Operators. 2nd edition. W₃C Recommendation. URL: http://www.w3.org/TR/xpath-functions/ (cited on page 110).
- Keet, C. Maria, Agnieszka Ławrynowicz, Claudia d'Amato, Alexandros Kalousis, Phong Nguyen, Raul Palma, Robert Stevens and Melanie Hilario (2015). "The Data Mining OPtimization Ontology". In: *Journal of Web Semantics* 32, pages 43–53. ISSN: 1570-8268. DOI: 10.1016/j.websem.2015.01.001 (cited on pages 120, 144).
- Kimball, Ralph and Margy Ross (2013). *The Data Warehouse Toolkit: The Definitive Guide to Dimensional Modeling*. 3rd edition. John Wiley & Sons (cited on page 141).
- Klein, Michel, Dieter Fensel, Frank van Harmelen and Ian Horrocks (2001). "The Relation between Ontologies and Schema-Languages". In: *Linköping Electronic Articles in Computer and Information Science* 6.4. URL: http://www.ep.liu.se/ea/cis/2001/004/ (cited on page 130).
- Klyne, Graham, Jeremy J. Carroll and Brian McBride, editors (2014). *RDF 1.1 Concepts and Abstract Syntax*. Available at https://www.w3.org/TR/rdf11-concepts/. W3C Recommendation (cited on pages 11, 22).
- Knublauch, Holger, Dean Allemang and Simon Steyskal, editors (2017). *SHACL Advanced Features*. Available at https://www.w3.org/TR/shacl-af/. W3C Working Group Note (cited on page 110).
- Knublauch, Holger, James A. Hendler and Kingsley Idehen, editors (2011). *SPIN Overview and Motivation*. Available at https://www.w3.org/Submission/spin-overview/. W3C Member Submission (cited on page 110).

- Kontchakov, Roman, Carsten Lutz, David Toman, Frank Wolter and Michael Zakharyaschev (2011). "The Combined Approach to Ontology-Based Data Access". In: *Proceedings of the 22nd International Joint Conference on Artificial Intelligence (IJCAI'11)*, pages 2656–2661 (cited on page 140).
- Kontchakov, Roman, Mariano Rodriguez-Muro and Michael Zakharyaschev (2013). "Ontology-Based Data Access with Databases: A Short Course". In: *Reasoning Web International Summer School (RW'13)*. Volume 8067. Lecture Notes in Computer Science, pages 194–229. DOI: 10.1007/978-3-642-39784-4_5 (cited on pages 22, 29).
- Koren, Yehuda (2009). "The BellKor Solution to the Netflix Grand Prize". In: *Netflix prize documentation* 81. Available at http://www.netflixprize.com/assets/GrandPrize2009_BPC_BellKor.pdf, pages 1–10 (cited on page 132).
- Krötzsch, Markus (2012). "OWL 2 Profiles: An Introduction to Lightweight Ontology Languages". In: *Reasoning Web International Summer School (RW'12)*, pages 112–183. DOI: 10.1007/978-3-642-33158-9_4 (cited on page 22).
- Ku, Harry H. (1966). "Notes on the Use of Propagation of Error Formulas". In: *Journal of Research of the National Bureau of Standards* 70C (4), pages 263–273. DOI: 10.6028/jres.070C.025 (cited on page 105).
- Lange, Christoph (2013). "Ontologies and Languages for Representing Mathematical Knowledge on the Semantic Web". In: *Semantic Web* 4.2, pages 119–158. DOI: 10.3233/SW-2012-0059 (cited on page 109).
- Lebo, Timothy, Deborah McGuinness and Satya Sahoo, editors (2013). *PROV-O: The PROV Ontology*. Available at http://www.w3.org/TR/prov-o/. W3C Recommendation (cited on pages 24, 84).
- Lenzerini, Maurizio (2002). "Data Integration: A Theoretical Perspective". In: *Proceedings of the 21st Symposium on Principles of Database Systems (PODS'02)*, pages 233–246. DOI: 10.1145/543613.543644 (cited on page 130).
- Lutz, Carsten, Inanç Seylan, David Toman and Frank Wolter (2013). "The Combined Approach to OBDA: Taming Role Hierarchies using Filters". In: *Proceedings of the 12th International Semantic Web Conference (ISWC'13)*. Volume 8218. Lecture Notes in Computer Science, pages 314–330. DOI: 10.1007/978-3-642-41335 -3_20 (cited on page 56).
- Ma, Li, Yang Yang, Zhaoming Qiu, Guotong Xie, Yue Pan and Shengping Liu (2006). "Towards a Complete OWL Ontology Benchmark". In: *Proceedings of the 3rd European Semantic Web Conference (ESWC'06)*. Lecture Notes in Computer Science, pages 125–139. DOI: 10.1007/11762256_12 (cited on page 56).
- Mercer (2017). *Quality of Living City Rankings*. URL: http://mercer.com/qol (visited on 14th Feb. 2017) (cited on page 4).
- Moreau, Luc and Paul Groth (2013). *Provenance: An Introduction to PROV*. Volume 3. Synthesis Lectures on the Semantic Web: Theory and Technology 4. Morgan & Claypool Publishers. DOI: 10.2200/S00528ED1V01 Y201308WBE007 (cited on page 25).
- Motik, Boris, Bernardo Cuenca Grau, Ian Horrocks, Zhe Wu, Achille Fokoue and Carsten Lutz, editors (2009). *OWL 2 Web Ontology Language: Profiles*. Available at http://www.w3.org/TR/owl2-profiles/. W3C Recommendation (cited on pages 18, 21, 30–32).
- Motik, Boris, Ulrike Sattler and Rudi Studer (2005). "Query Answering for OWL DL with Rules". In: *Journal* of Web Semantics 3.1, pages 41–60. DOI: 10.1016/j.websem.2005.05.001 (cited on pages 66, 75).
- Muñoz, Sergio, Jorge Pérez and Claudio Gutiérrez (2007). "Minimal Deductive Systems for RDF". In: *Proceedings of the 4th European Semantic Web Conference (ESWC'07)*. Volume 4519. Lecture Notes in Computer Science, pages 53–67. DOI: 10.1007/978-3-540-72667-8_6 (cited on page 31).

- Naisbitt, John (1982). *Megatrends: Ten New Directions Transforming Our Lives*. 1st edition. Warner Books. ISBN: 0446512516 (cited on page 3).
- Neumaier, Sebastian, Jürgen Umbrich, Josiane Xavier Parreira and Axel Polleres (2016). "Multi-level Semantic Labelling of Numerical Values". In: *Proceedings of the 15th International Semantic Web Conference (ISWC'16) Part I.* Volume 9981. Lecture Notes in Computer Science, pages 428–445. DOI: 10.1007/978-3-319-46523-4 _26 (cited on page 132).
- Neumaier, Sebastian, Jürgen Umbrich and Axel Polleres (2016). "Automated Quality Assessment of Metadata across Open Data Portals". In: *ACM Journal of Data and Information Quality* 8.1, 2:1–2:29. DOI: 10.1145/29 64909 (cited on page 84).
- Ngomo, Axel-Cyrille Ngonga, Sören Auer, Jens Lehmann and Amrapali Zaveri (2014). "Introduction to Linked Data and Its Lifecycle on the Web". In: *Proceedings of the 10th International Summer School 2014*, pages 1–99. DOI: 10.1007/978-3-642-39784-4_1 (cited on page 130).
- Niinimäki, Marko and Tapio Niemi (2009). "An ETL Process for OLAP Using RDF/OWL Ontologies". In: *Journal on Data Semantics* 13, pages 97–119. DOI: 10.1007/978-3-642-03098-7_4 (cited on page 131).
- Noy, Natalya F. (2004). "Semantic Integration: A Survey of Ontology-based Approaches". In: *ACM SIGMOD Record* 33.4, pages 65–70. DOI: 10.1145/1041410.1041421 (cited on page 18).
- Office for Official Publications of the European Communities (2004). *Urban Audit. Methodological Handbook.* Available at http://ec.europa.eu/eurostat/en/web/products-manuals-and-guidelines/-/KS-BD-04-002. ISBN: 9289470798 (cited on pages 88, 132, 143).
- Parsia, Bijan and Uli Sattler (2012). *OWL 2 Web Ontology Language Data Range Extension: Linear Equations*. Available at https://www.w3.org/TR/owl2-dr-linear/. W3C Working Group Note (cited on pages 78, 110).
- Patel-Schneider, Peter F. and Boris Motik, editors (2009). OWL 2 Web Ontology Language: Mapping to RDF Graphs. Available at http://www.w3.org/TR/owl2-mapping-to-rdf/. W3C Recommendation (cited on pages 20, 31).
- Paulheim, Heiko (2017). "Knowledge Graph Refinement: A Survey of Approaches and Evaluation Methods". In: *Semantic Web* 8.3, pages 489–508. DOI: 10.3233/SW-160218 (cited on page 132).
- Paulheim, Heiko and Johannes Fürnkranz (2012). "Unsupervised Generation of Data Mining Features from Linked Open Data". In: Proceedings of the 2nd International Conference on Web Intelligence, Mining and Semantics (WIMS'12), page 31. DOI: 10.1145/2254129.2254168 (cited on page 154).
- Pérez, Jorge, Marcelo Arenas and Claudio Gutierrez (2009). "Semantics and Complexity of SPARQL ". In: ACM Transactions on Database Systems 34.3, pages 1–45. DOI: 10.1145/1567274.1567278 (cited on pages 15, 16, 48, 140).
- (2010). "nSPARQL: A Navigational Language for RDF". In: *Journal of Web Semantics* 8.4, pages 255–270.
 DOI: 10.1016/j.websem.2010.01.002 (cited on pages 44, 135).
- Pérez, Juan Manuel, Rafael Berlanga Llavori, María José Aramburu and Torben Bach Pedersen (2008). "Integrating Data Warehouses with Web Data: A Survey". In: *IEEE Transactions on Knowledge and Data Engineering* 20.7, pages 940–955. DOI: 10.1109/TKDE.2007.190746 (cited on page 129).
- Pérez-Urbina, Héctor, Ian Horrocks and Boris Motik (2009). "Practical Aspects of Query Rewriting for OWL
 2". In: Proceedings of the OWLED 2009 Workshop on OWL: Experiences and Directions. CEUR Workshop
 Proceedings 529. URL: http://ceur-ws.org/Vol-529/owled2009_submission_17.pdf (cited on page 56).

- Pérez-Urbina, Héctor, Boris Motik and Ian Horrocks (2010). "Tractable Query Answering and Rewriting Under Description Logic Constraints". In: *Journal of Applied Logic* 8.2, pages 186–209. DOI: 10.1016/j.jal.2009.09 .004 (cited on pages 29, 55, 140).
- Perry, Matthew and John Herring (2012). OGC GeoSPARQL-A Geographic Query Language for RDF Data. OGC Implementation Standard OGC 11-052r4. Open Geospatial Consortium. URL: http://www.opengis.net/doc/I S/geosparql/1.0 (cited on page 110).
- Poggi, Antonella, Domenico Lembo, Diego Calvanese, Giuseppe De Giacomo, Maurizio Lenzerini and Riccardo Rosati (2008). "Linking Data to Ontologies". In: *Journal on Data Semantics X*. Volume 4900. Lecture Notes in Computer Science, pages 133–173. DOI: 10.1007/978-3-540-77688-8_5 (cited on pages 20, 67).
- Polleres, Axel, François Scharffe and Roman Schindlauer (2007). "SPARQL++ for Mapping between RDF Vocabularies". In: Proceedings of the 6th International Conference on Ontologies, DataBases, and Applications of Semantics (ODBASE'07) Part I. Volume 4803. Lecture Notes in Computer Science, pages 878–896. DOI: 10.1007/978-3-540-76848-7_59 (cited on page 99).
- Polleres, Axel and Johannes Wallner (2013). "On the Relation Between SPARQL 1.1 and Answer Set Programming". In: *Journal of Applied Non-Classical Logics (JANCL)* 23 (1-2). Special Issue on Equilibrium Logic and Answer Set Programming, pages 159–212. DOI: 10.1080/11663081.2013.798992 (cited on pages 16, 102).
- Posada-Sánchez, Mónica, Stefan Bischof and Axel Polleres (2016). "Extracting Geo-Semantics About Cities From OpenStreetMap". In: Proceedings of the Posters and Demos Track of the 12th International Conference Semantic Systems (SEMANTiCS'16). CEUR Workshop Proceedings 1695. URL: http://ceur-ws.org/Vol-1695/p aper39.pdf (cited on page 143).
- Prud'hommeaux, Eric and Andy Seaborne, editors (2008). *SPARQL Query Language for RDF*. Available at http://www.w3.org/TR/rdf-sparql-query/. W₃C Recommendation (cited on pages 17, 29).
- Pyle, Dorian (1999). Data Preparation for Data Mining. Morgan Kaufmann (cited on page 3).
- R Core Team (2017). *R: A Language and Environment for Statistical Computing*. R Foundation for Statistical Computing. URL: https://www.R-project.org/ (visited on 12th Oct. 2017) (cited on page 119).
- Ralph Hodgson, Paul J. Keller (2011). *QUDT Quantities, Units, Dimensions and Data Types in OWL and XML.* URL: http://www.qudt.org/ (cited on pages 78, 95, 110).
- Raskin, Robert G. and Michael J. Pan (2005). "Knowledge Representation in the Semantic Web for Earth and Environmental Terminology (SWEET)". In: *Journal of Computers and Geosciences* 31.9, pages 1119–1125. DOI: 10.1016/j.cage0.2004.12.004 (cited on page 110).
- Rijgersberg, Hajo, Mark van Assem and Jan Top (2013). "Ontology of Units of Measure and Related Concepts". In: *Semantic Web* 4.1. DOI: 10.3233/SW-2012-0069 (cited on pages 78, 110).
- Rodriguez-Muro, Mariano, Roman Kontchakov and Michael Zakharyaschev (2013). "Ontology-Based Data Access: Ontop of Databases". In: *Proceedings of the 12th International Semantic Web Conference (ISWC'13)*. Volume 8218. Lecture Notes in Computer Science, pages 558–573. DOI: 10.1007/978-3-642-41335-3_35 (cited on pages 29, 56).
- Rosati, Riccardo (2012). "Prexto: Query Rewriting under Extensional Constraints in DL-Lite". In: *Proceedings* of the 9th Extended Semantic Web Conference (ESWC'12). Volume 7295. Lecture Notes in Computer Science, pages 360–374. DOI: 10.1007/978-3-642-30284-8_31 (cited on page 140).
- Rosati, Riccardo and Alessandro Almatelli (2010). "Improving Query Answering over DL-Lite Ontologies". In: *Proceedings of the 12th International Conference on Principles of Knowledge Representation and Reasoning (KR'10)*, pages 290–300 (cited on page 140).

- Roweis, Sam T. (1997). "EM Algorithms for PCA and SPCA". In: *Proceedings of the 10th International Conference on Neural Information Processing Systems (NIPS'97)*, pages 626–632 (cited on pages 116, 117, 132).
- Sánchez A, V. David (2003). "Advanced Support Vector Machines and Kernel Methods". In: *Neurocomputing* 55.1, pages 5–20. DOI: 10.1016/S0925-2312(03)00373-4 (cited on page 143).
- Santos, Henrique, Victor Dantas, Vasco Furtado, Paulo Pinheiro and Deborah L. McGuinness (2017). "From Data to City Indicators: A Knowledge Graph for Supporting Automatic Generation of Dashboards". In: *Proceedings of the 14th International Conference (ESWC'17) Part II*, pages 94–108. DOI: 10.1007/978-3-319-58 451-5_7 (cited on pages 125, 129).
- Schmidt, Michael, Michael Meier and Georg Lausen (2010). "Foundations of SPARQL Query Optimization". In: *Proceedings of the 13th International Conference on Database Theory (ICDT'10)*, pages 4–33. DOI: 10.1145 /1804669.1804675 (cited on pages 48, 140).
- Schutt, Rachel and Cathy O'Neil (2013). *Doing Data Science: Straight Talk from the Frontline*. O'Reilly Media, Inc. ISBN: 1449358659 (cited on page 3).
- Shlens, Jonathon (2014). "A Tutorial on Principal Component Analysis". In: arXiv: 1404.1100 [cs.LG] (cited on page 132).
- Siegel, Michael, Edward Sciore and Arnon Rosenthal (1994). "Using Semantic Values to Facilitate Interoperability Among Heterogeneous Information Systems". In: ACM Transactions on Database Systems (TODS) 19.2. DOI: 10.1145/176567.176570 (cited on page 129).
- Sirin, Evren, Bijan Parsia, Bernardo Cuenca Grau, Aditya Kalyanpur and Yarden Katz (2007). "Pellet: A Practical OWL-DL Reasoner". In: *Journal of Web Semantics* 5.2, pages 51–53. DOI: 10.1016/j.websem.2007.03.004 (cited on page 75).
- Stadler, Claus, Jens Lehmann, Konrad Höffner and Sören Auer (2012). "LinkedGeoData: A Core for a Web of Spatial Open Data". In: *Semantic Web* 3.4, pages 333–354. DOI: 10.3233/SW-2011-0052 (cited on page 143).
- Stadtmüller, Steffen, Sebastian Speiser, Andreas Harth and Rudi Studer (2013). "Data-Fu : A Language and an Interpreter for Interaction with Read / Write Linked Data". In: *Proceedings of the 22nd International Conference on World Wide Web (WWW'13)*. DOI: 10.1145/2488388.2488495 (cited on pages 85, 154).
- Stevens, Stanley Smith (1946). "On the Theory of Scales of Measurement". In: *Science* 103.2684, pages 677–680. DOI: 10.1126/science.103.2684.677 (cited on page 141).
- Switzer, Fred S. and Philip L. Roth (2008). "Coping with Missing Data". In: *Handbook of Research Methods in Industrial and Organizational Psychology*, pages 310–323. ISBN: 978-1-4051-2700-4 (cited on page 132).
- The Economist Intelligence Unit (2012). *The Green City Index: A summary of the Green City Index research series*. Siemens AG. URL: https://www.siemens.com/entry/cc/features/greencityindex_international/all/en/pdf /gci_report_summary.pdf (visited on 10th Oct. 2017) (cited on pages 4, 76, 83).
- (2017). Global Livability Ranking 2016. URL: https://www.eiu.com/liveability2016 (visited on 14th Feb. 2017) (cited on page 4).
- Thellmann, Klaudia, Michael Galkin, Fabrizio Orlandi and Sören Auer (2015). "LinkDaViz Automatic Binding of Linked Data to Visualizations". In: *Proceedings of the 14th International Semantic Web Conference* (*ISWC'15*) Part I. Volume 9367. Lecture Notes in Computer Science. Springer, pages 147–162. DOI: 10.1007 /978-3-319-25007-6_9 (cited on page 141).

- United Nations (2015a). *Transforming our world: The 2030 Agenda for Sustainable Development*. General Assempbly, A/RES/70/1. URL: https://sustainabledevelopment.un.org/post2015/transformingourworld/publicatio n (visited on 12th Oct. 2017) (cited on pages 4, 88).
- (2015b). World Urbanization Prospects: The 2014 Revision, (ST/ESA/SER.A/366). Department of Economic and Social Affairs. United Nations. ISBN: 978-92-1-151517-6 (cited on page 4).
- U.S. Census Bureau (2007). County and City Data Book 2007. 14th edition. ISBN: 0-16-079598-5 (cited on page 142).
- Vandenbussche, Pierre-Yves, Ghislain A Atemezing, María Poveda-Villalón and Bernard Vatant (2017). "Linked Open Vocabularies (LOV): a Gateway to Reusable Semantic Vocabularies on the Web". In: *Semantic Web Journal* 8.3, pages 437–452. DOI: 10.3233/SW-160213 (cited on page 23).
- Varga, Jovan, Alejandro A. Vaisman, Oscar Romero, Lorena Etcheverry, Torben Bach Pedersen and Christian Thomsen (2016). "Dimensional Enrichment of Statistical Linked Open Data". In: *Journal of Web Semantics* 40, pages 22–51. DOI: 10.1016/j.websem.2016.07.003 (cited on page 141).
- Vassiliadis, Panos and Timos Sellis (1999). "A Survey of Logical Models for OLAP Databases". In: ACM SIG-MOD Record 28 (4). DOI: 10.1145/344816.344869 (cited on page 130).
- Vrandečić, Denny and Markus Krötzsch (2014). "Wikidata: A Free Collaborative Knowledgebase". In: *Communications of the ACM* 57.10, pages 78–85. DOI: 10.1145/2629489 (cited on page 143).
- Vrandečić, Denny, Christoph Lange, Michael Hausenblas, Jie Bao and Li Ding (2010). "Semantics of Governmental Statistics Data". In: *Proceedings of the WebSci10*. Available at http://journal.webscience.org/400/ (cited on page 131).
- West, Mike, P. Jeff Harrison and Helio S. Migon (1985). "Dynamic Generalized Linear Models and Bayesian Forecasting". In: *Journal of the American Statistical Association* 80.389, pages 73–83 (cited on page 143).
- Witten, Ian H. and Eibe Frank (2011). *Data Mining: Practical Machine Learning Tools and Techniques*. 3rd edition. Morgan Kaufmann Publishers Inc. ISBN: 9780123748560 (cited on page 115).
- Wood, David, Marsha Zaidman, Luke Ruth and Michael Hausenblas (2013). *Linked Data: Structured Data on the Web*. Manning. ISBN: 9781617290398 (cited on page 25).
- OWL Working Group, W₃C (2009). *OWL 2 Web Ontology Language: Document Overview*. Available at http: //www.w3.org/TR/owl2-overview/. W₃C Recommendation (cited on pages 17, 22).
- Zhou, Yujiao, Bernardo Cuenca Grau, Yavor Nenov, Mark Kaminski and Ian Horrocks (2015). "PAGOdA: Pay-As-You-Go Ontology Query Answering Using a Datalog Reasoner". In: *Journal of Artificial Intelligence Research* 54, pages 309–367. DOI: 10.1613/jair.4757 (cited on page 56).

Curriculum Vitae

Name:	Stefan Bischof
Degrees:	Diplom-Ingenieur (equivalent to Master of Science)
	Bakk. techn. (equivalent to Bachelor of Science)
Languages:	German (native), English (fluently)
E-Mail:	stefan.bischof@alumni.tuwien.ac.at

Education

03/2012–present	PhD study Computer Science
	Vienna University of Technology, Austria
	Thesis: "Complementary Methods for the Enrichment of Linked Data"
03/2007-11/2010	Master study Information & Knowledge Management
	Vienna University of Technology, Austria
	Thesis: "Implementation and Optimisation of Queries in XSPARQL"
03/2003-03/2007	Bachelor study Software & Information Engineering
	Vienna University of Technology, Austria
09/1997-07/2002	Secondary school Höhere Technische Lehranstalt Rankweil, Austria

Professional Experience

03/2012–present	Siemens AG Österreich, Corporate Technology, Austria
	Research Scientist at Corporate Technology
	Topics: Semantic Web Technologies
06/2014-09/2015	Institute for Information Business at Vienna University of Economics, Austria
	Project Assistant at the Data and Knowledge Engineering Group
	Topics: Semantic Web Technologies, Description Logics, Databases
10/2012-05/2014	Institute of Information Systems, Vienna University of Technology, Austria
	Project Assistant at the Database and Artificial Intelligence Group
	Topics: Semantic Web Technologies, Description Logics, Databases
12/2010-02/2012	Digital Enterprise Research Institute at National University of Ireland, Galway
	Researcher at the Unit for Querying and Reasoning
	Topics: XSPARQL specification, implementation, and optimization

05/2009-08/2009	Digital Enterprise Research Institute at National University of Ireland, Galway
	Research Intern for Master Thesis, XSPARQL Implementation in Java
Summer 2008	BOC Information Systems, Vienna, Austria
	Software Design and Development, Browser based test automation
Summer 2007	Julius Blum GmbH, Höchst, Austria
	Software Design and Development, Data Migration with XSLT
Summer 2005	OMICRON electronics GmbH, Klaus in Vorarlberg, Austria
	Software Design and Development, Parser
Summer 2004	Weber Informatik Lösungen, Göfis, Austria
	Software Development, End user systems

Selected Peer-Reviewed Publications

- Bischof, Stefan, Stefan Decker, Thomas Krennwallner, Nuno Lopes and Axel Polleres (2012). "Mapping between RDF and XML with XSPARQL". In: *Journal on Data Semantics* 1.3, pages 147–185. DOI: 10.1007/s13740-012-0008-7.
- Bischof, Stefan, Andreas Harth, Benedikt Kämpgen, Axel Polleres and Patrik Schneider (2017). "Enriching Integrated Statistical Open City Data by Combining Equational Knowledge and Missing Value Imputation". In: *Journal of Web Semantics: Special Issue on Semantic Statistics*. Preprint available at http://www.websemanticsjournal.or g/index.php/ps/article/view/509. DOI: 10.1016/j.websem.2017.09.003.
- Bischof, Stefan, Markus Krötzsch, Axel Polleres and Sebastian Rudolph (2014). "Schema-Agnostic Query Rewriting in SPARQL 1.1". In: *Proceedings of the 13th International Semantic Web Conference (ISWC'14)*. Volume 8796. Lecture Notes in Computer Science, pages 584–600. DOI: 10.1007/978-3-319-11964-9_37.
- Bischof, Stefan and Axel Polleres (2013). "RDFS with Attribute Equations via SPARQL Rewriting". In: *Proceedings of the 10th ESWC (ESWC'13)*. Volume 7882. Lecture Notes in Computer Science, pages 335–350. DOI: 10.1007/978-3-642-38288-8_23.